

The
SCIENCE of CHANGERING

by

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Hon. Member Central Council of Church
Bell Ringers.

with a foreword.

by

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Method Construction, which is the subject treated in the following pages, has been Mr. Trollope's special study for many years. It would indeed be hardly an exaggeration to say that he is almost alone among modern experts in this particular investigation. This statement will doubtless at first meet with the challenge of strong incredulity on the part of the reader. He will naturally recall the vast interest that the theory of bell-ringing has inspired during recent years, and the enormous number of new Methods that have been discovered and published. A little further thought should make my meaning clearer and and perhaps convince the objector that the statement is not unjustified.

The contemporary expert has not altogether escaped the consequences of contact with an utilitarian age. His time and his labour have been expended on the composition of peals of record length or such as possess musical or other qualities never before obtained. His efforts to evolve new Methods or extensions of old Methods have been directed by the desire to discover something more interesting or more difficult to ring than has been previously available in this belfry. If in the course of his work he has given thought to the construction of Methods or the correct manner in which they may be theoretically extended this has been incidental and generally speaking subservient

to the practical side of the art. In other words he has concerned himself with concrete figures and abjured abstract thought. Even at the moment when he is dealing with theory he is obsessed with the thought of practice, and as an almost inevitable result immediately his investigation brings him to a point where theory appears to conflict with practice he will be apt to drop the theory as useless. It may be a hard saying, but procedure such as I have outlined here bars the way absolutely against knowledge of the principles that underly the science of change-ringing, and so long as it is persisted in there can be no true vision. The trees block out the sight of the wood.

What then is it, that M^r. Trollope has done, or ^{at} any rate what has he tried to do? Wherein does his procedure differ from that of other authorities in modern times? Simply in this. He has put theory in the foreground. His mind has dwelt on abstractions rather than the concrete. Thus, for example, instead of experimenting with the figures of individual Methods to see where they will lead him, he has sought for the links that bind all Methods together, legitimate or illegitimate, regular or irregular.

It will be observed that he bases his reasoning on the axiomatic statement that all change-ringing consists of

relative movement. Some readers may be inclined to regard this axiom as a platitude of little meaning or worth. If they will consider seriously what it means and will follow consistently the road along which it takes them, they may probably find it difficult to deny the conclusions that are drawn from it in the following pages.

An objection that will rise to the minds of many readers consists in the occurrence of numerous examples of Methods that are unsuitable for practical ringing, either because they are unsymmetrical or on other accounts. But this objection falls to the ground when it is recognised why these particular

illustrations are chosen. Speaking generally M^r Trollope is not concerned in producing ringable Methods or ringable extensions of existing Methods, but in shewing the true principles of construction and extension. His purpose is to make known to the Exercise what may be called the scientific elements of which all Methods, legitimate or otherwise are compounded, and the ways in which ~~a~~ given^a set of figures on (say) 6 bells, these figures may or may not be extended in true Mathematical Series.

Arising out of this objection a further question may conceivably occur to the mind. Why bother about these useless Methods and Extensions at all? What we need are

Methods we can ring; we do not want to waste our time over so-called Methods that are of no practical value. The answer to this is that it is only by ignoring all accidental and artificial rules (such e.g. as that a bell must not strike more than 2 blows consecutively in one position) that the real foundations of change-ringing can be unearthed. When this process has been performed, it will become a comparatively simple business to select the Method or the Extension for practice in the Tower.

The importance of arriving at a sound conclusion on the actual foundations of change-ringing will be denied by no intelligent reader.

If Mr. Trollope is right, the consequences must be far reaching. Henceforth an acid test will be available to settle definitively whether (say) figures put forth as purporting to be Superlative Maximes are or are not a true extension of the Major. What is called the Bot Major Lead End will cease to be the subject of rancorous debate, and many other problems will receive their appropriate solution.

One further warning note must be struck. There are two ways in which the questions dealt with here can be approached. They can be worked out deductively after the manner of the Mathematician, or they can be argued as the logician argues in accordance

with inductive reasoning. The latter is Mr. Trollope's method. And it is just because most ringing experts try - with greater or less success - to follow the mathematician's methods that the caution is needed. Every one knows that if in a chain of mathematical or deductive reasoning a single link gives way the whole is naught; and those whose training has been on the lines of the mathematician or natural scientist are prone to imagine that the same thing must apply to every kind of argument. But this is by no means necessarily the case where the reasoning is inductive.

Of this an excellent example

is the case in the Law Courts built up on what is known as circumstantial evidence. So far from it being essential that every single item of testimony should be true, it may even conceivably happen that there is no one single piece of evidence which taken by itself is vital. The conclusiveness of the case presented depends on the evidence as a whole, so that taking it all in all no other verdict is reasonably possible.

The reader may and probably will find isolated statements in the following pages whose truth he is tempted to doubt. He is not on that account to be unduly critical. Still less must he thereupon condemn the whole. It is

only after he has read the complete argument and grasped its bearing in all respects that he will be able to form a sound judgment on its constituent parts.

When he has reached this stage I would ask him to put two questions to himself. First, is there or is there not an inner unity whereby ringing is bound together in a single science, and secondly, if there be such unity can it be of a different character speaking generally from that which is set out in the pages of this book?

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For Stedman read
Richard Duckworth I had
not then discerned the true
authorship of the Tintinnalogia

TINTINNALOGIA Pt. Stedman, I take it,
uses the word "invented" in its original
meaning i.e. as the equivalent of "introduced"
and not, as is common today, as practically
the same thing as "created"

cf. SHAKESPEARE'S Henry IV ii Act III, & II.

1.

The Science of Change Ringing.

Chapter I The Axiom

The beginning of ringing was natural and spontaneous; it was in no sense the invention of one man or one band. Exactly when it happened we do not know, but by the middle of the XVIIth century it was practised in many parts of England. The earliest date is that of the "invention" of the Sixes which Stedman says took place about 1600. Thence forward development was steady and continuous.

And the beginning of ringing was not among educated or particularly intellectual men. It sprang up among the common people of widely scattered towns and villages. Such people, as a class could neither read nor write, and means of personal communication between

I know now a good deal
more about singing history.
College singing was invented probably
at the Universities and Inns of Court.

12th of 22nd Henry VIII ; 25th of 27th Henry VIII
151 Edward VI also other Acts of Ed VI and Elizabeth.
See Froude J.R. Green etc.

places separated by more than the shortest
distances were so scanty as to be for
the great majority of men practically
non-existent. Stage coaches, to say nothing
of railway trains, were as yet unknown,
the badness of it all but a few main
roads prevented all vehicular traffic;
to ride horseback was the privilege of
the few; the many had perforce to
go afoot. Now were there the only
determents to travel. Savage vagrancy
Acts forbade anything like free migration
of labour from place to place; while a
"Host of broken men" and "sturdy beggars",
infested the roads the result of the social
religious, and political changes of the time
infested the highways and made travel
dangerous and precarious.

In these days of railway trains, cycles
and motors; of daily almost hourly posts;
of associations and guilds; of frequent
meetings and combined practices; with
a weekly ringing newspaper and a
Central Council; when ringers in all
parts of the country can look on each
other as personal acquaintances and
friends; when the Exercise is in reality

a unit - in these days it is rather difficult to grasp the idea of an Exercise consisting of independent and isolated units, where each tower, or perhaps each small group of towers, had to learn and develop its ringing by its own abilities and without any aid from outsiders.

It was, however, in such an Exercise that ringing began. And the remarkable fact is that, begun in this fashion, it was always the same thing. From small beginnings development started here more rapidly, there slower; But the developments were always in exactly the same direction. Not only so, but great as has been the development during the last three centuries ringing has throughout remained essentially the same thing. There are two great landmarks in its development. The first is the "invention of the Sixes." Somewhere about 1600; the other is the introduction of Crown Peals rather less than a hundred years later. Once the Exercise had reached these points it did not go back again. But from 1700 not

"Tintinnalogia" page 44. "Crown Peals" were known in 1667 and probably some years before. Plain Changes were abandoned by advanced ringers not many years later and died out except in the degraded form of Call Changes. Note that

Plain Changes were strictly scientific in their structure and contain the germs of all modern Method and peal Composition

Note "Cross Peals" was the original term used for Ringing in which every bell is continually moving in contradistinction to Plain Changes in which one pair of bells only is changed at a time.

I should have written the word "principle" instead of "idea" but that "principle" is used in ringing with a technical meaning and it is well to avoid any chance of confusion.

only is the general character of ringing unalterably fixed, but the Standard Methods, in which more than nine^{also} tenths of ringing is done, are fixed, and there is no likelihood whatever that any change or further development will, or can, displace them.

If by any chance one of John Barthon's band could once again find himself in the city of Norwich he would, even in that city, which more than any other has preserved outward links with the past, find himself in an absolutely new world. Only when once more he entered Mancroft belfry would he be at home. Gone indeed are the bells he knew, but he could still take his rope in Plain Bob or Grandeur or Stedman or Treble Bob just as he did more than five hundred years ago.

Now all this points conclusively and inevitably to one thing. There must have been, and there must be, one simple obvious and strong idea at the root of ringing which could thus create and develop in one strait fixed path. Simple and obvious to appeal to

appeal unconsciously to ordinary unlettered men. Strong enough to override all other ideas, to be proof against all changes of time, and different mens fancies. Alive enough to develop ringing from small beginnings to a complex science.

Such an idea must have its foundation in some great principle of natural law and it and it alone can supply the axioms on which we must build up the Science of Ringing.

Originally ringing was in England what it still is in France and other countries, the more or less promiscuous sounding of bells without much regard for either time or tune. From this it developed into a kind of sport, the attraction of the sport consisting in the strength and skill required to ring bells "up" with the faulty and imperfect hangings. This, naturally, produced "round ringing" and developed a sense of rhythm and good sticking. Then there came the time when, in different parts of the country, if one ringer said to another in so many words "Let's have some variety. Change places with me." And, at the moment that was said, change ringing,

"A Change is made between two Bells that strikes next to each other by removing into each others

places" Steadman "Tintinnalogia" page 3.

See Article Bell News. Sep 15. 1915 by J.A.T.

For a fuller account of Steadman's book and teaching
see Articles in Bell News Sep 15 1915 etc etc.

with all its possibilities and all its limitations was born. "Change places with me" - that is the root idea of change-ringing. The idea is essentially one of movement, the movement of the bells among each other, and it is this idea of movement that all along has, and still does, dominate both the science and the art.

But it may be objected that this account of the beginning of ringing, although very plausible and very possibly true, is after all only conjecture. That is true; but we are almost at once on the pure ground of historical fact. The first completed step in the development of change-ringing was as Steadman tells us the "invention of the Pieces." And Steadman not only tells us what the Pieces are, and how they can be rung, but how actually they were rung. This enables us to argue one step backwards and turns our conjecture into a certainty.

Further Steadman tells us how the idea of movement, which first produced the Pieces, continued to develop change ringing, and the reader who wishes to understand what ringing is and how it

inevitably come to be what it is today cannot do better than study carefully the first part of the *Tintinnalogia*, that part which deals with Plain Changes. Stedman's testimony is invaluable because he wrote at a time when the idea of movement had shown what it was capable of in the way of development and before more complete development had obscured that idea in the minds of composers. Moreover Stedman was better fitted intellectually, to write on ringing as a whole than almost any man who has since written about ringing.

The root idea of the *Tintinnalogia* is that movement of the bells is the principle on which ringing is based - not the particular rows which are rung. Unless this is fully grasped the book is unintelligible.

And now just for a moment consider the terms and phrases that always have been, and still are, used in practical ringing. Hunting, Dodging, Place-making, Leading, Lying, Snapping, Coursing, Bob, Whole Turn, Half Turn, Course, Lead, and the rest. Practically every one implies movement. These terms were

invented naturally and spontaneously by ringers because they describe, and in some part explain, the things they refer to. A ringer naturally talks about hunting, because the idea in his mind is movement, one bell following another. He naturally talks about dodging, because the idea in his mind is that of a backward step in a forward path. He naturally talks of a Place, for the idea in his mind is that of a definite stage in his journey. And so with the others.

And this testimony of terms has not only positive value, but also negative value. All the terms imply movement. They do not imply anything else. If the root idea of Ringing were music we should expect terms with a musical significance; but such are conspicuous only by their absence. It is quite remarkable that the word "peal" which in ordinary language has a musical meaning, should in ringing have a technical meaning with which music has nothing to do.

Still more noteworthy is the fact that

See Article on "Rows and Changes"
Bell News Mar 27 1915.

These terms which are so much occupied with the Changes, have so little to do with the Rows. The ordinary modern Composer is almost exclusively concerned with the Rows. He treats the Changes almost as if they were the result of the Rows. Historical Change Ringing reversed the process. The Changes (i.e. the movement) are the all important thing; the Rows are the result, the artificial Rows being a comparatively unimportant result.

And this idea of movement is still the dominant idea of practical ringing. When we go into the tower to ring a peal we do not go with the idea of ringing any particular Rows. We go with the idea of ringing a particular method, i.e. so much particular work or movement. What Rows we ring we probably never know. We do know that we do so much hunting, dodging, and place making. Just listen to a band discussing any bit of ringing. Their talk is almost entirely of movement. "You stopped up too long behind, you ought to have come down before the

tenor " "When I got into 5-6 there was no one there to dodge with me" "The third left the slow too soon" Anybody can multiply such instances from his own experience. When you are sitting down by yourself with pencil and paper, no doubt a method naturally appears to you as a collection of figures, a series of Rows. But when you are in the tower it is quite different. There ringing consists of a certain number of bells making more or less intricate movements among themselves, like dancers in a set dance, or soldiers in drill movements. Different formations are constantly being produced, but the one essential thing is the movement which produces the different formations. So much is this true of ringing that the ringer looks on himself and talks of himself as one personally engaged in a journey. He says "I was in 5-6" "I was at the Lead", "I was behind"; not "I struck my bell in sixth or the front or behind".

Now you cannot divorce theoretical ringing from practical ringing. They

Rev. H Law James Bell News Jan 14. 1914.

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are two sides of the same thing. No doubt there are many problems of theoretic ringing which must be settled in the study and not in the tower such problems as the Composing of nine peals. No doubt it is easier and apparently more satisfactory to take a method as a concrete set of figures and "follow where the figures lead you" You will find many interesting problems but you will not necessarily find out the truth about ringing. For a method is a thing which belongs to the tower and to practical ringing. If we are to understand problems of Method Construction and Extension we must first find out what the method is in the tower, and rigorously exclude all other considerations and theories. Two and a half centuries ago Steadman showed how it can be done, and his book can well serve as a model.

We reach then the conclusion that our axiom must be that Change-Ringing is movement among the

Bells which produces different Rows.
 Our present task is to investigate
 the nature of this movement and
 the different laws and rules which
 govern it.

Note.

I do not wish to convey the idea
 that all early ringers were illiterate.
 By the middle of the XVII century
 it obviously was not so. Stedman
 was a man who could write good
 English, and the fact that he
 published two books on ringing
 shows that there must have been
 quite a number of readers. The
 Norwich men, Melchior and Crane,
 could write lively controversial
 letters. Annable's M.S.S shows him
 to have been a practiced penman.

Still my point remains, that ringing began and its destiny was fixed among the unlettered, in obscure country villages equally as in the towns. And it must be remembered that the first book the *Tintinnalogia* does not profess to give anything new, but describes and explains and reduces to systematic order ringing as it was already practised.

Chapter II

The Postulate

The one postulate in the science of Change-
ringing is the Bell

A Bell is an abstract entity which
has no qualities other than Identity and
Relative Position

When, speaking of a method, either in reference to practical or theoretical ringing, you talk of a bell, you do not mean a musical instrument weighing so many hundredweights and giving forth a particular note. You mean something quite different, which is abstract, and which is expressed to your mind in several different ways. When you are dealing with pencil and paper it is expressed by one of several figures, or letters, or sometimes by a continuous line. You call these figures and letters the bells but you know quite well that they are only symbols which stand

for a something behind them. When you are in the tower the bell is expressed to your ~~left~~ mind, through your hearing, by the sound of the bell above. Much more frequently and really, (since ringing is a thing of sight rather than of hearing), it is expressed through your eyes by the rope and the ringer who is pulling it. The ringer identifies himself with the bell he is ringing. It is he that is the expression of the abstract bell. It is he that hunts and dodges and makes places, not the material bell in the chamber above him, which is merely an instrument which records what he is doing.

Now although the expressions of the bell thus differ in varying circumstances, it is always essentially the same thing and always abstract. It bears to the science of Change Ringing the same relation that Euclid's "point" does to the science of geometry. In fact it is almost the exact equivalent of the other. As you must think of the point to understand geometry so you must think of the bell to understand.

The science of Change Ringing.

At different times and under different circumstances, the bell acquires different qualities. When you are dealing with music in connection with ringing, the abstract bell acquires musical qualities; and the symbols 12345678 may stand for a definite musical sequence. Or when you are dealing with the construction of Methods or Peals a bell may become a Hunt or an Observation Bell. But these qualities are acquired and not inherent. The only inherent qualities are identity and relative position.

A bell always keeps its own identity; from first to last of a course or a peal it is the same thing, not like two occurrences of the same note in a piece of music which have nothing, necessarily, to do with each other.

From this quality of identity and from the idea of movement we get the first of the great laws of Change Ringing viz that a bell may move up or down only one step at a time. It is inconceivable that any thing that has identity, whether it be abstract or

material, can have occupied one position at one time and another at another time, without having passed through connected intervening positions. The earliest ringers having conceived (of course unconsciously) the idea of the movement of an individual bell, the idea of that bell moving in a connected path followed as a logical necessity, and remains to this day the foundation of all ringing. And a connected path naturally implies to most minds the rule that a bell in, say, thirds may move into seconds or into fourths, but may not, indeed cannot, move into fifths or sixths in one step. Hence this rule has always been observed by the Exercise with but few attempts (to be noticed later) in the early days to break it, and none for practically two hundred years.

To a man who is writing in his study it may seem fine to say that "it would be possible to ring changes in almost any fashion but that scientific ringers have agreed to bind themselves by certain rules which

Rev. C.D.P. Davies Bell. News.

1915.

Stedman "Tintinnalogia" p. 3.

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regarded by them as being fundamental
and which are never transgressed except
for grave and sufficient reason," but
the idea implied has no foundation
in historical facts. In totally different
circumstances perhaps it might have
been possible "to ring changes in almost
any fashion" but directly change ringing
began by two bells "removing into each
others places" all the fundamental
rules like the one we are considering
had to follow by logical necessity.
As for any agreement between ringers
to bind themselves there never was any
opportunity for such a thing even if
there had been any disposition to
do so, which may well be doubted.

I have mentioned two early attempts
to break the rule that a bell may not
move up or down more than one step
at a time. One is referred to in the
Glossary as Jumping Doubles. Now
to jump implies movement and it also
implies a connected path. But it also
implies a path which passes over, and
not touching, a particular point or
position. From the word we can gather

What was in the mind of the men who invented this particular form of ringing. They never thought of questioning the idea of movement as the one essential thing in Change Ringing. They took it as their axiom. But they tried to see how that idea could be developed in a new direction. The attempt is a most interesting one. It failed because to ordinary minds, as I have said, a continuous path involves a bell passing from one position to the next and not over it.

The other case is that of Grandine True. This was an attempt by R.R. "the author of Grandine Bob" to obtain a 120 of Grandine Doubles without Singles. This was done "by moving the bell which lies in thirds place down under two bells at once into the trebles place, or else by moving the bell in trebles place up into thirds place." A similar attempt was made to produce a 720 of Bob Minor without Singles - "The Seven-hundred and twenty Changes of Grandine Bob may be Rang without making any single change therein,

Stedman Tintinnalogia p. 80

Tintinnalogia p 103.

Which way of Ringing it, is called Grandsons
Bob true At the first bob-change
of any double bob, it may be made, by
moving the Bell in fourths place down
under five Bells at once into the
seconds place"

Here again the root idea of the bells
moving in a continuous path is carefully
kept. If we had merely the figures,
the rows, we should naturally assume
that the rule that a bell may move
only one step at a time was an arbitrary
rule agreed to by ringers. Fortunately
we can see what was in the minds of
the ancients, and can understand
how it came about as a necessary
logical result of the first simple idea
of movement.

The second inherent quality of
the Bell is position.

Movement implies varying position
and the different positions are the
measure of what movement has taken
place. But the Bell is an abstract
conception, not conditioned by material
ideas of time and space. The position
of a bell is therefore relative, and

is relative to the position of the other bells and to nothing else. It is not, for instance, relative to the piece of paper on which you write out rows, though that is the relation which most readily suggests itself. Even in material things position is relative; we judge the position of towns by its relation to other towns or to some natural geographical feature. But while every material thing has a positional relation to every other material thing, a bell which is abstract is outside that relationship.

The question of relativity is a very important one in the Science of Change-ringing. Many of the fallacies that are widely held by people about such things as variation, extension, and the like are due to the fact that it is not sufficiently understood.

A Row is a succession of Bells.

It follows from what I have already said that the only inherent qualities in a Row are identity and its

See also. Bell News. Dec 11 1915

position relative to other Rows.

A Row consists of a definite number of bells in a definite order. The figures 12345678 may stand for any row. But once you apply them to a particular row, then 21436587 or 13572468 or any other permutation is only applicable to a row which bears a definite relationship to the first row. This relationship is the result of the movement of the bells and is the measure of the movement.

A Change is the movement between two rows and the means by which row is produced from row

1 2 3 4 5 6 7 8

2 1 4 3 6 5 8 7

These figures represent two rows but only one change.

This distinction between rows and changes is important and historical.
The ringing we are dealing with is

Change ringing not row ringing. The important thing is not what you ring, not the rows - they are results; but the method by which you ring, the movement, the hunting dodging and place-making.

It is in the changes that we must look for the essentials of ringing. It is there that we shall find the laws of the science and the solution of such problems as Method Construction Extension, Post Major Lead Ends, and the like.

To Spedman and the ancients, the value of the row was only in its marking the change. You could ring a row as many times as you pleased; but you were not allowed, any more than at present, to repeat a change. The first Method and peal Composition consisted of different arrangements of bells. As Composition became freer and more complex it naturally developed into different arrangements of rows. The term change at first included the resulting row. Then it was used indiscriminately for

either. Later still, in Composition it was almost exclusively used to mean the row only. Until in quite recent times the term "row" was invented, and the term Change practically relegated to the power. This shows how the relative values of the Change and the row have allied in the minds of Composers. This of course is quite natural; for problems of real Composition are best settled by investigating the laws by which rows are joined together. The movement, which is the changes, is implied in the method which is taken for granted.

When however we are considering the Science of Change Ringing as a whole and the Laws of Method Construction Extension, and such like, we must go back and give again to the changes the importance they have never lost in practical ringing.

Chapter III

The Nature of Movement.

At the base of Change Ringing we have a given number of Bells arranged in a Row. We have to produce other rows by interchanging the bells among each other. The Bells move like dancers in a set dance, or soldiers in a complex drill movement, constantly producing fresh formations. The number of formations, that is the number of rows, is, as every body knows, fixed. With five bells you have one hundred and twenty rows, no more and no less. With six bells you have seven hundred and twenty rows, and so on. But while every body recognises this fact, they, to a greater or less degree, assume that the movement which produces these rows is subject to no general law. Of course they know that you cannot produce say the row 13572468 direct from 12345678.

They know by experience that you cannot produce the extent of Doubles without at least five Singles. They know pretty well the Law of the In and out of Course of the Changes, (though for very many years this was treated as a fact that could be recognized but at the same time a mystery that could hardly be explained.) But, generally speaking, ringers have assumed that apart from certain obvious limitations you could put rows together pretty much as you pleased. Methods were the results of mens jancies and conditioned only by certain "Conventions" which ringers tacitly agreed to conform to. That a crude touch of Honey should be an expression of Law would seem absurd; and even for Methods which clearly show design in their construction our Reading Composers hold that each has its own Laws which do not necessarily apply to another.

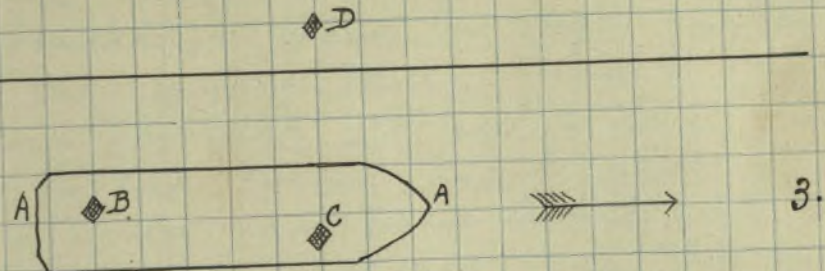
My present purpose is to show that once the idea is accepted that ringing is movement of the bells by which row is produced from row,

Then a general natural law becomes operative which controls all Method Construction, and which settles such questions as Extension and the like. To understand this law we must consider the nature of the movement

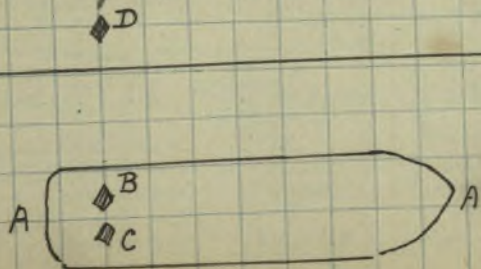
A. The Relativity of Movement.

All movement is relative. This is true of material things. When in ordinary affairs you think of speed or movement you always have in your mind some relation by which you judge that movement and you exclude all other relationships. If you walk quickly across the deck of a steamer you do not take into consideration the speed that the steamer is moving at. If you talk of an express train you do not think of the rate at which the earth is travelling round the sun. Yet of course the man is moving with the steamer, and the train is moving with the earth. Movement really means nothing more than that

The relative positions of two or more things are altered



Suppose that AA represents the deck of a steamer moving toward \rightarrow at the rate of four miles per hour. At B a man, we will call John is sitting in a chair. At C another man James is standing. And at D a third man ^{Charles} is sitting on a log on the quay alongside which the steamer is moving. When the steamer gets into this position James walks along the deck towards John at the rate of four miles an hour, and directly he reaches him the steamer and the three men are in the following positions



Which of the three men has moved?
 James would say "of course I moved. I wanted to speak to John and, as he was sitting still, I had to walk down the deck to get to him." But if he had looked to the right of him he would have found himself all the time opposite Charles; and Charles too was sitting still. John was quite comfortable in his chair, but as he was watching the people on the quay, he was quite sure in his mind that he was moving. Charles was sitting still on terra ferma, but he happened to be thinking of astronomy and he was calculating the exact rate he supposed the punt with earth "and all which it inherit" was travelling toward Sirius or some other "fixed" star, which he knew was anything but fixed.

Each of these men was thinking of movement and each had for the ~~the~~ moment a different standard to judge movement by. James was thinking of himself and John: all other relationships he ignored. John

was thinking of the steamer and the quay; he too ignored other relationships. Charles was thinking of the movement of solar bodies; and he too ignored other relationships. Relatively to Charles, James has not moved. Relatively to the steamer, John has not moved. Relatively to the quay, Charles has not moved.

Now try and imagine that John is relative in position to James, and James to John, and that all other relationships are utterly done away with. What should we find? Why that both John and James had moved, and moved in exactly equal proportion.

Bells are abstract entities, and by our postulate their positions are relative to each other, and to nothing else. They are not material, and therefore their movement is not relative to any material thing. Movement of a bell does not mean altering the position of a figure on a piece of paper. It means that the position of one bell relative to the position of

another bell is altered.

1	2	3	4
2	1	4	3
2	4	1	3
4	2	3	1
4	3	2	1

In the first change the 2nd moves from 2nds to the lead and its relative position to the other bells is altered.

In the second change it leads again; but since the rible at the same time moves into 3rds and the 4th into 2nds, the relative position of the 2nd also is altered. Therefore the whole pull on the front is as much movement as any other part of hunting.

This is true of all Place Making. Place-making is not an exception to movement but an integral part of it. Places are not something different from hunting, but the form hunting takes in particular circumstances.

And what is true of Places is also true of cases where one bell appears to lie idle in one position for a number of blows. There are always the result of movement and not of lack of movement. For instance the four blows behind in Plain Bob

Triples

4	2	3	4	5	6	7
2	4	3	6	5	7	
2	4	1	6	3	7	5
4	2	6	1	7	3	5
4	6	2	7	1	5	3
6	4	7	2	5	1	3
6	7	4	5	2	3	1
7	6	5	4	3	2	1
7	5	6	3	4	1	2
5	7	3	6	1	4	2
5	3	7	6	2	4	
3	5	1	7	2	6	4
3	5	2	7	4	6	
3	2	5	4	7	6	
4	3	5	2	7	4	6
3	1	2	5	4	7	6
3	2	1	4	5	6	7

All the bells are moving forward and this forward movement includes whole pulls before and behind. When the sixth leads the other bells have to make one step backwards. The forward path of the sixth has caused it to lie a whole pull behind. If the next step were forward it would bring the bell into 6th. But a backward step is required which causes another whole pull behind. Then the

forward movement is resumed and that causes a third whole pull. Hence the four blows in 4th.

Similarly we shall find that in many cases the result of movement is that one or more bells will remain for quite a long time in one position.

* 4.
 3 1 5 2 7 4 6 } 1st whole pull
 1 3 2 5 4 7 6 } 2nd whole pull
 1 3 5 2 7 4 6 } 3rd whole pull
 3 1 2 5 4 7 6

So long as the positional relationship of a bell is altered towards any other bell you have movement, and the laws which control movement are fully operative.

I am not concerned for the moment with the question as to whether any method in which a bell lies for more than five consecutive blows in any one position is suitable for practical ringing. That will be dealt with at the proper time. All we can say at present is, that the fundamental laws of Method Construction make no distinction. The same Construction which gives Plain Bob on an odd number of Extreme Bells without four consecutive blows, gives Plain Bob on an even number of Extreme Bells with four consecutive blows.

Knowledge of the relativity of movement will enable us to correct some false or exaggerated ideas of the position and value of Races in Method Construction which are widely held. In many men's opinion Races are the one essential thing in Construction. They

are the causes of which all hunting, dodging and other work are the results. Put your Places right and all else will follow as a matter of course. Now it is quite true that a most convenient way of analysing a method is by the Places. It is generally true also that if the Places are correct, the other work will be correct too. But it is not true that Places are the cause of hunting and dodging. Places are a part of movement equally with other work. Any theory which assumes that they are superior to or essentially different from other work is founded on a fallacy.

Sir Arthur Heywood on more than one occasion laid it down as an axiom of Method Construction that "every bell that can, must change its place at each blow."

In so far as this is a recognition of movement as the essential thing in ringing, we shall of course agree with it. In so far as it is a standard to which good methods should attain, it does not at this

point concern us. But as an axiom
 of the science of ringing it is based
 on two fallacies. The first is that
 Places are not movement, but the
 negation of movement. The second
 is that Places, or at any rate more
 than the minimum number of Places,
 are in themselves undesirable things.
 It is pointed out that with an even
 number of bells you must have two
 Places in every alternate change.
 With an odd number of bells you
 must have one Place in every change.
 "Less Place-making than this is
 not possible; more is not necessary."
 And consequently while Superlative
 is the ideal in construction Cambridge
 is "Crude" and "radically bad" and
 even Kent Treble Bob and London are
 not legitimate.

About this opinion it is only
 necessary to say that it is not
 supported by anything in the
 historical use and development of
 change ringing, and is contradicted
 by modern experience
 So long as you keep to the minimum

* Sir Arthur Heywood.

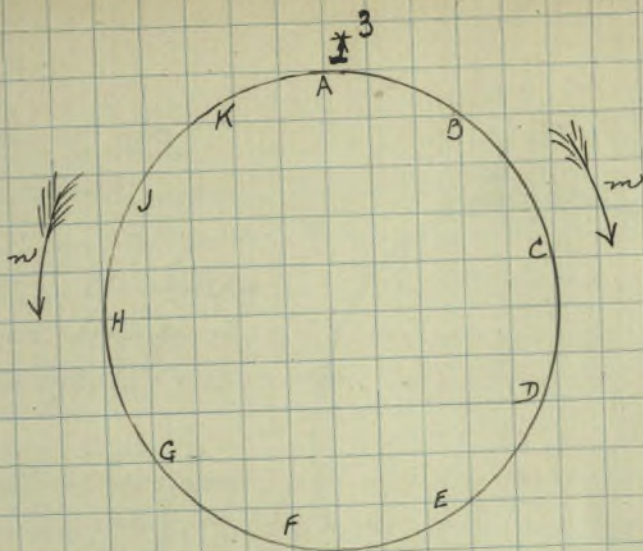
number of Places, you preserve a regular succession of Odd and Even Rows. No one who knows anything about real Composition will deny the importance of having odd and even rows in due proportion and in due order. But a few men go much further, notably the Rev C. P. Davies and make this regular succession into a fundamental rule; so that the reverend gentlemen could "assert that Kent, London, Cambridge and Bristol are illegitimate and are so obviously illegitimate that there is no possibility of questioning the fact."

I however do "question the fact" and not I only but the whole Exercise. This "fundamental rule" is fundamental only in the mind of one or two men. Our present business is not to invent rules to which we think Methods ought to conform, but to find out the laws to which they do actually conform.

37.

B - The Cyclical Nature of Movement.

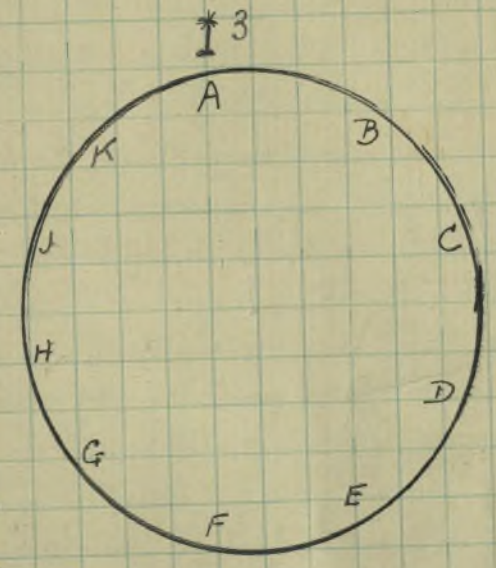
All Movement in Change Ringing
is cyclical in form. It is movement
which takes a bell from a point, and
at the same time, tends to return
it back again to the same point. It
is movement which takes the bells
from a row, and at the same time
is bringing them back again to the
same row. Every collection of rows
produced by Change Ringing is not
necessarily a Round Block; but every
collection, whether produced by the
most complex of methods, or by the
crudest bit of Stoney, is necessarily
in Round Block form, and is either
a Round Block or part of a Round
Block. There is no exception.
Upon this point hangs all the science
of Change Ringing.



Let ADG be a circle, and 3 an object stationed on the circle at A . Suppose you want to move 3 along ADG . You can do so in one of two directions. Either you can move it from left to right in the direction of the arrow m . Or you can move it from right to left in the direction of the arrow n . You have no third choice.

If you move 3 from left to right you will move it through $BCDEF$ G and if the movement is continued you will ultimately reach A again. Similarly, if you move it from right to left, you will move it KJH

and, if the movement is continued, you will ultimately reach A again through GFED CB.



But when you are moving 3 from left to right you can, after you have reached any point, reverse the direction of the movement, and move 3 from right to left. Suppose you have reached C; you now reverse the direction. What happens? If you continue the reversed movement 3 passes again through B and again reaches A. It has now travelled forward and backward along an arc of the circle.

Again, suppose you move 3 from left to right until you reach any point D. Now reverse the movement which will be toward A through C and B. Before you reach A, at the point

B again reverse the movement. After the second reversal the movement is toward A through EHK and if it is continued will ultimately reach A. Similarly however many times you reverse of the movement it is always toward A either through the complete circle or else backwards & forward and then backward along an arc of the circle. Further every reversal involves 2 travelling from some point of the circle along an arc of the circle and back along the same arc to the same point. No movement is possible which is not included in the above.

This exactly illustrates the movement of a bell in ringing. It is definitely restricted to the circle and the arc and because it is so restricted we can definitely calculate it.

In setting down the movement of a bell on paper we could use circles to illustrate it; but we have more than one bell to deal with, and it is convenient to stick to the ordinary straight line diagrams

Bear in mind however that a circle which shows the Places in exactly the same form as the rest of the hunting is so far, a better illustration of the real nature of the movement than a diagram with straight lines and Places shown by vertical lines.

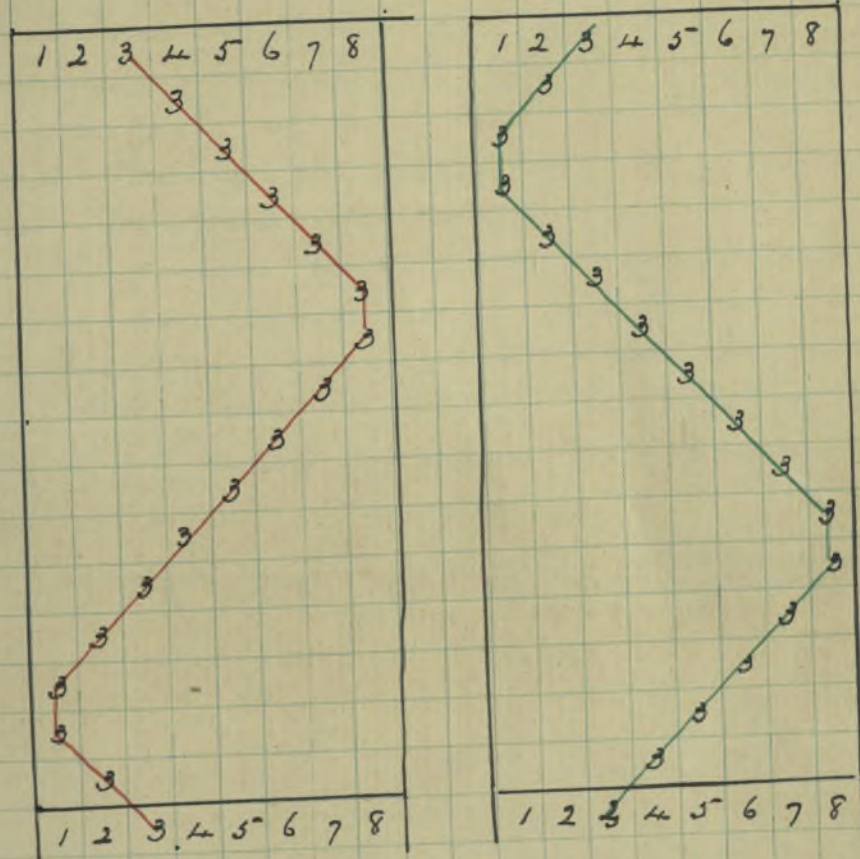
Let 12345678 be any Row consisting of any one number of Bells, and 3 be any one Bell in that Row.

3 can change positions with either the Bell in front of it - 2 - or the Bell behind it - 4 - ; but with no other Bell.

If 3 changes position with 4 it moves into fourths place and a cyclical movement is begun which tends to return 3 back to the position from which it started; and will do so unless the movement is interrupted.

Similarly if 3 changes position with 2 it moves into seconds place and a cyclical movement is begun which tends to return 3 back to the position from which it started; and will do so unless the movement is interrupted.

Fans: -



These two movements are exactly similar to each other except in direction - one is the opposite of the other.

The first we will call Forward or + Movement

The second we will call Backward or - Movement.

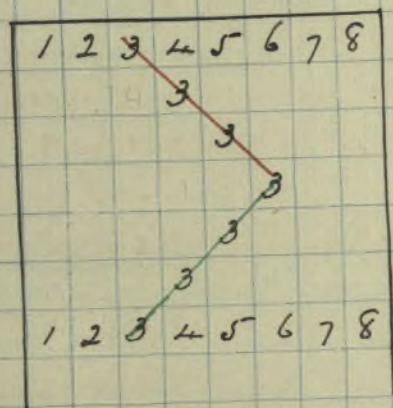
Interruption of this cycle can take

place in one of two ways only.

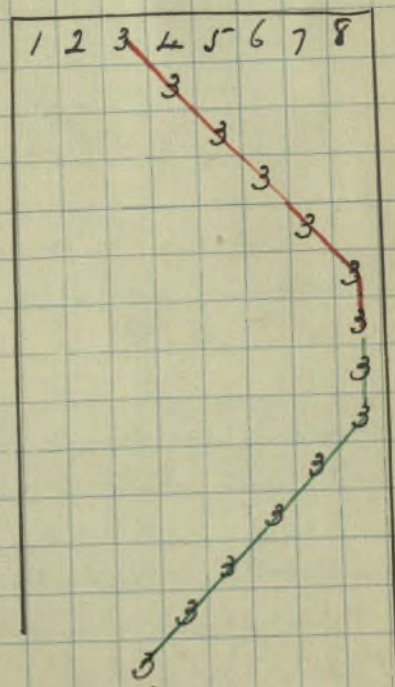
First at any point in the first cycle Backward Movement can be substituted for Forward Movement.

Similarly, at any point in the second cycle Forward Movement can be substituted for Backward Movement.

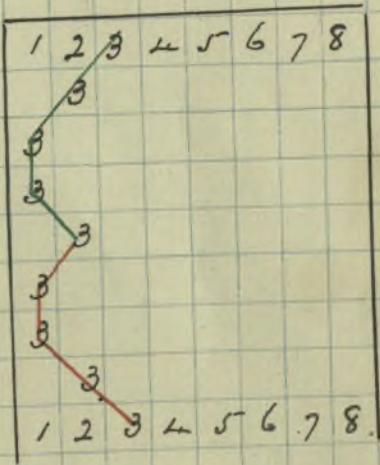
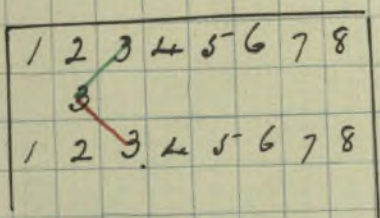
A. If at any point in a Forward Cycle Backward Movement is substituted, a movement is begun which tends to take the bell back again to the position from which it started and will do so unless it is interrupted.



— = Forward Movement
— = Backward "



Similarly, if at any point of a Backward Cycle, Forward movement is substituted, a movement is begun, which tends to take the bell back again, to the position from which it started; and will do so unless it is interrupted



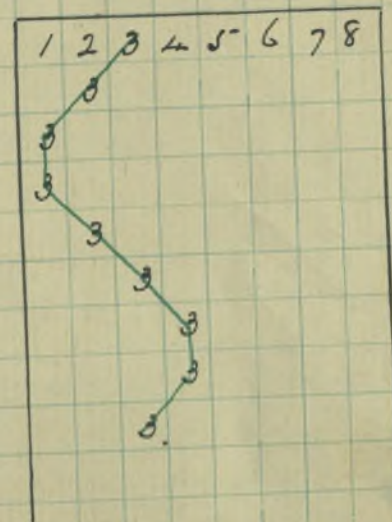
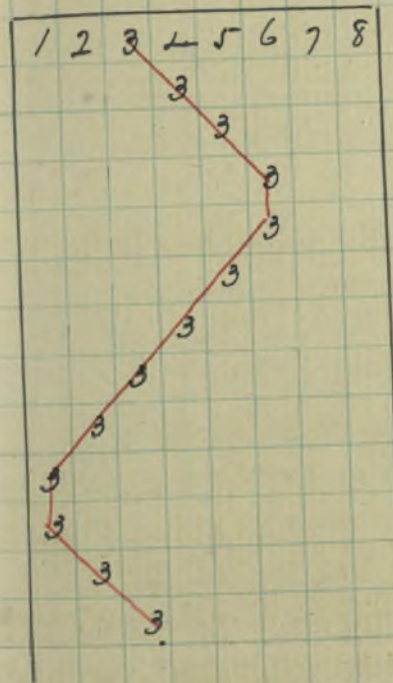
— = Forward Movement
— = Backward "

B. Secondly. A bell which starts a cyclical path among a given number of other bells may make a Race in any one position.

When this is done the cycle is turned into one on a number of bells less than that of the original path.

If the starting movement is Forward this smaller cycle remains throughout Forward. And if the starting movement

is Backward this smaller cycle remains
throughout Backward.



When as explained in par. A. page 43 the
 movement of a bell consists of x steps of
 Forward movement followed by x steps
 of Backward movement, the bell moves
 forward and backward along the arc
 of a cycle. This may be called a
Dodging movement. Similarly with
 x steps of Backward movement followed
 by x steps of Forward movement.

Interruption of a Dodging Movement can only take place by substituting Forward Movement at any one point for Backward Movement (or vice versa);

or, by the introduction of a cycle on less number of bells than those of the original row. (as explained par B. p. 44.)

In either case the movement tends to return the bell to the position from which it started.

It follows that no matter how you write out changes, the path of a single bell will consist of a number of complete cycles of (perhaps) different sizes and sometimes with the addition of a number of dodging movements of different sizes.

Also that all movements and all combinations of movements tend to return the bell to the position from which it started. And will do so unless either (a) the bell perpetually moves in a cycle which does not include the original position or (b) it, by means of dodging movements, oscillates between two points.

In Change Ringing, these two cases are ruled out by the law which forbids

any row being rung more than once.

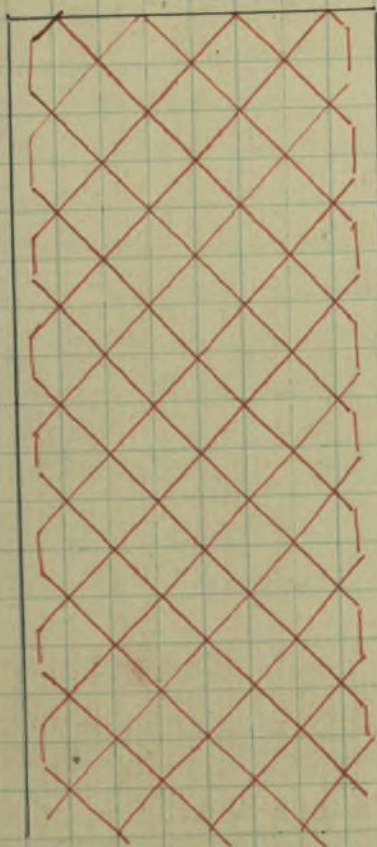
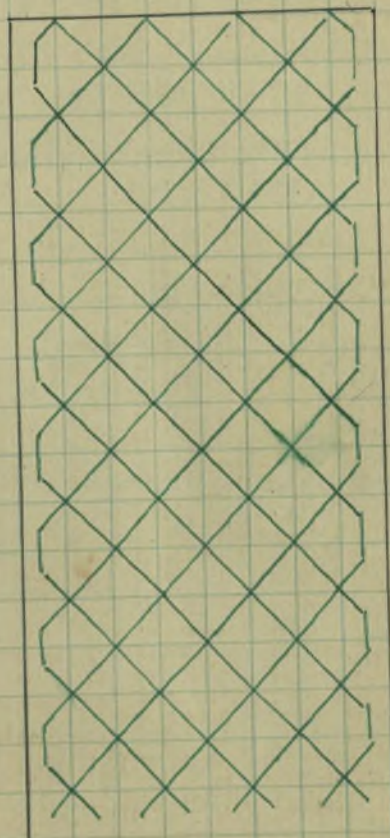
But the movement of one bell is not independent. It implies and involves the movement of other bells. In the

Example given the movement of
 2 3 3 into 2nd position necessitates
 3 2 the movement of 2 into 3's
 position. If 3 is at that
 moment moving Backward 2 will also
 be moving Backward; and if 3 is
 moving Forward 2 will also be moving
 forward.

Similarly each step in the Cycle consists of the bell changing positions with another bell, and if the cycle is forward the movement of the other bells will be forward too. Or if the cycle is backward the movement of the other bells will be backward too.

And if this movement of the other bells is continued each will complete a cycle. and so we get the following as the simplest form of movement in Change Ringing -

Note that the distinction is between Forward and Backward Movement, not between Upward and Downward Movement.

A Cycle of Forward
Hunting.A Cycle of Backward
Hunting.

The above is a Hunting Course and is produced when all the bells move continuously forward, or all move continuously backward. It is movement which starting from a given Row is always tending to bring the bells back.

again to that Row.

Let $1\ 2\ 3\ 4\ 5\ 6\ 7\ 8$ be any one Row
 and from it
 let $2\ 1\ 4\ 3\ 6\ 5\ 8\ 7$ be produced
 by Forward Hunting of all the bells.
 Every bell has started a movement
 which tends to return the bells
 back to the row $1\ 2\ 3\ 4\ 5\ 6\ 7\ 8$ and
 will do so unless it is interrupted.

Interruption of this movement can
 take place only as follows -

I In any Change Backward Movement
 on all the bells may be substituted
 for the Forward Movement

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8

This Backward Movement tends to
 return the bells to the Row $1\ 2\ 3\ 4\ 5\ 6\ 7\ 8$,
 and will do so unless it is

interrupted.

II In any Change Backward Hunting can be substituted for the Forward Hunting of part of the bells. This introduces a Secondary Movement on the bells involved which tends to return those bells to the Row from which the movement began; and will do so unless the movement is interrupted. When the Completion of the Primary Cycle coincides with the Completion of the Secondary Cycle (and not till then) the bells will return to the Row from which at first they started.

III The Movement begun as Forward Hunting on all the bells may in the second Change be turned into two or more Cycles each of Forward Hunting, the bells involved in one not taking part in the other. When the completion of one Cycle coincides with the Completion of the other and not till then the bells will return to the Row from which they first started.

1	2	3	4	5	6	7
2	1	4	3	6	5	7
2	4	1	3	6	7	5
4	2	3	1	7	6	5
4	3	2	1	7	5	6
3	4	1	2	5	7	6
3	1	4	2	5	6	7
1	3	2	4	6	5	7
1	2	3	4	6	7	5
2	1	4	3	7	6	5
2	4	1	3	7	5	6
4	2	3	1	5	7	6
4	3	2	1	5	6	7
3	4	1	2	6	5	7
3	1	4	2	6	7	5
1	3	2	4	7	6	5
1	2	3	4	7	5	6
2	1	4	3	5	7	6
2	4	1	3	5	6	7
4	2	3	1	6	5	7
4	3	2	1	6	7	5
3	4	1	2	7	6	5
3	1	4	2	7	5	6
1	3	2	4	5	7	6
1	2	3	4	5	6	7

1	2	3	4	5	6	7	8	9	0	E
2	1	4	3	6	5	8	7	0	9	E
2	1	4	6	3	8	5	7	0	E	9
1	2	6	4	8	3	7	5	E	0	9
1	2	6	8	4	7	3	5	E	9	0
2	1	8	6	7	4	5	3	9	E	0
2	1	8	7	6	5	4	3	9	0	E
1	2	7	8	5	6	3	4	0	9	E
1	2	7	5	8	3	6	4	0	E	9
2	1	5	7	3	8	4	6	E	0	9
2	1	5	3	7	4	8	6	E	9	0
1	2	3	5	4	7	6	8	9	E	0
1	2	3	4	5	6	7	8	9	0	E
2	1	4	3	6	5	8	7	0	9	E
2	1	4	6	3	8	5	7	0	E	9
1	2	6	4	8	3	7	5	E	0	9
1	2	6	8	4	7	3	5	E	9	0
2	1	8	6	7	4	5	3	9	E	9
2	1	8	7	6	5	4	3	9	0	E

Etc.

When movement is introduced among bells, that movement always tends to return the bells to the Row from which they started; and it can only be interrupted by movement which also tends to return the bells to the starting row. In its turn this movement can only be interrupted by movement which equally tends to return the bells to the starting Row. And so on.

Thus the whole of Change Ringing consists of the bells doing a number of movements in the form either of completed cycles or forward and backward along the arcs of cycles. In some of these cycles all the bells are involved in some only a part of the bells. Every cycle involves at least five bells.

Our task is now to investigate the way these cycles can be put together so as to form the finished Methods and Goals.

But first it will be well to say something about Symmetry and Form.

Note:-

In the foregoing I have spoken of a Bell starting from and returning to the same position and of the Bells starting from and returning to the same Row; and I deliberately chose those expressions as best conveying my meaning. But it must be understood that any idea of the bells starting or finishing is subjective and not objective. A Round Block is movement in cyclical form and being independent of all considerations of time and space is, essentially, neither start nor finish but like a circle is perpetual. A starting point or a starting row is really the point or the row which we select in our own minds as that from which we trace the movement; and this may be any point or any row we please.

Chapter IV

Symmetry.

See also Article on Symmetry (J.A.T) in
Bell News Dec 18 1915. Also Article
on "The Law of Truth" ibid. Aug 28 1915 essay.

There are many rules in Change Ringing, some of them so stringent that not the slightest breach is tolerated. And there are many standards by which men judge methods and scales, whether they be good bad or indifferent.

When we consider the history of the art, we find that these rules and standards have been, and are, at all times and in all places practically the same. Development has of course taken place, and has had its effect on them, but the rules and standards of any one period are not different from those of the preceding generation, but the same modified by the continual progress that is going on.

Now when we find a large number of men, scattered over a wide area, and belonging to different periods of time, unanimously and unquestioningly agreeing to be bound by any rules, we must

* Read "submitting" submitting

Come to the conclusion that one of two things must have happened. Either that there was some central authority with power to decree laws, and sanctions sufficient to enforce them. Or else that the rules were so inevitably connected with the matter to which they relate, that they arose spontaneously and carried their own sanctions with them. Rules which are essentially arbitrary can be enforced if there is sufficient power to do so. Rules which are based on mere fancies or fashions will endure as long as the fashions last, and will pass away with them.

Sports like football and cricket have many rules, the majority of which are arbitrary. In each case there is a central recognised authority, which has the power to make these rules and the power to alter them; power which is continually being exercised. Moreover, and particularly in the case of the Football Association, they have power to see that they are enforced, cheats being punished with

* If anyone thinks that the Method Report was an attempt to enforce new rules may I say (and no one knows better about the matter than I) that it was an attempt more or less successful to reduce to order rules which were already in operation.

heavy penalties.
 In Change Ringing there is no such central authority. The Central Council has disclaimed any idea of being a legislative body. It had never attempted to introduce new rules into practical ringing; all it has done is to some extent to define and codify rules already in operation. And in any case it is a modern body while the rules and standards have been observed for a couple of centuries.

It follows that the rules and standards which ringers observe must arise from the essential nature of ringing itself; and this is particularly true of those which can be grouped together under the general name of Symmetry.

From the very beginning ringers felt that the movement which is ringing, must not be promiscuous, but must have proper form; and from this idea, developed, we get the division of changes into Leads, Courses, and Peals.

We have seen that any block of

rows must inevitably be produced by combinations of different cycles or Round Blocks, and we could develop the idea and show the laws which govern these combinations, irrespective of whether these blocks are arranged or not in any symmetrical order. It will however very much simplify our task if we confine ourselves at first to the traditional forms of ringing and afterwards show that the same laws are operative in all possible blocks of rows.

Symmetry is a quality inherent in nature and may be defined as the relationship of two things to each other when one is balanced by, and complementary to the other.

Now the root thing in Change Ringing is the Change, which is made by "two Bells removing into each others places" * 1 2.

2 1 and in the Change you have as good an example of symmetry as you will find anywhere. The movement of 1 into 2's place is exactly balanced by

* Tintinnalogia page 3.

and complementary to the movement of 2 into 1st place. Not only so, but one movement is dependent on and cannot take place without the other movement. Again when we have the Hunting Course on more than two bells we have perfect symmetry.

Symmetry thus being inherent in the very fundamentals of ringing, it would be strange indeed if it were not operative in the more highly developed forms.

Now all blocks of changes must be produced by cyclical movements. These cyclical movements are either Hunting Courses or of the nature of Hunting Courses and therefore each movement is itself symmetrical.

It is only when you get combinations of cyclical movement that a greater or less degree of symmetry is possible in their arrangement. A promiscuous touch of stoney will consist of a number of changes on two bells and each of these changes is perfectly symmetrical. It is in the arrangement

* The Lead of Course always depends on
the Cycle made by the "Whole Hunt"

Not quite historically correct

** Terminologia Page 72.

of the Changes alone that more or less
Symmetry can be shown.

The earliest form of ringing took
the shape of Hunts and Exquisite Bells
and the Ancients found it necessary
to arrange these Hunts in Symmetrical
form. The division was not at first
into Leads and Courses, but into the
Cycles which the Whole Hunt, Half
Hunt and Quarter Hunt performed.

A Seal was one Round Block; there
was as yet no Method with Plain
Leads and Robs. The Conductor was
in supreme Command, no bell moved
from any position but at his direction.

When Cross Seals were introduced
each ringer had a work which he
had to do and the Conductor's task
was restricted to telling him what
variations he had to make in his
work. At first the ringer's work was
merely to hunt his bell, the Conductor
telling him when to dodge, all
variation from plain hunting being
called Robs. ** Then as more complex
work was introduced the ringer was
expected to do some dodging and

* Method Report "Rules and Decisions" of the
Central Council page 17.

59.
place making without being warned, the
Conductor only giving notice of any
alteration. Thus we get the modern form
of plain Courses and Ribs.

If a man is expected to do a work without
being prompted, it is almost necessary
that that work should be as regular
as possible, and to this the inherent
symmetry in ringing naturally lent
itself. In addition to this the old
Composers had the task before them
of producing all the possible number
of rows on the bells (usually five
or six) and they found that this
can best be done by symmetrical
arrangements of the changes.

It followed that it was accepted
as a rule that the Plain Course of
any Method must consist of as
many Leads as there are Working
Bells each Lead to be exactly alike.*

Or in the case of Methods like
Stedman, where "every bell hath a
Course alike" of as many Divisions
as there are bells each Division
Exactly alike.

This rule is in operation to the

present day and probably will always be in force. There does not however seem any real reason why future development should not introduce methods with dissimilar Leads. Nor would such development, be necessarily be contrary to the spirit of the above rule. For, it must be remembered that the rule was not introduced to restrict ringing, but it grew up because men recognised that by its help they could best get ringing. And this is really the only test by which you can judge any rule, whether it is already in operation, or whether you think it should be made. Does it help you to get the best out of ringing or does it restrict you? And there is no rule in ringing that may not freely be broken if the result justifies it. But you will find that, since the accepted rules are spontaneous and not arbitrary, the instances where you may break them and do good are very, very,

few indeed.

Symmetry is an inherent quality in Change Ringing and must be taken into account. It is not as has been said merely "looking pretty on paper" you cannot have any Block of Rows without symmetry, but it is obvious that there are degrees of symmetry and the Exercise has adopted an increasingly high standard in the matter. Of late years the word has been taken to apply solely to the arrangement of the work in any one Lead or Division of a Method. A Method is said to be symmetrical or not according to whether its Lead or Division is balanced about a certain axis. Now whether we hold or not that this particular form of symmetry is essential to a Method for ringing purposes, we must admit that this is a standard and not, like symmetry in general, a fundamental quality. We can argue, and I think argue correctly, that it is a stage of development which Ringing has reached and to abandon it is to go backwards. We can show its value in getting true

* See Article (JAT) Bell News. Aug 18 1915

feels. ^{*} But we may not say that Methods cannot exist without it. We may not treat it as an essential quality of a Method, and proceed to draw (as has been done) general rules of Method Construction from it.

The standard of symmetry has shifted in the past, and may possibly shift in the future. But the general quality on which it is based is inherent and symmetry must always be a dominant factor in Change Ringing.

I propose to confine my arguments and illustrations mainly to those Methods which agree with the traditional forms; but I wish to point out that no general fundamental laws may be laid down which are based on those forms alone.

The following are illustrations of different degrees of symmetry. All four blocks show symmetry to some extent; but B is more symmetrical than A, C than B, and D than C. At early times the standard of symmetry required was between A and B. In the course of time it has been raised

A.

1	2	3	4	5	6	7	8
1	3	2	4	5	6	8	7
1	2	3	5	4	6	8	7
2	1	5	3	6	4	7	8
2	5	1	6	3	7	4	8
3	2	6	1	7	3	8	4
5	6	2	7	1	8	3	4
6	5	7	2	8	1	4	3
6	7	5	8	7	4	1	3
7	6	6	8	2	4	1	3
7	5	6	2	8	1	4	3
5	7	2	6	1	8	3	4
5	2	7	1	6	3	8	4
2	5	1	7	3	6	4	8
2	1	5	3	7	4	6	8
1	2	3	5	4	7	6	8
1	2	3	4	5	6	7	8

B. YORKSHIRE COURT MAJ.

1	2	3	4	5	6	7	8
2	1	4	8	6	5	8	7
2	4	1	8	5	6	7	8
4	2	3	1	6	5	8	7
2	4	3	6	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	8	3	7	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	5	3	1
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	6	3	4	2	1
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	5	7	3	8	2	6	4

C. LOUCHBOROUGH B. MAJ.

1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
2	3	1	6	4	8	5	7
3	2	6	1	8	4	7	5
2	3	6	8	1	7	4	5
3	2	8	6	7	1	5	4
3	8	7	7	6	5	1	4
8	3	2	6	7	5	4	1
8	2	3	7	6	4	5	1
1	8	3	6	7	4	1	5
2	3	8	7	6	1	4	5
3	2	7	8	6	5	4	1
2	3	7	8	5	6	4	1
3	2	1	7	5	8	4	6
3	1	7	5	7	4	8	6
1	3	2	5	4	7	6	8
1	3	5	2	7	4	8	6

D. D. NORWICH C.B. MAJ.

1	2	3	4	5	6	7	8
2	1	4	8	6	5	8	7
2	4	1	8	5	6	7	8
4	2	3	1	6	5	8	7
2	4	3	6	1	5	7	8
4	2	6	3	5	1	8	7
2	4	3	6	5	8	1	7
4	2	6	3	8	5	7	1
4	6	2	8	3	7	5	1
6	4	8	2	7	3	1	5
4	6	2	8	7	1	3	5
6	4	8	2	1	7	5	3
4	6	8	1	2	7	3	5
6	4	1	8	7	2	5	3
6	1	4	8	2	7	3	5
1	6	8	4	7	2	5	3
1	8	6	7	4	5	2	3

* J. W. Washbrooks METHOD CAVERSHAM. is not symmetrical according to this standard.

to between B and C and though there are able people* who do not accept that standard the general experience of the Exercise has decided that is the best place. But note that there is no essential necessity for fixing it there; the general experience of the Exercise could have raised it still higher and fixed it between C and D. However it has not done so.

Chapter V

The Principle & Coursing Order.

If from any given Row all the bells
move forward,
and if that movement is continued,
then a Forward Hunting Course is produced.

Similarly; if from any given Row
all the bells move backward,
and if that movement is continued,
then a Backward Hunting Course is
produced.

A. FORWARD HUNTING C. B. BACKWARD H.C.

1	2	3	4
2	1	4	3
2	4	1	3
4	2	3	1
4	3	2	1
3	4	1	2
3	1	4	2
1	3	2	4
1	2	3	4

1	2	3	4
1	3	2	4
3	1	4	2
3	4	1	2
4	3	2	1
4	2	3	1
2	4	1	3
2	1	4	3
1	2	3	4

These are exactly the same thing except that one is the opposite of the other in the direction of the movement and the order in which the Rows turn up. Since 1234 may represent any Row, either Blocks may be considered as Forward or as Backward; but if once A is considered as Forward then B must be considered as Backward; and vice versa.

With x bells the total number of Rows = P . P being the result of the well known mathematical product.

$$1 \times 2 \times 3 \times 4 \times 5 \dots$$

These P Rows will divide into $\frac{P}{2x}$ Hunting Courses, which are mutually exclusive.

Each of these $\frac{P}{2x}$ Hunting Courses can be produced either by Forward or by Backward Hunting.

The P Rows cannot be divided into any other group of Blocks which -

a. are mutually exclusive;

b. do not contain repetition of Rows.

By mutually exclusive I do not mean that you cannot divide the P rows into other groups of Blocks which

product (ESP)

are equal to each other and which together contain the total number of Rows,

but that you cannot have two Hunting Courses which contain the same Row unless every Row is the same. And conversely if one Hunting Course has a Row different from any Row in another Hunting Course then all the Rows must be dissimilar.

The Hunting Course thus being

- a. The result of the most simple form of movement; and
 - b. The only exclusive Block possible,
- naturally becomes the unit of Construction and Composition.

It is to some extent analogous to the atom in Chemistry.

In any Hunting Course the cyclical paths of the Pieces follow each other in a definite regular order.

This order is Causing Order and it is cyclical in form.

It is advisable always to write down Causing Order cyclically.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8

6	2	8	7	5	3	1	4
6	8	2	5	7	1	3	4
8	6	5	2	1	7	4	3
8	5	6	1	2	4	7	3
5	8	1	6	4	2	3	7
5	1	8	4	6	3	2	7
1	5	4	8	3	6	7	2
1	4	5	3	8	7	6	2
4	1	3	5	7	8	2	6
4	3	1	7	5	2	8	6
3	4	7	1	2	5	6	8
3	7	4	2	1	6	5	8
7	3	2	4	6	1	8	5
7	2	3	6	4	8	1	5
2	7	6	3	8	4	5	1
2	6	7	8	3	5	4	1
6	2	8	7	5	3	1	4

C.O. =

4	6
2	8
1	7
3	5

C.O. =

8	5
6	1
2	4
7	3

In practical singing the term *Causing Order* is used in a rather wider and looser sense. In the science

of ringing it belongs exclusively to the Hunting Course.

Each Hunting Course has its own Coursing Order and therefore the Co. may stand as the signature of the Hunting Course. If at any time changes the bells are in the same Co. that is a sign that those time changes belong to the same Hunting Course.

Coursing Order belonging exclusively to the Hunting Course it is obvious that there can be no Common Co. in any Change where part of the bells are hunting forward and part are hunting backward.

1 2 3 4 5 6 7 8	← No Common Co.
2 1 3 5 4 7 6 8	← Co. = 21578643
1 2 5 3 7 4 8 6	← No Common Co.
2 1 5 7 3 8 4 6	← do do.
2 5 1 7 8 3 6 4	← Co. 25734681.
5 2 7 1 3 8 4 6	

But there is a Co. among those bells which are hunting forward, and among those bells which are hunting

Backwards.

All that has been said about Hunting Courses which are made by all the bells applies with equal force to Hunting Courses which are made by a part of the bells only; and equally whether as in Ex A

A

1	2	3	4	5	6	7	8
2	1	4	3	5	7	6	8
3	2	3	4	7	5	8	6
4	1	4	3	7	8	5	6
5	2	1	3	8	7	6	5
6	2	3	1	8	6	7	5
7	2	4	1	3	6	8	5
8	2	3	1	6	5	8	7
5	2	4	3	6	1	5	7
6	4	2	6	3	5	7	8
7	4	2	6	3	5	7	8

whether as in Ex A the whole Hunting Course is made together, or whether part is made in one Lead and part in another.

It will be noted that in any Hunting Course either on all the bells or on part either made straight off or at different times the Rows come in a definite order either forward or backward. No other order is possible

C.O. of Hunting Course on 5678 =

5 7 8
6

In a Dodging Movement (page 45) the bells

Having done some part of a Hunting Course reliace their steps back to the row from which they started.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8

This will reproduce the same Rows which have already appeared.

As the bells are all moving forward at the same time, or backward at the same time, they

keep the same Coursing Order.

Similarly any Block formed by mixed Hunting Courses and Dodging Movements when all the bells are moving forward at the same time or backward at the same time will consist of the Rows of the Hunting Course with varying repetitions, and no other Rows. And the bells will be in the same Coursing Order throughout.

These Blocks are the Principles on which Methods are built.

Their claim to be the scientific foundations of all Methods depends

entirely on the fact that they alone have the same coursing order throughout.

Theoretically it is not necessary for a Principle to be symmetrical; but the standard of symmetry adopted by the Exercise has for practical purposes confined the Principles in use to two - the Plain Principle and the Treble Bob Principle; though the Double Dodging and Triple Dodging Principles are occasionally used.

PLAIN PRINCIPLE

TREBLE BOB PRINCIPLE

1	2	3	4	5	6
2	1	4	3	6	5
2	4	1	6	3	5
4	2	6	1	5	3
4	6	2	5	1	3
6	4	5	2	3	1
6	5	4	3	2	1
5	6	3	4	1	2
5	3	6	1	4	2
3	5	1	6	2	4
3	1	5	2	6	4
1	3	2	5	4	6

1	2	3	4	5	6
2	1	4	3	6	5
1	2	3	4	5	6
2	1	4	3	6	5
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3

Etc.

DOUBLE DODGING P.

TRIPLE DODGING P.

1	2	3	4	5	6
2	1	4	3	6	5
1	2	3	4	5	6
2	1	4	3	6	5
1	2	3	4	5	6
2	1	4	3	6	5
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3
6	4	5	2	3	1
6	5	4	3	2	1
5	6	3	4	1	2
6	5	4	3	2	1
5	6	3	4	1	2
5	6	3	4	1	2
5	3	6	1	4	2

1	2	3	4	5	6
2	1	4	3	6	5
1	2	3	4	5	6
2	1	4	3	6	5
1	2	3	4	5	6
2	1	4	3	6	5
1	2	3	4	5	6
2	1	4	3	6	5
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
4	6	2	5	1	3
6	4	5	2	3	1
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3
6	4	5	2	3	1
6	5	4	3	2	1

ALLIANCE PRINCIPLE

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
6	4	8	2	7	1	5	3
8	8	4	7	2	5	1	3

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8

All the Principles given as examples consist of a single Hunting Course with a number of Dodging Movements, similar to each other, inserted at intervals so as to produce a symmetrical Round Block.

The explanation of Method Construction I propose to give is this. That just as a Composer takes the Plain Cause of a Method, and from it by means of Bobs + Singles constructs Touches and peals: So you can take a Principle and from it by means of Shunts, construct Methods.

And that just as Bobs cannot be put haphazardly into a Deal, but must obey certain natural Laws, such as the Law of the 9 sets: So and equally, Shunts must obey certain natural Laws.

It has been objected that the Triple Bob Principle is impossible and does not exist. I do not understand the objection. Surely it cannot be denied that you can have a Round Block in which every bell does a

Treble Bob hunting path. Certainly there are repetitions of Rows but what is that to the point? A Principle is not a thing that you ring, but the foundation of Methods. You cannot get such Courses of Bedman, Triples without repetitions of rows. nor twenty three Courses of Cambridge Major without falseness. yet these Courses can be used to produce true peals.

My present definition differs somewhat from that of the Method Report. In that Report a Principle is defined as a collection of rows which form a perfect round block in which, -

- (a) each bell does the same work;
- (b) no bell moves up or down more than one place at a time;
- (c) no bell lies more than five consecutive blows in any one place.

(c) is wrong. It is a bad case of mixing up standards of good Methods with fundamental rules.

(a) is essential only if your finished Method is to conform to some standard.

(b) of course is implied in the nature of any Round Block.

At the time of the Method Report the Committee was of the opinion that any symmetrical Round Block which obeyed these rules was a Principle, and could be used as the base of Methods. As the result of further investigations I am of the opinion that the term can only be applied to Blocks in which the C.O. is the same throughout, and that rules (a) and (c) do not apply.

But though the Method Report definition is faulty, the general idea on which it was founded is sound, and was a great step forward in the then knowledge of Methods.

Chapter VI

Methods "in which every Bell
hath a Course alike."

All Methods which are constructed
in the traditional forms of ringing fall
into two groups:—

I Methods in which every bell hath
a Course alike.

II Methods which have a Hunt or
Hunts and Extreme (or Working) Bells.

We used to call the first group,
Principles used as Methods;
and the second group,
Methods founded on Principles;
but the altered definition of a Principle
makes these terms no longer applicable.

The Glossary calls the first group
the Stedman Group after the best
known method in it, and this is not
a bad name for it.

At other times these Groups have

been called Treble Dominated and now Treble Dominated; which are clumsy names, and may suggest an untruth. The name I have given to Group I is the description Steadman gave to his Method and does fairly distinguish it from other Methods. Its chief defect is in the obsolete meaning of the word Course, which must be taken as equal to "Work" or "movement".

Group I Methods subdivide as follows:-

- A. Original.
- B. Methods in which the Division Heads and Ends are those of the Principle on which it is founded; and which have Shunts made in the interior of the Divisions.
- C. Methods in which Shunts begun in one Division are completed in another; or in some cases are spread over three or more Divisions.

A. Original This is the Hunting Course used as the Course of a Method. It is interesting to notice that this Block

has different uses and different names at different stages in the science of ringing. First it is the Hunting Course, the most elementary form of movement possible. Then it is the Plain Principle, the foundation on which a large proportion of methods are built. Lastly it is Original a Complete Method in itself.

In its construction it shows most of the qualities of methods. It consists of a single cyclical movement; all methods consist of cyclical movements. It divides into a number of divisions, the number of divisions being equal to the number of bells making the movement. This quality is common to all methods, though in some cases it is not so obvious as in others. The Division Heads and Ends are the Rows of the Hunting Course; these are the natural Division Heads and Ends of all methods. It is symmetrical; and this symmetry is reproduced to a greater or less degree in all methods. It is an excellent method to study both from the point of construction

and Teal Composition. One or two Teals
of it have been rung, but owing to
the sameness of its work it is not
likely to be even a popular method.

B.

1	2	3	4	5	6
2	1	4	3	6	5
1	2	3	4	5	6
2	1	4	3	6	5
2	4	1	6	3	5
4	2	6	1	5	3
2	4	1	6	3	5
4	2	6	1	5	3
4	6	2	5	1	3
6	4	5	2	3	1
4	6	2	5	1	3
6	4	5	2	3	1
6	5	4	3	2	1
5	6	3	4	1	2
6	5	4	3	2	1
5	6	3	4	1	2
5	3	6	1	4	2
3	5	1	6	2	4
5	3	6	1	4	2
3	5	1	6	2	4

3	1	5	2	6	4
1	3	2	5	4	6
3	1	5	2	6	4
1	3	2	5	4	6
1	2	3	4	5	6

is the Treble Bob Principle
on six bells. It consists
of six equal divisions,
and all the bells work
alike. It is symmetrical
in form. Therefore it
would be very suitable
for the Cause of a method
but, for the fact that
it contains repetition
of rows. To make it
suitable we must
alter some of the Rows
so as to get rid of this

repetition. All the Methods in the Sub-division B. we are now considering have as their Division Heads and Ends the Rows of the Hunting Course. These are the Division Heads and Ends of the Principle and they must remain unaltered. The alteration must be in the Rows in the interior of the Division. The Division Heads and Ends include all the Rows in the same Coursing Order, therefore the alteration must be by introducing fresh C_o. Each Division of any Method in this Group is exactly alike in its work. Therefore it will be sufficient to take one Division and see what can be done with it, the other Divisions following automatically.

a	1	2	3	4	5	6	x
c	2	1	4	3	6	5	7.
d	1	2	3	4	5	6	3.
b.	2	1	4	3	6	5	

Rows a. and b may not be altered. Rows c and d. must be altered.

In the Change x the bells are making a forward movement. This movement we must interrupt in order to produce a Row different from c. As we saw on page 49 we have three alternatives.

First we can substitute backward movement of all the bells for the forward movement of all the bells. This would give us -

1	2	3	4	5	6
1	3	2	5	4	6

But backward movement on all the bells, equally with forward movement on all the bells, retains the same C.O. and produces the Row 132546. Which is already marked out as a Division End in the Method.

Second. We can turn the movement on all the bells, into two separate and independent cyclical movements, one on part of the bells, and the other on the rest. This is forbidden by the Condition of this Group of Methods that every bell hath a Cause alike.

Thirdly, we can substitute backward hunting for the forward hunting of some of the bells.

Thus 3 and 4 by forward hunting change positions. If all the bells

were backward hunting, 3 would go into
2nd position and 4 into 5th. But
if these two bells are backward
hunting among themselves only, the
result is as follows. 34
 34

This will be readily understood if we
see what would happen if the bells
were 3564 . Then the first change
of backward hunting would be. —

3564

3654

34 have now begun a cyclical movement
among themselves which tends to
return them to their original positions.
Continue the movement and we get —

p. 43 .

34

34

43

m. 43 .

34 .

Notice that the cycle
is completed from the
point p., half way
between 43 and 34 ,
and the point m,
half way between 43
and 34 . The last 34 need not
come up to complete the cycle.
Meanwhile the other bells have been
doing the combined forward and

Backward movement of the Treble Bob Principle, and the completion of the Hunting Course on 3-4

1	2	3	4	5	6
2	1	3	4	6	5
1	2	4	3	5	6
2	1	4	3	6	5
2	4	1	6	3	5

coincides with that movement. The bells drop again into the same Coursing Order and are in a position

to continue the cyclical movement of the Treble Bob Principle. But unless the Hunting Course on 3-4 is completed the Coursing Order is not regained, and the bells will not come round at the Course End.

We have therefore a primary cycle, that of the Principle, consisting of mixed forward and backward hunting; and a secondary cycle, on this bells 3-4, consisting of a Backward Hunting Course.

Secondary cycles like the above I call skunts. And by a skunt is to be understood not merely a breakage of Coursing Order but the whole movement which breaks and regains the Coursing Order. When I first, some years ago.

introduced the term, I applied it to any interruption of Causing Order. I called two such interruptions made in conjunction a Compound Shunt and the whole operation of breaking and regaining Causing Order a Compound Resolved Shunt. But in Method Construction the breakage of Causing Order without the means by which it is regained is meaningless. If you break C.O. it is implied (by the nature of a Round Block) that you regain it. And I now apply the term Shunt to the whole operation. Some people, however, who have copied my use of the word, use it still in my first meaning.

Since all the Divisions in the Method belonging to the Group we are considering are alike, it remains only to introduce into every Division a Shunt similar to the one we introduced into the first Division and you have a Plain Course of the Method.

By a Plain Course is meant any complete Course starting from any Row,

* The Courses of Grand Treble Bobs are not Plain Courses although there are no formal Bobs. The whole Method consisting of mixed Oxford and Kent.

87.
which Course is produced without Bobs, Singles, or any special Call.*

The Course beginning or ending with Rounds - 1 2 3 4 5 6 ... - is usually called the Plain Course. Rightly so in practical ringing, where Changes always begin with Rounds. In theoretic ringing this Course is nowise different from any other Course, except so far as every individual Course is composed of individual Rows. But following Convention I usually chose it for illustration.

The Method we have constructed - Forward Minor - consists of,
first the Treble Bob Principle, which has just equal Divisions, as many as there are bells.
and secondly of a Skunt in each Division consisting of a Backward Hunting Course on the first bell in 3-4.

The only feature which gives unity to the Course and which settles the length of the Course is the Principle. The Skunts are independent of each

T. B. PRINCIPLE

FORWARD MINOR

1 2 3 4 5 6
2 1 4 3 6 5
1 2 3 4 5 6
2 1 4 3 6 5
2 4 1 6 3 5
4 2 6 1 5 3
2 4 1 6 3 5
4 2 6 1 5 3
4 6 2 5 1 3
6 4 5 2 3 1
4 6 2 5 1 3
6 4 5 2 3 1
6 5 4 3 2 1
5 6 3 4 1 2
6 5 4 3 2 1
5 6 3 4 1 2
5 3 6 1 4 2
3 5 1 6 2 4
5 3 6 1 4 2
3 5 1 6 2 4
3 1 5 2 6 4
1 3 2 5 4 6
3 1 5 2 6 4
1 3 2 5 4 6
1 2 3 4 5 6

1 2 3 4 5 6
2 1 3 4 6 5
1 2 4 3 5 6
2 1 4 3 6 5
2 4 1 6 3 5
4 2 6 1 5 3
2 4 1 6 3 5
4 2 6 1 5 3
4 6 2 5 1 3
6 4 5 2 3 1
4 6 2 5 1 3
6 4 5 2 3 1
6 5 4 3 2 1
5 6 3 4 1 2
6 5 4 3 2 1
5 6 3 4 1 2
5 3 6 1 4 2
3 5 6 1 2 4
5 3 1 6 4 2
3 5 1 6 2 4
3 1 5 2 6 4
1 3 5 2 4 6
3 1 2 5 6 4
1 3 2 5 4 6
1 2 3 4 5 6

1 2 3 4 5 6
2 1 3 4 6 5
1 2 4 3 5 6
2 1 4 3 6 5
2 4 1 6 3 5
4 2 1 6 5 3
2 4 6 1 3 5
4 2 6 1 5 3
4 6 2 5 1 3
6 4 2 5 3 1
4 6 5 2 1 3
6 4 5 2 3 1
6 5 4 3 2 1
5 6 4 3 1 2
6 5 3 4 2 1
5 6 3 4 1 2
5 3 6 1 4 2
3 5 6 1 2 4
5 3 1 6 4 2
3 5 1 6 2 4
3 1 5 2 6 4
1 3 5 2 4 6
3 1 2 5 6 4
1 3 2 5 4 6
1 2 3 4 5 6

other. Any one could be altered or omitted without affecting the rest or altering the Course, except so far as the particular his bells are immediately concerned. This is shown by Example on page 88.

Forward Minor is an exact illustration of the construction of every Method in Group I Subdivision B.

First you have the Principle.

Then you have one or more Shuntis in each Division.

These Shuntis must always consist of Complete Movements - either Hunting Courses or Dodging Movements.

The simplest are a class of Methods in which the Principle is Triple Bob Hunting, Double Dodging Hunting, Triple Dodging Hunting etc. and the Shuntis consist of a Plain Hunting Course, the length of which exactly coincides with the number of Changes in a Division of the Principle.

These Hunting Courses will be reverse movement to the main movement of the

Principle. The following are Examples.

THE PRINCIPLE

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

FORWARD MAJOR

1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
1	2	4	3	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	5	6	8	7
1	2	3	4	6	5	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

BARNSBURY MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	3	5	4	6	8	7
1	2	5	3	6	4	7	8
2	1	5	6	3	4	8	7
1	2	6	5	4	3	7	8
2	1	6	4	5	3	8	7
1	2	4	6	3	5	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

THE PRINCIPLE

1	2	3	4	5	6	7
1	3	2	5	4	7	6
1	2	3	4	5	6	7
1	3	2	5	4	7	6
1	2	3	4	5	6	7
1	3	2	5	4	7	6
3	1	5	2	7	4	6

REVERSE ERIN TRIP.

1	2	3	4	5	6	7
2	1	3	5	4	7	6
2	3	1	4	5	6	7
3	2	1	5	4	7	6
3	1	2	4	5	6	7
1	3	2	5	4	7	6
3	1	5	2	7	4	6

ERIN TRIP.

1	2	3	4	5	6	7
2	1	4	3	6	5	7
2	4	1	6	3	7	5
2	1	4	3	6	5	7
2	4	1	6	3	7	5
2	1	4	3	6	5	7
2	4	1	6	3	7	5
4	2	6	1	7	3	5

1	2	3	4	5	6	7
2	1	4	3	6	5	7
1	2	4	6	3	7	5
1	4	2	3	6	5	7
4	1	2	6	3	7	5
4	2	1	3	6	5	7
2	4	1	6	3	7	5
4	2	6	1	7	3	5

REVERSE ERIN TRIPLES

1	2	3	4	5	6	7
2	1	4	3	6	5	7
1	2	3	4	5	6	7
2	1	4	3	6	5	7
1	2	3	4	5	6	7
2	1	4	3	6	5	7
2	4	1	6	3	7	5

1	2	3	4	5	6	7
2	1	4	3	5	7	6
1	2	3	4	7	5	6
2	1	4	3	7	6	5
1	2	3	4	6	7	5
2	1	4	3	6	5	7
2	4	1	6	3	7	5

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	6	8	5	7
2	1	4	6	3	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
1	2	4	3	6	5	8	7
2	1	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7

1	2	3	4	5	6	7	8
2	1	3	5	4	7	6	8
1	2	5	3	7	4	8	6
2	1	5	7	3	8	4	6
1	2	7	5	8	3	6	4
2	1	7	8	5	6	3	4
1	2	8	7	6	5	4	3
2	1	8	6	7	4	5	3
1	2	6	8	4	7	3	5
2	1	6	4	8	3	7	5
1	2	4	6	3	8	5	7
2	1	4	3	6	5	8	7

The foregoing class of Methods we will call the FORWARD CLASS.

When the Principle is the Double Dodging, 4-full Dodging, 6-full Dodging, and so on in a regular progression (2-4-6-8-10-12 etc). The Shunt will be made by an odd number of bells, and must be immediately next Before or Behind.

When the Principle is the Treble Bob, 3 full Dodging, 5-full dodging and so on in a regular progression (1-3-5-7-9-11 etc) The Shunt will be made by an even number of bells; and may be either at Behind or Before or in the interior. When the Shunt is made at Behind or Before, certain bells will lie or lead ^{four} ~~three~~ consecutive blows.

The next Class of Methods consists of those in which two or more similar Shunts are made in the same Division. The following Examples will be sufficient explanation:—

THE PRINCIPLE.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	3	4	5	6	8	7
1	2	4	3	6	5	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
1	2	4	3	5	6	8	7
2	1	3	4	6	5	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	6	3	5	7	8
1	4	2	3	6	7	5	8
4	1	2	6	3	7	8	5
4	2	1	3	6	8	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5

Two similar Shunts cannot be made in the same Division of any Principle on an odd number of bells.

When the Principle is the Double Dodging or in the following progression (2-4-6-8-10-- full dodging) and when the dodging is in 2-3, 4-5, 6-7 etc; the Shunts will be Hunting Courses on an odd number of bells. and must be made immediately next Before and Behind, never in the interior of the Division.

When the Principle is 2-4-6-8-- pull dodging, and the dodging is in 1-2, 3-4, 5-6 etc. these Shunts cannot be made.

When the Principle is Treble Bob or in the following progression (1-3-5-7-9-- pull dodging). The positions and possible numbers of Shunts are in direct ratio to the number of bells.

Consequently a simple formula can be set down giving all possible Methods in the last two Classes (see Formula No. page.

The next Class consists of Methods that have two or more dissimilar

Sheets in each Division Examples:-

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
1	2	4	3	6	5	7	8
2	1	3	4	5	6	8	7
1	2	4	3	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	5	6	8	7
1	2	4	3	6	5	7	8
2	1	3	4	5	6	8	7
1	2	3	4	6	5	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7

1	2	3	4	5	6	7	8
2	4	3	6	5	8	7	
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	6	8	5	7
1	3	2	6	4	8	7	5
3	1	6	2	4	7	8	5
3	6	1	4	2	7	5	8
6	3	4	1	2	7	8	5
4	4	3	2	1	7	5	8
4	6	2	3	1	5	7	8
4	2	6	1	3	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5

1	2	3	4	5	6	7	8	9
2	1	4	3	6	5	8	7	9
2	4	1	6	3	8	5	9	7
2	1	4	3	6	5	8	7	9
2	4	1	6	3	8	5	9	7
2	1	4	3	6	5	8	7	9
2	4	1	6	3	8	5	9	7
2	1	4	3	6	5	8	7	9
2	4	1	6	3	8	5	9	7
2	1	4	3	6	5	8	7	9
2	4	1	6	3	8	5	9	7
4	2	6	1	8	3	9	5	7

1	2	3	4	5	6	7	8	9
2	1	4	3	6	5	8	7	9
1	2	3	4	6	8	5	9	7
1	3	2	6	4	8	9	5	7
3	1	6	2	4	9	8	7	5
3	6	1	4	2	9	7	8	5
6	3	4	1	2	7	9	5	8
6	4	3	2	1	7	5	9	8
4	6	2	3	1	5	7	8	9
4	2	6	1	3	5	8	7	9
2	4	1	6	3	8	5	9	7
4	2	6	1	8	3	9	5	7

2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6

2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
1	2	4	3	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	2	5	3	7
6	8	4	7	5	2	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	4	3	1	2
8	7	6	5	3	4	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	5	2	4	7	6	8
3	1	2	5	7	4	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6

2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
1	2	4	3	6	5	7	8
2	1	4	3	5	6	8	7
2	4	1	5	3	8	6	7
4	2	5	1	8	3	7	6
4	5	2	8	1	7	3	6
5	4	8	2	7	1	6	3
5	8	4	7	2	6	1	3
8	5	7	4	2	6	3	1
5	8	7	4	6	2	1	3
8	5	4	7	6	2	3	1
8	4	5	6	7	3	2	1
4	8	6	5	7	3	1	2
8	4	6	5	3	7	2	1
4	8	5	6	3	7	1	2
4	5	8	3	6	1	7	2
5	4	3	8	1	6	2	7
5	3	4	1	8	2	6	7
3	5	1	4	2	8	7	6
3	1	5	2	4	7	8	6
1	3	5	2	7	4	6	8
3	1	2	5	7	4	8	6
1	3	2	5	7	4	6	8
3	1	5	2	4	7	8	6

A

2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6

B.

2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	3	5	4	6	8	7
2	3	1	4	5	8	6	7
2	1	3	5	4	6	8	7
2	3	1	4	5	8	6	7
2	1	3	5	4	8	7	6
2	3	1	4	5	7	8	6
3	2	1	5	4	8	7	6
3	1	2	4	5	7	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6

C

2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	3	5	4	6	8	7
2	3	1	5	4	8	6	7
2	1	3	4	5	6	8	7
2	3	1	5	4	8	6	7
2	1	3	4	5	8	7	6
2	3	1	5	4	7	8	6
3	2	1	4	5	8	7	6
3	1	2	4	5	7	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6

D

2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	3	5	4	6	8	7
2	3	1	5	6	4	7	8
3	2	5	1	4	6	8	7
2	3	1	5	4	8	6	7
3	2	1	4	5	8	7	6
2	3	4	1	5	7	8	6
3	2	1	4	7	5	6	8
3	1	2	4	5	7	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6

In all these Methods there are:—

First, the Principle. That is a Cyclical movement shared equally by all the bells. This alone gives unity to the Course and settles the number of Rows in the Course, as well as the number of Divisions and the Division Heads and Ends.

Second, a number of Shunts one or more in each Division. Each Shunt is a Cyclical movement on part of the bells, and consists of either a Hunting Course or of a Dodging Movement. Each Shunt is independent and complete in itself.

The Examples given on pages 90, 91, 92, 94 and 96 are easily understood. In them the Shunts are all Hunting Courses, the movement being retrograde to the movement of the Principles.

In the first Example on page 96 a each Division has five Shunts the first being a Hunting Course on five bells the other a Dodging Movement on three bells, four changes of forward movement being followed by four changes of backward movement.

The Principle of Example on page 97.

consists of a Hunting Course of backward movement into each Division of which a Hunting Course of forward movement and four Dodging Movements are inserted. Each Division has six Shunts, each a Hunting Course on five bells.

The first Example on page 98 is rather more complex but the construction is essentially the same.

The Principle is the 4-pull Dodging Principle on eight bells.

Figure B is produced by two 3-bell Hunting Courses; one consisting of a^1 and a^2 is done in two pieces; the other consisting of b^1, b^2, b^3 is in three pieces.

Figure C is produced from Figure B by one 2-bell Hunting Course on 5-bells which is in two pieces.

Figure D.

In this last Example some of the bells are not only engaged in the primary cycle of the Principle and the secondary cycle of a Skunt, but at the same time in more than one secondary cycle. The actual movement of the bell depends not on one cycle only but on the total of all the movements cycles.

All the Methods I have given as examples divide into a number of equal Divisions and each Division is symmetrical in form. This is so because first the Principles are symmetrical, and second because the arrangements of the Skunts in the Divisions are symmetrical. These Methods conform to the standard of Symmetry usually accepted by the Exercise.

But the essential features of the Construction of these Methods do not depend on this symmetry. Each Hunting Course, and each Dodging Movement, in a Principle is in itself symmetrical; but the arrangement of these Hunting Courses

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2

Continued.

1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
1	2	4	3	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	1	3	6	8	7	5
2	4	3	1	8	6	5	7
4	2	3	8	1	6	7	5
2	4	8	3	6	1	5	7
4	2	8	6	3	1	7	5
2	4	6	8	1	3	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	1	7	5	3
4	6	2	8	7	1	3	5
6	4	2	8	7	1	5	3
4	6	8	2	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	4	3	1	2
8	7	6	5	3	4	2	1
7	8	5	6	3	4	1	2

Continued.

7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8

7	5	8	3	6	1	4	2
5	7	8	3	1	6	2	4
7	5	3	8	6	1	4	2
5	7	8	3	6	1	2	4
7	5	3	8	1	6	4	2
5	7	3	8	6	1	2	4
7	5	8	3	1	6	4	2
5	7	3	8	6	1	2	4
7	5	8	3	1	6	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	8	2	4	6
3	5	7	1	2	8	6	4
5	3	1	7	8	2	4	6
5	3	7	1	2	8	6	4
3	5	7	1	8	2	4	6
5	3	1	7	2	8	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	5	2	4	7	6	8
3	1	2	5	7	4	8	6
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8

and Dodging Statements within the Principle needs not be symmetrical.

And each Shunt is, in itself, symmetrical but the arrangement of the Shunts within the Divisions needs not be symmetrical. Neither is there any essential need for the Shunts in one Division to be similar to those in another. Of course the capacity of the Method of producing the full extent of the Rows depends largely on its symmetry and the regularity of its Divisions, but that is a point which does not concern us here.

On page 102 is an Example of a Method founded on an unsymmetrical Principle, which has also unequal Divisions, some of the Divisions not being symmetrical. It will be seen that in all essential things its construction is similar to that of the other Methods given as illustrations.

As all the Examples given are produced from Principles by means of Shunts, so every Method in Group I in which the Division Heads and Ends are in the

same Causing Order, are produced. There is no exception.

Subdivision C. Methods in which a Theme begun in one Division is continued and completed in one or more other Divisions.

It seems to be the general opinion that the construction of Group I Methods depends on (a) having a Division End which will repeat the required number of times; and (b) on all the Divisions being exactly similar.

Thus you write down a number of Rows on x bells to form your first Division. The Division End is a Row which will repeat $x-1$ times. You repeat the whole Division $x-1$ times and you have your plain Course.

Different men insist on various other conditions. Some for instance that the Divisions should be symmetrical. Some that the Division Heads and Ends should be in the same Causing Order. But these conditions are secondary, the others are essential.

Now, if the essential thing about the construction of these Methods is that the Division Ends should repeat the required number of times, then clearly any set of Rows which will so repeat is valid. Bob Major Lead Ends (i.e. Division Heads and Ends that are all in the same Counting Order) might be, for other reasons, superior, but essentially they would be one set among many sets. "Of course," to quote Sir Arthur Heywood, "there are scores of Lead Ends that will produce a cycle", and if the above hypothesis is sound he was right to argue that they are all of equal value.

But we saw that in the case of Methods in which the Division Heads and Ends are all in the same Counting Order, the length of the Cycle and the number of Divisions depend on the Principle P.I.E. on the primary Cyclical movement in which all the bells are concerned, and not on the ability of the Division Ends to repeat, or on the Divisions being exactly similar. The Point is 3-4

in the first Division of Forward is Complete,
in itself, and has no Constitutional Connection

1 2 3 4 5 6
2 1 4 3 6 5
1 2 4 3 5 6
2 1 3 4 6 5
2 3 1 6 4 5
3 2 6 1 5 4
2 3 1 6 4 5
3 2 6 1 5 4
3 6 2 5 1 4
6 3 5 2 4 1
3 6 2 5 1 4
6 3 5 2 4 1
6 5 3 4 2 1
5 6 4 3 1 2
6 5 4 3 2 1
5 6 3 4 1 2
5 3 6 1 4 2
3 5 1 6 2 4
5 3 6 1 4 2
3 5 1 6 2 4
3 1 5 2 6 4
1 3 2 5 4 6
3 1 5 2 6 4
1 3 2 5 4 6
1 2 3 4 5 6

with the similar Stunts
in other Divisions. Clearly
it must be equally true
that any similar Stunt
begun in one Division
and completed in another
is also self-contained
and independent. It
has no effect except so
far as the two bells making
it are immediately concerned.
It obscures the "Bob Major
Lead Ends" of the
Principle but they remain
the "natural" Division
Heads and Ends of the
Course. And as in
the case of the Methods
we have previously
considered the Principle
remains the one thing
which settles the length
of the Course and the
number and size of the
Divisions.

A The PRINCIPLE

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	3	6	5	7	8
2	1	3	4	5	6	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
4	6	2	8	1	7	3	5
6	4	2	8	1	7	5	3
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1

C. DUFFIELD MAJOR

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	3	6	5	7	8
2	1	6	4	3	8	7	5
1	2	6	5	4	3	7	8
2	1	5	6	3	4	8	7
2	5	1	3	6	8	4	7
5	2	3	1	8	6	7	4
2	5	3	8	1	6	4	7
5	2	8	3	6	1	7	4
2	5	8	6	3	1	4	7
5	2	6	8	1	3	7	4
5	6	2	1	8	7	3	4
6	5	1	2	7	8	4	3
5	6	1	7	2	8	3	4
6	5	7	1	8	2	4	3
5	6	7	8	1	2	3	4
6	5	8	7	2	1	4	3
6	8	5	2	7	4	1	3
8	6	2	5	4	7	3	1
6	8	2	4	5	7	1	3
8	6	4	2	7	5	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1

A is the Double Dodging Principle on eight bells.

B is produced from A by making five Complete Shunts in each Division, each Shunt being a backward Hunting Course on five bells.

C is produced from B by eight independent Shunts (four in each half of the Course) A Shunt on 6-3 is begun in the first Division and completed in the second

A Shunt on 4-5 is begun in the first Division and completed in the fourth

A Shunt on 1-8 is begun in the second Division and completed

in the third. And so on.

This clearly shows that Duffield Major is produced by a number of cyclical movements just as much as Forward Major is. And in the same way it can be shown that every Round Block is so produced.

On page 109 I give another example.

B is produced from the Principle, by a number of Shunts each consisting of Hunting Courses on five bells.

C is produced from B. by a number of Shunts each of which consists of substituting two Dodging Movements for a Hunting Course on five bells.

AB		AB
BA	instead of	AB
AB		BA
BA		BA

In each Division of C. the result of the Shunt is that three bells take three steps in a Backward Hunting Course, — that is, exactly half the complete cycle. Three steps Forward is also exactly half the complete

A. The Principle

1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
3	5	1	7	2	8	4	6
5	3	7	1	8	2	6	4
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1

B.

1	2	3	4	5	6	7	8
1	2	3	5	4	6	7	8
1	3	2	4	5	7	6	8
1	3	2	5	4	7	6	8
3	1	5	2	7	4	8	6
3	1	5	7	2	4	8	6
3	5	1	2	7	8	4	6
3	5	1	7	2	8	4	6
5	3	7	1	8	2	6	4
5	3	7	8	1	2	6	4
5	7	3	1	8	6	2	4
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
7	5	8	6	3	4	1	2
7	8	5	3	6	4	1	2
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1

C. CONWAY MAJOR

1	2	3	4	5	6	7	8
2	1	3	5	4	6	8	7
2	3	1	4	5	8	6	7
3	2	1	5	4	8	7	6
2	3	5	1	8	4	6	7
3	2	5	8	1	4	7	6
3	5	2	1	8	7	4	6
5	3	2	8	1	7	6	4
3	5	8	2	7	1	4	6
5	3	8	7	2	1	6	4
5	8	3	2	7	6	1	4
8	5	3	7	2	6	4	1
5	8	7	3	6	2	1	4
8	5	7	6	3	2	4	1
8	7	5	3	6	4	2	1
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1

D. BANGOR MAJOR

1	2	3	4	5	6	7	8
2	1	3	5	4	7	6	8
2	3	1	4	5	7	8	6
3	2	1	5	4	8	7	6
2	3	5	1	8	4	6	7
3	2	5	8	1	6	4	7
3	5	2	1	8	6	7	4
5	3	2	8	1	7	6	4
3	5	8	2	7	1	4	6
5	3	8	7	2	4	1	6
5	8	3	2	7	4	6	1
8	5	3	7	2	6	4	1
5	8	7	3	6	2	1	4
8	5	7	6	3	1	2	4
8	7	5	3	6	1	4	2
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1

Cycle and brings the bells to the same point. Therefore one can be substituted for the other

678		678
768	instead of	687
786		867
876		876.

This Shunt made in each Division produces D.

These last five Methods, Conway and Bangor (p. 109) raise a rather important point. I have pointed out that every Round Block must consist of a number of complete cyclical movements on all or part of the bells; either of full cycles, or of forward and backward movement along arcs of cycles; yet in these two Methods we have, since in each Division, three bells which make half a Hunting Course only, and the second half is made nowhere, neither in the same Division nor in any other Division. Does this not prove that my statement

is wrong? No. The point is that not every case, where a number of bells is hunting together, is part of one of the movements in the construction of the method. These two methods actually are produced by a number of complete cyclical movements, as I have shown. As a result of these movements some of the bells do part of other movements; but these latter are only accidental and need not be completed.

Similarly if in any method certain bells begin a hunting course among themselves, it does not follow that that hunting course will be completed. But it is certain that the movement of the bells, (and all the movement of the bells), is part of some cycle or arc (or cycles or arcs) which must be completed before the bells can return to the Row from which they started.*

* In the case of an arc the bells must traverse it and return along it to its starting point.

Chapter VII

Hunts.

A Hunt is a Bell that performs a cyclical movement through the Coupling Order of other Bells which are called Extreme Bells.

Extreme Bells. These are more usually called "Working" Bells. But as this term is liable to cause misunderstanding I revert to the older and better term.

Before explaining what a Hunt is, it will be well to say what it is not. It is not, necessarily, a bell which has a simple or regular path, or one that is repeated a number of times. A Hunt's path may be both simple and regular, and it may be repeated, but it may also be complex and irregular.

A Hunt is a bell which does a distinct and important Constitutional work; one of the most important in the whole Science of Ringing

The term is one of the oldest we

have, and from the earliest times it was used for this Constitutional work. Steadman informs us that the first step in the development of ringing was "the invention of the Sices". He goes on to explain that the Sices were not rung as Hunting Courses, as they could have been rung, and as we should have expected them to be rung, but as Hunt and Excieme Bells. He then fully describes this way of ringing them. What a

Fig 1.

1	2	3	4
2	1	3	4
2	3	1	4
2	3	4	1
3	2	4	1
3	2	1	4
3	1	2	4
1	3	2	4
1	2	3	4

can be seen from Fig 1.

It is the cyclical path of one bell (in the Ex. the treble) through the other bells until it returns to its original position. The Hunt moves, the other bells stay still, except when each has to make way for the treble. Really

what is going on is a continual alteration in the relative positions of the Hunt on the one hand, and

The Extreme Bells on the other hand. The Extreme Bells retain the same relative positions among themselves, but as their positions relative to the Hunt are continually changing, they share the movement equally with that bell. This is shown clearly, and in a most instinctive way, in the fourth Change. Here the Hunt is lying its whole Pull behind. If the Extreme Bells also continued to lie still, the relative movement would cease. So to carry on that movement, as the Hunt is lying still, the Extreme Bells must move, — they must make what the Ancients called an Extreme Change.

The following things can clearly be seen from the Example 1.; and they are the important characteristics of all operations consisting of Hunts and Extreme Bells.

1. The operation divides the bells into two kinds.
 - (a) The Hunt (or Hunts)

(b) The Extreme Bells.

2. So far as the operation is concerned the Hounts (if there be more than one) retain the same relation to each other throughout; and the Extreme Bells retain the same relation to each other throughout.
3. But the relation of the Hount (or Hounts) to the Extreme Bells is altered at every Change.
4. The Hount's path consists of changing positions with each of the Extreme Bells, as it comes to it. It can change position with only one bell at a time and only with the bell next to it.
5. The Hount's path is Cyclical. If it begin by changing positions with the Bell next after it, and if the movement thus begun is persisted in, it will return to the position from which it started, by completing the cycle; changing

positions on the way with all the Extreme Bells in due order.

Fig II

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	6	5	8	7
4	2	3	1	6	5	8	7
4	3	2	6	1	5	8	7
4	3	6	2	5	1	8	7
4	3	6	5	2	8	1	7
4	3	6	5	8	2	7	1
4	3	6	5	8	7	2	1
3	4	5	6	7	8	1	2
3	4	5	6	7	1	8	2
3	4	5	6	7	2	8	1
3	4	5	1	6	2	7	8
3	4	1	5	2	6	7	8
3	1	4	2	5	6	7	8
3	2	4	5	6	7	8	1
1	2	3	4	5	6	7	8

Fig II shows a Round Block with two Hunts (1 and 2) and six Extreme Bells, and it will be seen that it is similar to Fig I (page 113).

The two Hunts retain the same relationship to each other; but this relationship is not the same relation in position but in Counting Order.

This has got to be borne in mind to understand the

nature of a Hunt. Bells in the same relationship means bells which are at the same time doing the same cycle, whether they be Hunts or Extreme Bells. In Fig II the two

Hunts are both, at the same time, doing Plain Forward Hunting.

The Extreme Bells are not actually doing a cycle, but they are in the position of all doing the same cycle at the same time. There is potential movement among themselves, besides being relative movement as regards the Hunts.

In modern forms of ringing this potential movement does not occur; or occurs only in an obscure manner. But potential movement is to be considered a real thing in the Science of Ringing and since it is potentially cyclical it has Coursing Order.

Thus, the operation of Hunt and Extreme Bells is the interworking of two cyclical movements; one, that of the Hunts, with a Common Coursing Order; the other that of the Extremes with a Common Coursing Order. And the two cycles will each be repeated until the completion of one coincides with the completion of the other,

When the original Coupling Order of all the Bells is regained, and the Bells return to the Row from which they started.

Fig III

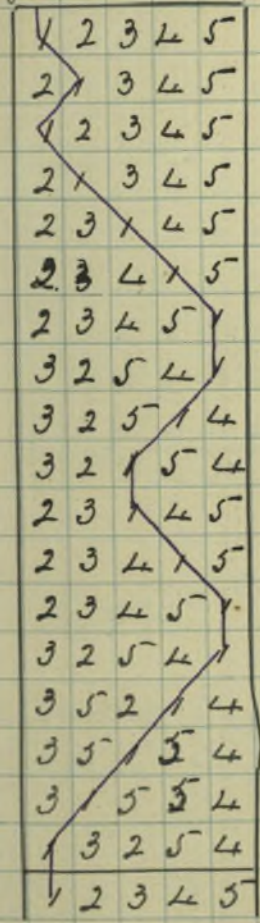


Fig III shows a Hunt with a more complex path. It is still strictly cyclical, but instead of doing a complete cycle straight off, it introduces dodging movements into its path. All the laws of cyclical movement and of Hunts are however obeyed to the letter.

This example too furnishes an illustration of Hunts in more complex methods; the potential movement of the Extreme Bells being replaced by actual cyclical

movement.

Fig IV

		Coursing Order.															
1	2	3	4	5	6	7	8	←	2	1	3	5	7	8	6	4	a
1	3	2	5	4	7	6	8										
1	3	5	2	7	4	8	6	←	2	3	1	5	7	8	6	4	b.
1	5	3	7	2	8	4	6										
1	5	7	3	8	2	6	4	←	2	3	5	1	7	8	6	4	c
1	7	5	8	3	6	2	4										
1	7	8	5	6	3	4	2	←	2	3	5	7	1	8	6	4	d.
1	8	7	6	5	4	3	2										
1	8	6	7	4	5	2	3	←	2	3	5	7	8	1	6	4	e
1	6	8	4	7	2	5	3										
1	6	4	8	2	7	3	5	←	2	3	5	7	8	6	1	4	f
1	4	6	2	8	3	7	5										
1	4	2	6	3	8	5	7	←	2	3	5	7	8	6	4	g	
1	2	4	3	6	5	8	7										
1	2	3	4	5	6	7	8										

Fig V

The Coursing Order.

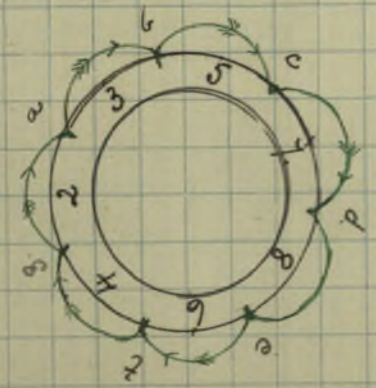


FIG IV (page 119) is another illustration of Hunt and Extreme Bells.

The first Change - $\begin{array}{cccccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ & & 1 & 3 & 2 & 5 & 4 & 7 & 6 & 8 & - \end{array}$

is backward movement on all the Bells and if continued will produce a Complete Hunting Course ^{second}

But in the Third Change, a secondary movement is introduced. In addition to the cyclical movement of all the bells a movement is begun by 1 and 3 changing positions.

If the primary cycle only were made, the second Change would be -

$$\begin{array}{cccccccc} 1 & 3 & 2 & 5 & 4 & 7 & 6 & 8 \\ 3 & 1 & 5 & 2 & 7 & 4 & 8 & 6 & - \end{array}$$

and if added to this a secondary cycle is begun by 1-3 Changing positions, the second Change will be -

$$\begin{array}{cccccccc} \underline{1} & \underline{3} & 2 & 5 & 4 & 7 & 6 & 8 \\ 1 & 3 & 5 & 2 & 7 & 4 & 8 & 6 \end{array}$$

The primary cycle is now resumed, and the Third Change will be -

$$\begin{array}{cccccccc} 1 & 3 & 5 & 2 & 7 & 4 & 8 & 6 \\ 1 & 5 & 3 & 7 & 2 & 8 & 4 & 6 \end{array}$$

The result of this double movement is first, that the pebble remains on the

Lead. This is however not because of absence of movement, but as the result of two movements, one positive and the other negative.

And, second, the Coupling Order of the bells is altered by 1 and 3 changing positions. The Coupling Order by the first Change is -

2 1 3 5 7 8 6 4

That of the third Change is 2 3 1 5 7 8 6 4

In the fourth Change the treble changes positions with the 5.

1 5 3 7 2 8 4 6

1 5 7 3 8 2 6 4

and in the fifth Change, where all the bells are doing the primary cycle, the Coupling Order is -

2 3 5 1 7 8 6 4

Similarly as each Extreme Bell, comes to the Hunt, those two bells change positions, until the Hunt has completed

~~2 1 3 5 7 8 6 4~~

~~2 3 1 5 7 8 6 4~~

~~2 3 5 1 7 8 6 4~~

~~2 3 5 7 1 8 6 4~~

~~2 3 5 7 8 1 6 4~~

~~2 3 5 7 8 6 1 4~~

~~2 3 5 7 8 6 4 1~~

a cycle as shown in Fig V (p. 119) when the treble is again between 2 and 3, the original Coupling

Order of all the bells is regained, and the bells return to the Row from which they started.

The result of this cyclical movement of the Hunt is that the Extreme Bells make a Complete Hunting Course among themselves.

The primary movement on all the bells is Backward.

The Hunting Course on the Extreme Bells is the opposite and therefore Forward.

The Construction of the Blocks shown in Fig IV (p 119) consists of three Complete Cycles.

1. The primary cycle of all the bells.
2. The cycle of the Hunt in Coursing order.
3. The Hunting Course on the Extreme Bells.

In Fig IV the Hunt is one bell. Figs. VI. VIII & (TP123-4.5) show similar Blocks with two bells as Hunt.

In Fig VIII the Hunt perform a Hunting Course among themselves. In Fig X they perform Dodging Movements among themselves.

Fig VI.

1	2	3	4	5	6	7	8
1	2	4	3	6	5	8	7
1	2	4	6	3	8	5	7
1	2	6	4	8	3	7	5
1	2	6	8	4	7	3	5
1	2	8	6	7	4	5	3
1	2	8	7	6	5	4	3
1	2	7	8	5	6	3	4
1	2	7	5	8	3	6	4
1	2	5	7	3	8	4	6
1	2	5	3	7	4	8	6
1	2	3	5	4	7	6	8
1	2	3	4	5	6	7	8

Coursing Order.

← 3 **12**. 4 6 8 7 5 a

← 3 4 **12** 6 8 7 5 b.

← 3 4 6 **12** 8 7 5 c

← 3 4 6 8 **12** 7 5 d.

← 3 4 6 8 7 **12** 5 e

← 3 4 6 8 7 5 **12**. f

Fig VII

The Coursing Order.

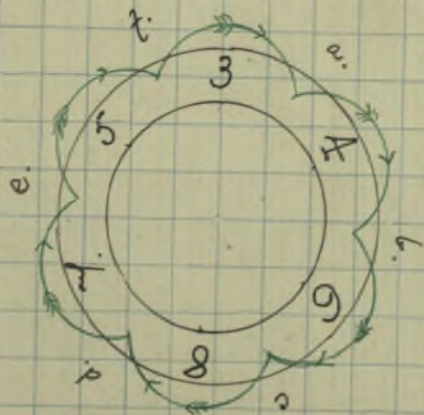


Fig VIII

Coursing Order.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	1	4	6	3	8	5	7
1	2	6	4	8	3	7	5
1	2	6	8	4	7	3	5
2	1	8	6	7	4	5	3
2	1	8	7	6	5	4	3
1	2	7	8	5	6	3	4
1	2	7	5	8	3	6	4
2	1	5	7	3	8	4	6
2	1	5	3	7	4	8	6
1	2	3	5	4	7	6	8
1	2	3	4	5	6	7	8

- ← 3 **1** 2. 4 6 8 7 5 a
- ← 3 4 **2** 1 6 8 7 5 b.
- ← 3 4 6 **1** 2 8 7 5 c
- ← 3 4 6 8 **2** 1 7 5 d.
- ← 3 4 6 8 7 **1** 2 5 e
- ← 3 4 6 8 7 5 **2** 1. f.

Fig IX

The Coursing Order.

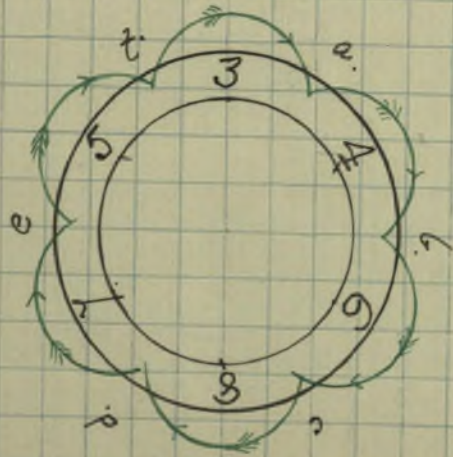


Fig X.

1	2	3	4	5	6	7	8	←	3	1	2	4	6	8	7	5	a
2	1	4	3	6	5	8	7	←	3	4	1	2	6	8	7	5	b
1	2	4	6	3	8	5	7	←	3	4	6	1	2	8	7	5	c
2	1	6	4	8	3	7	5	←	3	4	6	8	1	2	7	5	d
1	2	6	8	4	7	3	5	←	3	4	6	8	7	1	2	5	e
2	1	8	6	7	4	5	3	←	3	4	6	8	1	2	7	5	f
1	2	8	7	6	5	4	3	←	3	4	6	8	7	1	2	5	g
2	1	7	8	5	6	3	4	←	3	4	6	8	7	1	2	5	h
1	2	7	5	8	3	6	4	←	3	4	6	8	7	1	2	5	i
2	1	5	7	3	8	4	6	←	3	4	6	8	7	1	2	5	j
1	2	5	3	7	4	8	6	←	3	4	6	8	7	1	2	5	k
2	1	3	5	4	7	6	8	←	3	4	6	8	7	1	2	5	l
1	2	3	4	5	6	7	8										

Fig XI

The Coursing Order.

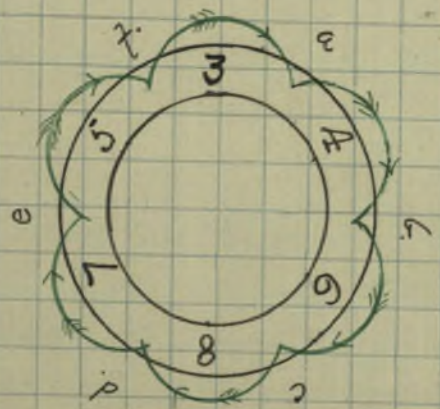


FIG XII



Let FIG XII represent the Coursing Order of any Principle.

To be an accurate illustration, this figure should be doubly Cyclical -

1. each line should be a cycle
2. the order of the lines should be in a cycle, the first one following the last.

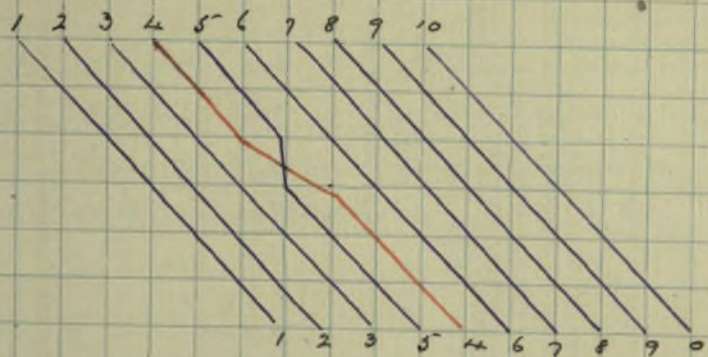
Such a figure, of course, cannot be put down on paper, but it must be understood.

Sp. FIG. XII Let one bell - 4 - be a Hunt.

It can change positions either with the bell Coursing next before it, or the one Coursing next after it.

Let it change with the bell next after it - 5 -.

Fig XIII



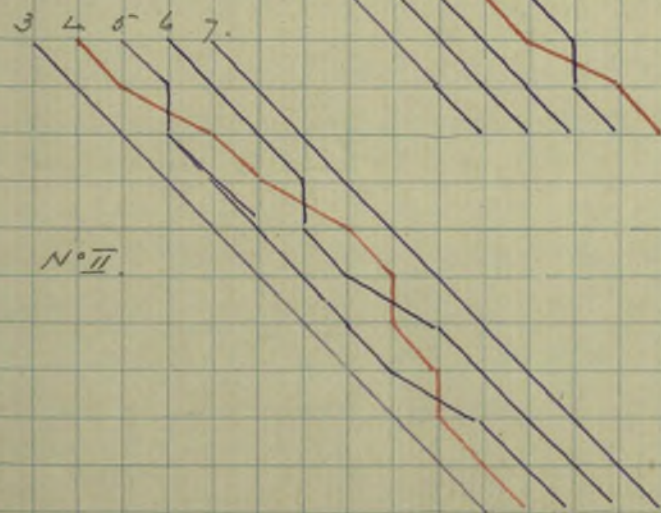
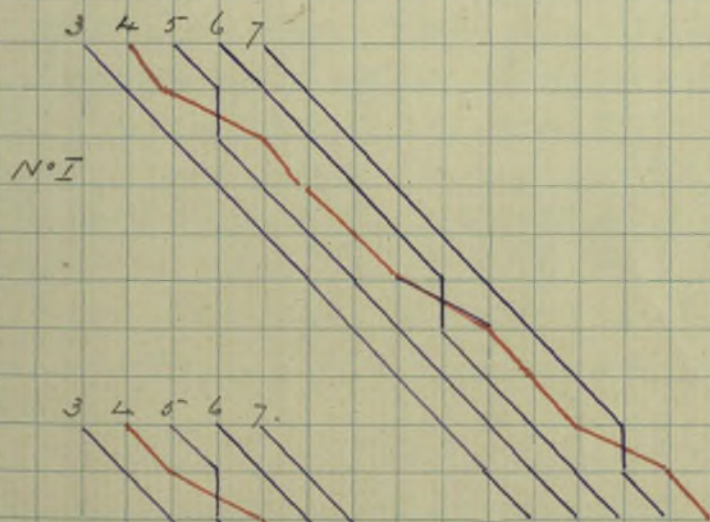
This introduces a fresh Courning Order. The bells cannot return to the Row from which they started until the original Courning Order is regained.

If it remains a Hunt and 1,2,3,5,7,8,9,0 remain Extreme Bells, the original Courning Order can be regained only in one of three ways.

1. The Hunt can complete its cyclical path in Courning Order, changing positions successively with each of the Extreme Bells as it meets them.
2. Having changed positions with one or more Extreme Bells, it can regain its original position by changing positions with the same bells, but in reverse order.

3. A Combination of 1- and 2.

These three are the equivalents of the
Plain Hunting, the Dodging Movement,
and the mixed Plain Hunting and
Dodging Movement



One of the best examples of a Hunt and Exclamation Bells, and one where practical ringing in the tower shows the nature of a Hunt, is the Plain Course of 13 or Major.

When you start ringing it from Rounds, the order you meet the bells (which is the Counting Order) is 31246875
Immediately after 2nds is made at the first Lead End the order is -
13246875

The working bells are all in the same order as in the first Lead, but 1 and 3 have changed positions, the bell is between 3 and 5 instead of between 2 and 3.

In the third Lead, the bell and 5 have changed positions, and the bell is between 5 and 7.

In the fourth Lead 1 and 7 have changed positions, and the bell is between 7 and 8.

In the fifth Lead, 1 and 8 have changed positions, and the bell is between 8 and 6.

In the sixth Lead, 1 and 6 have changed positions, and the bell is

between 6 and 4.

In the seventh Lead, the riddle has changed positions with the 4th, and is between 4 and 2.

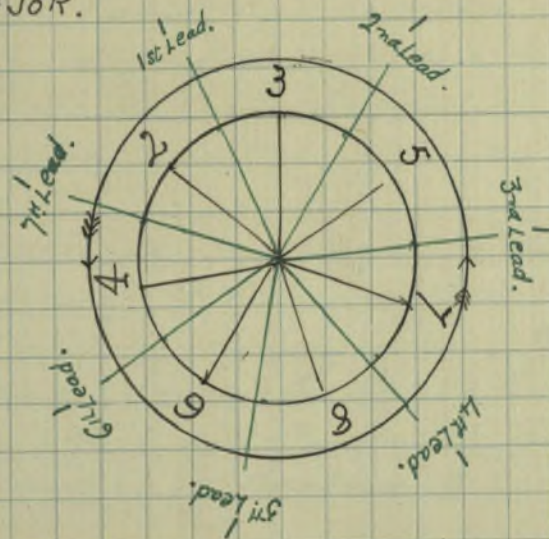
At the East Lead end 1 and 2 change positions, and the riddle is between 2 and 3.

This is her first position, the original Coursing Order is regained, and the bells return to the Row from which they started.

All through the Working Bells keep the same Coursing Order, and during the Course the riddle makes a complete cycle through them, changing position in Coursing Order with one at a time, in the order in which it comes next to them.

It is this cyclical movement, that makes the riddle a Hunt, not its regular, uninterrupted, and repeated hunting path.

The Plain Course of
BOB. MAJOR.



Coursing Order.

First. Lead	2 4 6 8 7 5 3 1
Second. do	2 4 6 8 7 5 1 3
Third. do	2 4 6 8 7 1 5 3
Fourth. do	2 4 6 8 1 7 5 3
Fifth. do	2 4 6 1 8 7 5 3
Sixth. do	2 4 1 6 8 7 5 3
Seventh. do	2 1 4 6 8 7 5 3
First do.	1 2 4 6 8 7 5 3

The Division of the Plain Course of Bob Major into equal Leads, and the number of Leads, depend on the number of

steps the Hunt has to make to complete is cyclical movement, and not on the Lead End and its Capacity to repeat the required number of times.

The cyclical movement of the Hunt in Counting Order involves the Extreme Pells making a secondary cycle consisting of a Counting Course which (as the primary cycle of the Principle is forward) is backward.

1	2	3	4	5	6	7	8
1	3	2	5	4	7	6	8
1	3	5	2	7	4	8	6
1	5	3	7	2	8	4	6
1	5	7	3	8	2	6	4
1	7	5	8	3	6	2	4
1	7	8	5	6	3	4	2
1	8	7	6	5	4	3	2
1	8	6	7	4	5	2	3
1	6	8	4	7	2	5	3
1	6	4	8	2	7	3	5
1	4	6	2	8	3	7	5
1	4	2	6	3	8	5	7
1	2	4	3	6	5	8	7
1	2	3	4	5	6	7	8

This will be seen to be identical with the Block given on page 119.

And so we get the three cyclical movements which are characteristic of all Hunts and Extreme Pells:—

1. The primary cycle of the Principle;
2. The cycle of

The Hunt in Coursing Order;
 3. The Hunting Course in the Extreme
 Cells.

FIG XVI.

1	2	3	4	5	6	← 1 2 4 6 5 3 1
2	4	3	6	5		
2	3	4	5	6		
2	4	3	6	5	← 2 4 6 5 3	
4	2	6	3	5		
4	6	2	5	3		
4	2	6	3	5		
4	6	2	5	3	← 2 4 6 5 3	
6	4	5	2	3		
6	5	4	3	2		
6	4	5	2	3	← 2 4 6 5 3	
5	6	3	4	2		
5	3	6	2	4	← 2 4 6 5 3	
3	5	2	6	4		
3	2	5	4	6	← 2 4 6 5 3 1	
2	3	4	5	6		

Fig. XVII

The Coursing Order.

1 2 3 4 5 6 7 8	←	2 4 6 8 7 5 3 1
2 1 4 3 6 5 8 7		
1 2 4 6 3 5 7 8		
2 1 6 4 5 3 8 7	←	2 6 4 5 8 7 3 1
2 6 1 4 5 8 3 7	←	2 6 4 8 7 3 5 1
6 2 4 1 8 5 7 3		
2 6 4 8 1 5 3 7		
6 2 8 4 5 1 7 3	←	2 6 8 4 5 7 3 1
6 8 2 4 5 7 1 3	←	2 6 8 4 7 3 1 5
8 6 4 2 7 5 3 1		
6 8 4 7 2 5 1 3		
8 6 7 4 5 2 3 1	←	2 6 8 7 4 5 3 1
8 7 6 4 5 3 2 1	←	2 5 6 8 7 4 3 1
7 8 3 4 5 6 1 2	←	2 6 8 7 3 4 5 1
7 3 8 4 5 1 6 2	←	2 6 5 8 7 3 4 1
3 7 1 4 5 8 2 6	←	2 6 8 7 3 1 4 5
3 1 7 4 5 2 8 6	←	2 6 8 5 7 3 1 4
1 3 2 4 5 7 6 8	←	2 4 5 6 8 7 3 1
1 2 3 4 5 6 7 8	←	2 4 6 8 7 5 3 1

Figs. XVI (p. 133) and XVII (p. 134) are two further illustrations of Hunt's and Extreme Bell's. The first has one Hunt, the second two.

In all these illustrations the Hunt has a regular path; its steps in Coursing Order are symmetrically arranged; and the result is, in each case, a symmetrical Course, which is divided into as many Divisions or Leads as there are steps in the Hunt's cyclical path in Coursing Order.

FIG XVIII is an illustration of a Hunt which has an irregular path and a Course which is not divided into equal Leads. It is however a fine construction by Hunt and Extreme Bell. The Fable is the Hunt. First it changes positions in C.O. with 2. Then with 4. Then with 4 again. And again with 2. which brings it back to its original position. It has made a Dodging Movement in Coursing Order.

Fig XVIII.

Coursing Order.

2 3 4 5 6 7 8	←	6 8 7 5 3 1 2 4
2 4 3 6 5 8 7		
2 3 4 5 6 7 8		
2 4 3 6 5 8 7	←	6 8 7 5 3 2 1 4
4 2 6 3 8 5 7		
4 6 2 8 3 7 5		
4 6 8 2 7 3 5		
6 4 8 7 2 5 3		
6 8 4 2 7 3 5	←	
8 6 4 7 2 5 3		
6 8 7 4 5 2 3	←	6 8 7 5 3 2 4 1
8 6 7 5 4 3 2		
8 7 6 5 3 4 2		
7 8 5 6 3 2 4		
7 5 8 3 6 2 4		
5 7 3 8 2 6 4		
7 5 8 3 6 2 4	←	6 8 7 5 3 2 1 4
5 7 3 8 2 6 4		
7 5 8 3 2 6 4		
5 7 3 8 2 6 4		
5 3 7 8 2 6 4	←	6 8 7 5 3 1 2 4
3 5 7 2 8 4 6		
3 5 2 7 4 8 6		
3 2 5 4 7 6 8		
2 3 4 5 6 7 8		

The Construction which consists of Hunt and Extreme Bells is the interworking of two Cycles; and as all Cycles are essentially of the same nature, it follows that wherever you have two Cycles you have Hunt and Extreme Bells. Further since all Construction consists of creating and regaining Coursing Order, and this can only be done by different Cycles on some part of the Bells, it follows that there are Hunts and Extreme Bells in every Course or Block other than the Principles.

This is so even in the case of Group I Methods, which are usually assumed to have no Hunts. For instance the first Division of Barnsbury Major (p. 90). Here 1, 2, 7, 8 are Hunts, 3, 4, 5, 6 are Extreme Bells.

The Coursing Order is:—

3	1	2	4	6	8	7	5
3		4	8	7	6	5	1
3	8	7	4	6	1	2	5
3		4	1	2	6	5	8
3	1	2	4	6	8	7	5

* "Granderie" p. 116

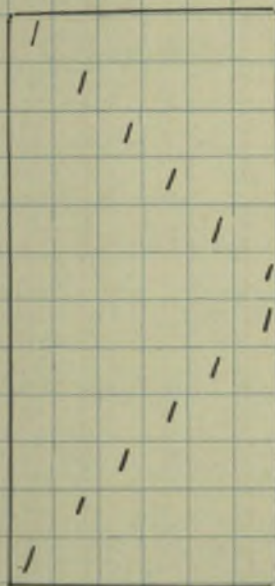
See Tintinnaloga p. 90.

As I have already pointed out the use of the Hunt was the first step in composition and it was by Hunts that the Ancients produced all their "peals", a peal being any Round Block. Snowden says that Granderie Bob was what we now call Plain Bob.* But that is not strictly true. Plain Bob is a method which has a Plain Course from which you get touches and peals by certain recognized Bobs and Singles. Granderie Bob was a particular arrangement of Hunts and had no Plain Course in the modern sense of the term.

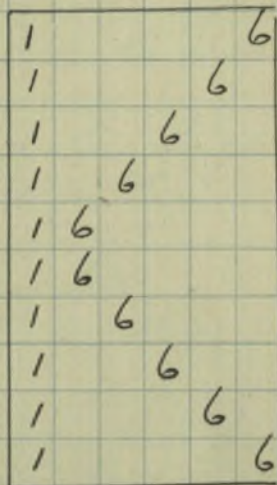
One bell (usually but not necessarily the treble) was selected as the whole Hunt. This did a regular repeated plain hunting cycle.

Another bell (the fifth, or another) was the Half Hunt. This, while sharing the primary cycle of the whole Hunt, performed a secondary cycle which caused it to fall into every different position relative to the whole Hunt.

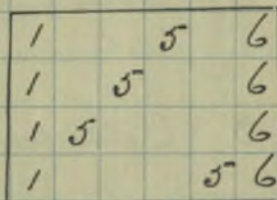
(a) The Whole Hunt



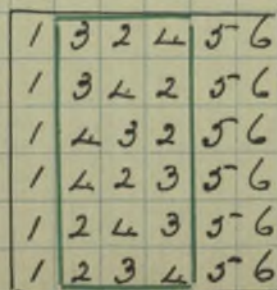
(b) The Half Hunt.



The Quarter Hunt



The Extreme Bells.



A third bell was the Quarter Hunt. This, while sharing the other two cycles, did a tertiary cycle, which caused it to fall into every different position relative to the whole Hunt and the Half Hunt.

The three remaining Bells were the Extreme Bells, and they do

a cycle among themselves consisting of a complete Hunting Course.

This gave 360 Rhos and to produce the 720 a Single was made half way and end. The effect of this Single is to make the 2nd a Hunt and to produce a Hunting Course on 3-4. The Ancients could have called the 2nd a Half-Quarter Hunt.

By the use of Hunting, in a similar way, Annable produced his 6-part feat of P³ Triple* and his well known 3-part feat of P³ Major**, and by carrying the same construction still further, I produced the full extent of P³ Measurus, 479,001,600 changes*. There is nothing really in the composition of this latter which is not a logical development of "R.R."s Grandine P³; and on the same plan a formula can be produced without much difficulty, which will give the full extent of Plain P³ on all numbers to infinity.

Garth's feat of Grandine Triples, and all the P³ and Single feats in

* Hubbard. 4th Ed. p. 54

* C.C. Collection of Feats Section II p. 174

† C.C. Collection of Feats Section II p. 251.

* *Tintinnalogia* p. 27.

that method are produced by Horatio; so too are the feats of Plain P.B., Double Norwich etc on the 5-course plan. Earlier still than any of these * examples, are the 720's of Plain Changes. These are logical developments of the "Pices". P. far from being crude and melancholy forms of ringing, they are as scientifically constructed as the best of modern feats, and they show clearer than most, the one fundamental Law of Composition, the Law of Cyclical movement. Plain Changes differ from modern feats in this thing only, - that the first are based on potential movement, and the second on the movement of a Principle.

The idea of the Ancients was not only to use Horatio in Composition, but to use them symmetrically. This naturally restricted Composition to very narrow limits. Later Composers retained the symmetrical limits so far as the Course is concerned, but to get greater variety introduced bells and singles as they thought

Thomas Melchior

See Letter by ~~Edward Crane~~ in the Norwich Gazette Dec 11 1731. "If John Garthou had been alive he would have laughed at your Ignorance for assigning Hunt's to Stedman's Triples."

* A Note on GRANDSIRE TRIPLES by W.H. Thompson
1886.

fit. By doing so they fancied they had dropped altogether the idea of Hunt's for real Composition. They did not recognize that there are, and must, be strict Laws which govern the relationships of different hobs in a real. Composition was, with them almost entirely a matter of Experiment, and it was only in recent years that Mr Thompson showed that in any 5040 of Grand sire Triples the hobs must be arranged in what he called "9 sets." * Later still it has been generally recognized that the Law of "9 sets" is a universal one for real in all methods.

But a 9 set is only another name for a Constitution consisting of Hunt and Extreme Bells.

The hob making bells are Extreme Bells; they retain the same Causing Order among themselves, and they make a complete Hunting Course.

The other bells are Hunt's; they make a complete Cyclical movement through the Causing Order of the

bob-making bells.

Examine a 9 set in any method.
Take Grandring Triples. Call a Bob
in the Plain Course when the 3rd is
Before and complete the 9 set.

Coursing Order.

3	1	5	2	7	4	6
1	3	5	7	2	6	4
3	1	7	5	6	2	4
1	3	7	6	5	4	2
3	1	6	7	4	5	2
1	3	6	4	7	2	5
3	1	4	6	2	7	5
1	3	4	2	6	5	7
3	1	2	4	5	6	7
1	3	2	5	4	7	6

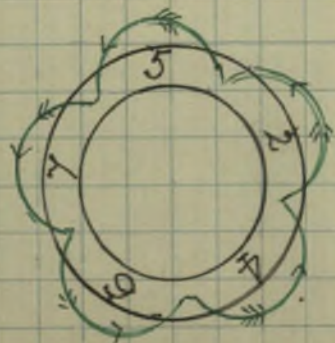
3 1 5 2 4 6 7 31.

5 2 4 6 31 7

5 2 4 31 6 7

5 2 31 4 6 7

5 31 2 4 6 7.



Compare this
with Fig X
p. 125.

Take Bob Major, Double Oxford Major
 London, Cambridge, Superlative etc.
 Call a bob at R in the Plain Course
 and complete the 9 set.

Coursing Order.

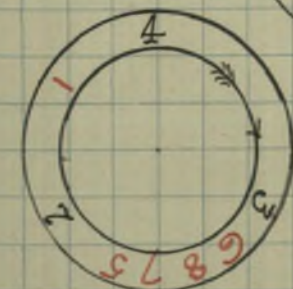
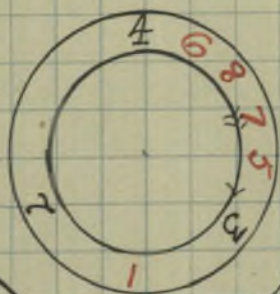
1	2	4	3	6	5	8	7
1	4	2	3	5	6	7	8
1	4	3	2	6	5	8	7
1	3	4	2	5	6	7	8
1	3	2	4	6	5	8	7
1	2	3	4	5	6	7	8

1 4 3 6 8 7 5 2.

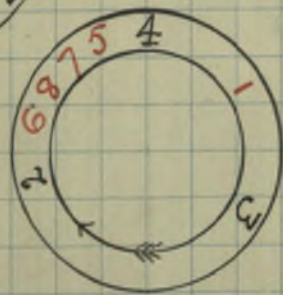
6 8 7 5 4 1 3 2.

4 6 8 7 5 3 1. 2.

C.O.
1st Course



C.O. 2nd. Course



C.O. 3rd Course

A "q set" of Oxford and Kent Major

Coursing Order.

1 8 7	6 5 4 3 2				
1 7 8	6 4 5 2 3	8176	5	3	2 4 817
1 8 7	4 6 2 5 3				
1 7 8	4 2 6 3 5	6	5	3	2 817 4
1 8 7	2 4 3 6 5				
1 7 8	2 3 4 5 6	6	5	3 817	2 4
1 8 7	3 2 5 4 6				
1 7 8	3 5 2 6 4	6	5 817	3	2 4
1 8 7	5 3 6 2 4				
1 7 8	5 6 3 4 2	6 817	5	3	2 4

A q set of Double Norwich C.P. Major

1 6 8 4 7	2 5 3				
1 8 6 7 4	2 3 5	2	5		3 4 6 1 8 7
1 6 8 4 7	3 2 5				
1 8 6 7 4	3 5 2	2		5 4 6 1 8 7	3
1 6 8 4 7	5 3 2				
1 8 6 7 4	5 2 3	2 4 6 1 8 7	5		3

Thus Mr Thompsons Law of 2 sets is really a restatement of the original truth on which the Ancients based their peals, but in different terms, and on wider lines. And it is most significant that the idea which was in the minds of the earliest of all change ringers when they invented the Pieces, should be proved to be the one important truth which lies at the base of all Composition. And surely, since it is now generally recognized in the case of peal Compositions, it should not be difficult for men to recognize that the same truth must apply to the construction of Methods.

Chapter VIII

Methods which are founded on Hunts & Working Bells.

Every Round Block except the Principles, and therefore every Method except Originals, must contain Hunts and Extreme Bells in some form or other.

But, as we saw, the main construction of Group I Methods depends on the Principle. The length of the Course is the length of the Principle; the Divisions of the Course are the Divisions of the Principle. The Hunts are secondary.

In Group II Methods the main construction is that of a Hunt (or Hunts) and Extreme Bells. The Course consists of the cyclical path of the Hunt through the Coursing Order of the Extreme Bells, and the number of Leads depends on the number of steps in that path.

In many cases there will be secondary movements consisting of Hunts and

Extreme Bells, but in all cases ^{the former} these will be the main movement.

It is a postulate in this Group of Methods that the Hunt should have a regular repeated path; and we will confine ourselves for the moment to Methods in which that path is throughout Plain Hunting or Treble Bob Hunting.

In all these Methods the bells will share equally the Primary Movement of the Principle.

To that movement is added the secondary cyclical movement of the Extreme Bells, which causes the Hunt's cyclical path in Coursing Order. This movement of the Extreme Bells, I call Constitutional Shunts.

In addition to this, there may be other cyclical movements or parts of the Extreme Bells. These do not affect the main Constitution of the Course. I call them Additional Shunts.

Fig I

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8

Let Fig I be the Plain Principle on 8 bells and in it let any one bell 1. be selected to be the Hunt of a Method; and the remainder 2, 3, 4, 5, 6, 7, 8 to be Eschime Bells.

By the nature of a Hunt, in addition to the Cyclical movement of the Principle, which is shared equally by all the bells, there will be

a cyclical path of the Hunt through the Coursing Order of the Eschime Bells, and a cyclical movement of the Eschime Bells, among themselves.

By the conditions of Group II Methods the Plain Hunting path of the Hunt may not be altered.

The Constructive Hunts which

will comply with these conditions are classified as follows, -

A. EXTREME CONSTRUCTIONAL SHUNTS

- (a) R. Extreme Constructional Shunts
(b) P. Extreme Constructional Shunts

B. COURT SHUNTS

- (a) R. Court Shunts
(b) P. Court Shunts

C. SINGLE COURT SHUNTS

- (a) R. Single Court Shunts
(b) P. Single Court Shunts

D. SLOW WORK SHUNTS.

An EXTREME CONSTRUCTIONAL SHUNT is made as follows; -

Position - With an odd number of Humps, when the middle Hump is lying its whole pull either Before or Behind.

With an even number of Humps, midway between the whole pulls before or behind of the middle two Humps.

Operation - One Backward step by.

each of the Extreme Bells.

An R. Extreme Skunt is one made on an odd number of Extreme Bells. The number of Places is the same as in the Principle and therefore the Succession of the Nature of the Rows - odd and Even is the same.

A P. Extreme Skunt is one made on an even number of Extreme Bells. The number of Places is two more than in the Principle, and therefore the Succession of the Nature of the Rows is altered.

Examples of R. Extreme Skunts. -

3 5 / 7 2 8 4 6	6 4 8 2 7 / 5 3
3 / 5 2 7 4 8 6	6 8 4 7 2 5 / 3
3 2 5 / 4 7 6 8	8 6 7 4 5 2 3
3 5 2 7 4 8 6	6 8 4 7 2 5 3
3 / 2 5 4 7 6 8	8 6 7 4 5 2 3
3 2 / 4 5 6 7 8	8 7 6 5 4 / 2 3

5	7	6	2	4	3	
5	7	2	6	3	4	
5	2	7	3	6	4	
1	2	5	3	7	4	6
2	5	7	3	6	4	
2	5	3	7	4	6	
5	2	3	1	4	7	6
5	3	2	4	1	6	7

5	8	7	8	2	6	4	
5	5	7	2	8	4	6	
3	5	2	7	4	8	6	
1	3	2	5	4	7	6	8
1	2	3	5	7	4	8	6
2	5	3	4	7	6	8	
2	5	1	4	3	6	7	8
5	2	4	1	6	3	8	7

4	3	6	2	7	5	
4	6	3	7	2	5	1
6	4	7	3	5	2	1
4	6	3	7	5	1	2
6	4	7	3	5	2	
6	7	4	3	2	5	

6	4	8	2	7	5	3	
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	5	3	2	1
8	6	7	4	3	5	1	2
8	7	6	3	4	5	2	

Examples of P Extreme Shunts.

3	5	7	2	6	4	
3	5	2	7	4	6	
1	3	2	5	4	7	6
1	3	5	2	7	4	6
3	2	5	4	7	6	
3	2	4	5	6	7	

3	5	2	7	4	8	6	
3	2	5	4	7	6	8	
1	2	3	4	5	6	7	8
2	1	3	5	4	7	6	8
2	3	1	4	5	6	7	8
3	2	4	1	6	5	8	7

One Extreme Hunt in each Lead,
made when the Hunt is Before gives -
with one Hunt - Plain Bob.
with two Hunts - Grandiose
with three Hunts - Plain Bob Short Courses.

One Extreme Hunt in each Lead,
made when the Hunt is Behind, gives -
with one Hunt - Reverse Bob.
with two Hunts - Reverse Grandiose
with three Hunts - Reverse Bob, Short
Courses.

Two Extreme Hunts in each Lead
one made when the Hunt is Before
and the other when the Hunt is
Behind give -
with one Hunt - Double Bob.
with two Hunts - Double Grandiose.
with three Hunts - a variation of
Double Bob.

If two Extreme Hunts are made in
each Lead, the Hunt will perform,
within the Course, two complete Cycles
in Coursing Order. When as many
Hunts have been made as there are

2	3	4	5	6	
2	4	3	6	5	
2	4	6	3	5	
4	2	6	5	3	
4	6	2	5	3	
6	4	5	2	3	
4	6	2	5	3	
6	4	5	2	3	
6	5	4	1	2	3
5	6	1	4	3	2
5	6	3	4	2	
5	3	6	2	4	
5	6	3	4	2	
5	3	6	2	4	
5	3	1	2	6	4
3	5	2	1	4	6
3	2	5	4	1	6
2	3	4	5	6	1



3	5	2	6	4	
3	2	5	4	6	
3	2	4	5	6	
2	3	4	6	5	
2	4	3	6	5	
4	2	6	3	5	
2	4	3	6	5	
4	2	6	3	5	
4	6	2	1	3	5
6	4	5	2	3	
6	5	4	3	2	
6	4	5	2	3	
6	1	5	4	3	2
6	5	1	3	4	2
5	6	3	1	2	4
5	3	6	2	1	4
3	5	2	6	4	1



3	2	5	4	6	
2	3	4	5	1	6
2	4	3	1	5	6
4	2	3	6	5	
4	2	6	3	5	
4	6	2	5	3	
4	6	2	5	3	
4	6	1	5	2	3
6	4	5	1	3	2
6	5	4	3	1	2
5	6	3	4	2	1
6	5	4	3	2	
5	6	3	4	2	
5	3	6	1	4	2
3	5	1	6	2	4
3	5	2	6	4	
3	2	5	4	6	



5	3	6	2	4	
3	5	2	6	1	4
3	2	5	1	6	4
2	3	1	5	4	6
2	3	4	5	6	
2	4	3	6	5	
2	3	4	5	6	



A Plain Course of
DOUBLE BOB MINOR

Showing the Constructional
Shunts and the
Coursing Order.

Extreme Bells the first cycle will be completed, The bells will then be again in the Causing Order of the Principle, and if no more Shenti are made the bells will return to the Row from which they originally started as soon as the cycle of the Principle is completed, that is at the Lead End. But since, before that, another Shenti is made, the bells will not come home until the completion of both cycles coincides. See Diagram on page 154.

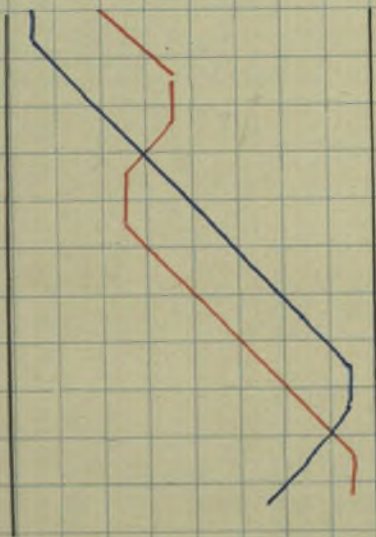
A Court Shenti is made in any change when the Hunt is neither Before nor Behind. At such a point the Extreme Bells are not all together as they are when an Extreme Shenti is made. Consequently, they cannot all at the same time make the one backward step. The Court Shenti is therefore made in two parts, one on one side of the Hunt's path and one on the other.

When the Hunt is hunting up, all the Extreme Bells above it, make in

* Strictly speaking this is not exactly true. In the course of the Shunt each of the Extreme Bells makes one backward step relative to the Hunt. In the case of the dodging bells this backward step is made at the dodge. In the case of the place-making bell this backward step is made in two parts viz one half in the process of making each place. It will be observed that when a bell dodges the dodging bell is, as it were, delayed two rows in its hunting path, while to delay the place making bell two rows, would put it in the place of the Hunt, as might be anticipated from the consideration that the Court Shunt has the effect of interchanging in position the Hunt and the bell before it in Coursing Order — E. S. POWELL.

any one Change, one backward step. Two Changes later all the Extreme Bells below the Hunt make one backward step *

	1	2	3	4	5	6	7	8	
	2	1	4	3	6	5	8	7	A1
	2	4	1	3	5	6	7	8	
A2	4	2	3	1	6	5	8	7	
	2	4	3	6	1	8	5	7	← C.O. = 51324687.
	4	2	6	3	8	1	7	5	



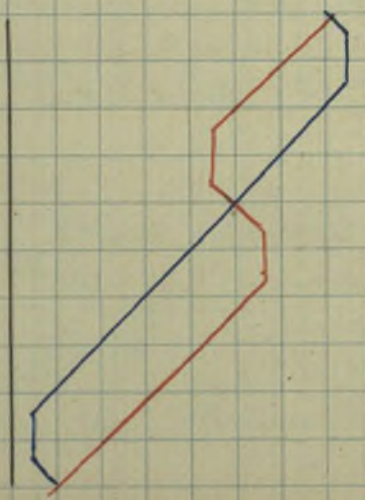
The result is that the Extreme Bells retain the same Coursing Order among themselves, but the bell that previously had coursed immediately in front of the Hunt, now courses immediately behind it. The

Hunt and this bell have changed positions in Coursing Order, and the Hunt has made the first step

in its cyclical path.

When the Hunti is hunting down all the Extreme Bells below it, make, in any one Change, one backward step. Two Changes later all the Extreme Bells above the Hunti make one backward step.

8 7 6 5 4 3 2	← C.O. = 53124687.
<u>7 8 5 6 3 4</u> 1 2	
8 7 6 5 3 1 4 2	
7 8 5 6 1 3 2 4	
7 5 8 6 3 4 2	
5 7 8 3 6 2 4	← C.O. = 51324687.
5 7 3 8 2 6 4	



The result is exactly the same as in the last case (p. 156). The Hunti has changed positions in Coursing Order with the shell next in front of it.

An R Court Shunt is a Court Shunt in which the number of Extreme Bells in both the part above, and the part below the Shunt, is ~~even~~ odd, as in the Court Shunt examples.

The number of Places made is the same as in the Principle, and therefore the succession of the Nature of the Rows is the same as in the Principle.

A I Court Shunt is a Court Shunt in which the number of Extreme Bells in both the part above and the part below the Shunt is even.

In each part of the Shunt two more Places are made than in the Principle. Therefore the first part will alter the succession of the Nature of the Rows, and the second part will regain it.

When the total number of Extreme Bells is even, one part of the Shunt will be R, and the other part I. The I part will alter the succession of the Nature of the Rows.

Examples of P Cant Numbers :-

1	2	3	4	5	6	7	8	← C.O. = 53124687
2	4	3	6	5	8	7		
2	4	1	6	3	8	5	7	
4	2	6	1	3	5	8	7	
4	6	2	3	1	8	5	7	
4	2	6	3	8	1	7	5	← C.O. = 51324687
4	6	2	8	3	7	1	5	

8	7	6	5	4	3	2	1	← C.O. = 53124687
7	8	5	6	3	4	1	2	
7	5	8	3	6	1	4	2	
7	8	5	3	1	6	2	4	
7	5	8	1	3	2	6	4	
5	7	1	8	3	6	2	4	← C.O. = 51324687
5	7	3	8	2	6	4		

1	2	3	4	5	6	7	← C.O. = 5312467
2	4	3	6	5	7		
2	4	1	3	5	6	7	
4	2	3	1	6	5	7	
2	4	3	6	1	7	5	← C.O. = 5132467.
4	2	6	3	7	1	5	

A Single R. Court Shunt, is a Court Shunt in which the first part is made, when the Hunt is hunting up, on all the Extreme Bells above the Hunt, in any Change where the number of those bells is odd. The second part is made above the Hunt when the Hunt is hunting down.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	6	5	8	7
4	3	2	6	1	8	5	7
3	4	6	2	8	1	7	5
3	6	4	8	2	7	1	5
6	3	8	4	7	2	5	1
6	8	3	7	4	5	2	1
8	6	7	3	5	4	1	2
8	7	6	5	3	1	4	2
7	8	5	6	3	2	4	1
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	7	3	8	2	6	4	1
5	3	7	2	8	4	6	1
1	3	5	2	7	4	8	6

← C.O. = 53124687

A1

A2

← C.O. = 51324687

A Single P Count Shunt is the same as a Single R Count Shunt, except that the number of Extreme Bells in both parts is even.

1	2	3	4	5	6	7	8	
2	1	4	3	6	5	8	7	← c.o. = 53124687
2	4	1	6	3	8	5	7	A1
4	2	6	1	3	5	8	7	
4	6	2	3	1	8	5	7	
6	4	3	2	8	1	7	5	
6	3	4	8	2	7	1	5	
3	6	8	4	7	2	5	1	
3	8	6	7	4	5	2	1	
8	3	7	6	5	4	2	1	
8	7	3	5	6	4	2	1	
7	8	5	3	6	2	4	1	
7	5	8	3	2	6	4	1	A2.
5	7	1	8	3	6	2	4	← c.o. = 51324687.
5	1	7	3	8	2	6	4	
5	3	7	2	8	4	6	1	
1	3	5	2	7	4	8	6	

The Change, (with the Hunt ^{down} hunting up), in which the second part of a Single Count Shunt is made, corresponds with the Change, (with the Hunt ^{up} hunting up),

in which the second part of a Cant
Shunt is made. The Rows are the same,
but with the bells in reverse order.

The effect on the succession of the names
of the Rows is the same in the single
Cant Shunt as in the Cant Shunt.

1 2 3 4 5 6 7 8	← C.O. = 5 3 1 2 4 6 8 7
2 1 4 3 6 5 8 7	
2 4 1 3 5 6 7 8	A1.
4 2 3 1 6 5 8 7	
4 3 2 6 1 8 5 7	
3 4 6 2 8 1 7 5	
3 6 4 8 2 7 1 5	
6 3 8 4 7 2 5 1	
6 8 3 7 4 5 2 1	
8 6 7 3 5 4 1 2	
8 7 6 5 3 1 4 2	
7 8 5 6 1 3 2 4	
7 5 8 1 6 2 3 4	A2.
5 7 1 8 2 6 3 4	
5 1 7 2 8 3 6 4	← C.O. = 5 1 2 3 4 6 8 7
5 2 7 3 8 4 6	
2 5 3 7 4 8 6	

Where the total number
of Extreme Bells
is even, half of the
Shunt will be R.
and part P.

A Reverse Single Count Shunt is the same as a Single Count Shunt, except that both parts are made below the Hermis path.

8 7 6 5 4 3 2	← C.O. = 5 3 1 2 4 6 8 7
7 8 5 6 3 4 1 2	
8 7 6 5 3 4 2	
7 8 5 6 1 3 2 4	
7 5 8 6 2 3 4	
5 7 1 8 2 6 4 3	
7 5 2 8 4 6 3	
7 2 5 4 8 3 6	
1 2 7 4 5 3 8 6	
2 1 4 7 3 5 6 8	
2 4 1 3 7 6 5 8	
4 2 3 1 6 5 8 7	
2 4 3 6 1 8 5 7	← C.O. = 5 1 3 2 4 6 8 7
4 2 6 3 8 1 7 5	
4 6 2 8 3 7 1 5	

(S.S.P) 5 7

Reverse Single Count Shunts divide into \overline{R} and \overline{P} , and the effect on the succession of the Nature of the Rows is the same as in other Count Shunts.

Although the Extreme Shanti and the different varieties of Court Shanti, differ in the positions they are made, and to some extent in the way they are made, the effect is the same in each case - the Shanti has changed position in Courting Order with the bell next before it, and made one step in its cyclical path.

In any Method on the Plain Principle of x Bells, there will be x Shantis and $x-y$ Extreme Bells.

The number of positions ^{in each lead} in which Extreme and Court Shanti can be made is as follows. -

I. With an Odd Number of Extreme Bells.

Extreme Shunts.	Before.	1.
	Behind.	1.
R. Court Shunts.		
	Hunt hunting Up.	$\frac{x-y-3}{2}$
	" " Down	$\frac{x-y-3}{2}$
P. Court Shunts.		
	Hunt hunting Up.	$\frac{x-y-1}{2}$
	" " Down	$\frac{x-y-1}{2}$
Single R. Court Shunts.		$\frac{x-y-3}{2}$
Single P. Court Shunts.		$\frac{x-y-1}{2}$
Reverse R. Court Shunts.		$\frac{x-y-3}{2}$
Reverse P. Court Shunts.		$\frac{x-y-1}{2}$

II With an Even No. of Extreme Bells.

Extreme Shunts		2.
Court Shunts.	Hunt up.	$x-y-2$.
	do. " down	$x-y-2$.
Single Court Shunts.		$x-y-2$.
Reverse do do		$x-y-2$.

PLAIN. PRINCIPLE. 8 Bells. 1 Hunt. 7 Extreme Bells.

1. Extreme Shunt. Before

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	3	5	2	7	4	8	6

2. Extreme Shunt Behind

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	3	5	2	7	4	8	6

3. R. Court. Shunt. Hunt up.

1	2	3	4	5	6	7	8	
2	1	4	3	6	5	8	7	
2	4	1	3	5	6	7	8	
4	2	3	1	6	5	8	7	
2	4	3	6	1	8	5	7	
4	2	6	3	8	1	7	5	
4	6	2	8	3	7	1	5	
6	4	8	2	7	3	5	1	
6	8	4	7	2	5	3	1	
8	6	7	4	5	2	3	1	
8	7	6	5	4	3	2	1	
8	6	7	4	5	2	1	3	
8	7	6	5	4	1	2	3	
7	8	5	6	1	4	3	2	
7	5	8	1	6	3	4	2	
5	7	1	8	3	6	2	4	
5	7	1	8	3	8	2	6	4
5	7	1	8	3	8	2	6	4
5	3	7	2	8	4	6		
1	3	5	2	7	4	8	6	

4. R. Court. Shunt. Hunt up.

1	2	3	4	5	6	7	8	
2	1	4	3	6	5	8	7	
2	4	1	6	3	8	5	7	
4	2	6	1	8	3	7	5	
4	6	2	8	1	3	5	7	
6	4	8	2	3	1	7	5	
4	6	2	8	3	7	1	5	
6	4	8	2	7	3	5	1	
6	8	4	7	2	5	3	1	
8	6	7	4	5	2	1	3	
8	7	6	5	4	1	2	3	
7	8	5	6	3	4	1	2	
7	5	8	3	6	1	4	2	
5	7	1	8	3	6	2	4	
5	7	1	8	3	8	2	6	4
5	3	7	2	8	4	6		
1	3	5	2	7	4	8	6	

5. R. Court Shunt Hunt Down.

1	2	3	4	5	6	7	8	
2	1	4	3	6	5	8	7	
2	4	1	6	3	8	5	7	
4	2	6	1	8	3	7	5	
4	6	2	8	1	7	3	5	
6	4	8	2	7	1	5	3	
6	8	4	7	2	5	1	3	
8	6	7	4	5	2	3	1	
8	7	6	5	4	3	2	1	
7	8	5	6	3	4	1	2	
7	5	8	3	6	1	4	2	
7	5	8	1	6	3	4	2	
5	7	1	8	3	6	2	4	
5	7	1	8	3	8	2	6	4
5	3	7	2	8	4	6		
1	3	5	2	7	4	8	6	

6. R. Court Shunt Hunt Down.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	7	3	8	2	6	4	
5	7	3	8	2	6	4	
5	3	7	2	8	4	6	
1	3	5	2	7	4	8	6

7. P Court Shunt.
Hunt Up.

1	2	3	4	5	6	7	8
2	1	3	4	5	6	7	8
2	3	1	4	5	6	7	8
2	3	4	1	6	5	8	7
2	4	3	6	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	8	3	7	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	5	3	1
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

8. P Court Shunt
Hunt Up.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	3	5	8	7
4	6	2	3	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	8	3	7	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	5	3	1
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

9. P Court Shunt
Hunt Up.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	3	5
6	8	4	7	2	3	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	5	3	1
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

10. P Court Shunt
Hunt Down

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
8	8	5	6	4	3	5	3
8	7	6	5	4	1	3	2
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

11. P Court Shunt
Hunt Down

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
7	8	5	3	1	6	2	4
7	5	8	1	3	2	6	4
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

12. P Court Shunt
Hunt Down

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
7	8	5	3	1	6	2	4
7	5	8	1	3	2	6	4
5	7	3	8	6	2	4	1
5	3	7	8	2	6	4	1
5	3	7	2	8	4	6	1
1	3	5	2	7	4	8	6

13. R. Single Court Shunt.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	6	5	8	7
4	3	2	6	1	8	5	7
3	4	6	2	8	1	7	5
3	6	4	8	2	7	1	5
6	3	8	4	7	2	5	1
6	8	3	7	4	5	2	1
8	6	7	3	5	4	1	2
8	7	6	5	3	1	4	2
7	8	5	6	1	3	2	4
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
5	3	7	2	8	4	6	1
3	5	2	7	4	8	6	1

14. R. Single Court Shunt.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	3	5	7
6	4	8	2	3	1	7	5
6	8	4	3	2	7	1	5
8	6	3	4	7	2	5	1
8	3	6	7	4	5	2	1
3	8	7	6	5	4	1	2
3	7	8	5	6	1	4	2
7	3	5	8	6	2	4	1
7	5	3	1	8	2	6	4
5	7	1	3	2	8	4	6
5	1	7	3	8	2	6	4
5	3	7	2	8	4	6	1
3	5	2	7	4	8	6	1

15. P. Single Court Shunt.

1	2	3	4	5	6	7	8
2	1	3	5	4	7	6	8
2	3	1	4	5	6	7	8
3	2	4	1	6	5	8	7
3	4	2	6	1	8	5	7
4	3	6	2	8	1	7	5
4	6	3	8	2	7	1	5
6	4	8	3	7	2	5	1
6	8	4	7	3	5	2	1
8	6	7	4	5	3	1	2
8	7	6	5	4	1	3	2
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
5	3	7	2	8	4	6	1
3	5	2	7	4	8	6	1

16. P. Single Court Shunt

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	3	5	8	7
4	6	2	3	1	8	5	7
6	4	3	2	8	1	7	5
6	3	4	8	2	7	1	5
3	6	8	4	7	2	5	1
3	8	6	7	4	5	2	1
8	3	7	6	5	4	1	2
8	7	3	5	6	1	4	2
7	8	5	3	1	6	2	4
7	5	8	1	3	2	6	4
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
5	3	7	2	8	4	6	1
3	5	2	7	4	8	6	1

17. P. Single Court Shunt.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	3	5
6	8	4	7	2	3	1	5
8	6	7	4	3	2	5	1
8	7	6	3	4	5	2	1
7	8	3	6	5	4	1	2
7	3	8	5	6	1	4	2
3	7	5	8	1	6	2	4
3	5	7	1	8	2	6	4
5	3	1	7	2	8	4	6
5	1	3	2	7	4	8	6
5	3	7	2	8	4	6	1
3	5	2	7	4	8	6	1

18. Reverse R. Single
Court Shunt

19. Reverse R. Single
Court Shunt.

20. Reverse P. Single
Court Shunt.

x	2	3	4	5	6	7	8
2	x	4	3	6	5	8	7
2	4	x	6	3	8	5	7
4	2	6	x	8	3	7	5
4	6	2	8	x	7	3	5
6	4	8	2	7	x	5	3
6	8	4	7	2	5	x	3
8	6	7	4	5	2	3	x
8	7	6	5	4	3	2	x
A1	7	8	5	6	3	4	2
8	7	6	5	3	1	4	2
7	8	5	6	1	3	2	4
7	5	8	1	6	2	3	4
5	7	1	8	2	6	4	3
5	1	7	2	8	4	6	3
1	5	2	7	4	8	3	6

x	2	3	4	5	6	7	8
2	x	4	3	6	5	8	7
2	4	x	6	3	8	5	7
4	2	6	x	8	3	7	5
4	6	2	8	x	7	3	5
6	4	8	2	7	x	5	3
6	8	4	7	2	5	x	3
8	6	7	4	5	2	3	x
8	7	6	5	4	3	2	x
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
B1	5	7	3	8	1	6	2
7	5	3	1	8	2	6	4
5	7	1	3	2	8	4	6
5	1	7	2	3	4	8	6
1	5	2	7	4	3	6	8

x	2	3	4	5	6	7	8
2	x	4	3	6	5	8	7
2	4	x	6	3	8	5	7
4	2	6	x	8	3	7	5
4	6	2	8	x	7	3	5
6	4	8	2	7	x	5	3
6	8	4	7	2	5	x	3
8	6	7	4	5	2	3	x
8	7	6	5	4	3	2	x
8	6	7	4	5	3	1	2
8	7	6	5	4	1	3	2
7	8	5	6	1	4	2	3
7	5	8	1	6	2	4	3
5	7	1	8	2	6	3	4
5	1	7	2	8	3	6	4
1	5	2	7	3	8	4	6

x	2	5	4	7	3	8	6
2	x	4	5	3	7	6	8
2	4	x	3	5	6	7	8
A2	4	2	3	x	6	5	8
2	4	3	6	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	8	3	7	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	5	3	1
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

x	2	5	4	7	6	3	8
2	x	4	5	6	7	8	3
2	4	x	6	5	8	7	3
4	2	6	x	8	5	3	7
4	6	2	8	x	3	5	7
6	4	8	2	3	x	7	5
6	8	4	7	2	5	3	x
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

x	2	5	3	7	4	8	6
2	x	3	5	4	7	6	8
2	3	x	4	5	6	7	8
2	3	4	x	6	5	8	7
2	4	3	6	x	8	5	7
4	2	6	3	8	x	7	5
4	6	2	8	3	7	x	5
6	4	8	2	7	3	5	x
6	8	4	7	2	5	3	x
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6

21. Reverse P. Single
Court Shunt

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
7	8	5	3	1	6	2	4
7	5	8	1	3	2	6	4
5	7	1	8	2	3	4	6
5	1	7	2	8	4	3	6
5	1	5	2	7	4	8	6

B1.

22. Reverse P. Single
Court Shunt.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	8	2	6	4	1
5	3	1	7	2	8	4	6
5	1	3	2	7	4	8	6
1	5	2	3	4	7	6	8

C1.

1	2	5	4	7	6	8	3
2	1	4	5	6	7	3	8
2	4	1	6	5	3	7	8
4	2	6	1	3	5	8	7
4	6	2	3	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	8	3	7	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	5	3	1
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
5	1	5	3	7	2	8	4
1	3	5	2	7	4	8	6

B2.

1	2	5	4	3	6	7	8
2	1	4	5	6	3	8	7
2	4	1	6	5	8	3	7
4	2	6	1	8	5	7	3
4	6	2	8	1	7	5	3
6	4	8	2	7	1	3	5
6	8	4	7	2	3	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	5	3	1
8	6	7	4	5	2	1	3
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
5	1	5	3	7	2	8	4
1	3	5	2	7	4	8	6

C2.

The Slow Work Shunts. A Hunt
 can change positions in Coursing Order
 only with one of the two bells that
 is Coursing immediately next to it on
 either side. The Extreme Shunts
 and the different varieties of Court
 Shunts include all the positions in
 the Plain Principle in which the Hunt
 can change positions with the bell
 Coursing in front of it. If the Hunt
 is to change positions with the bell
 Coursing behind it, its movement
 must be retarded to allow that
 bell to pass it

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	1	3	5
8	6	7	4	1	2	5	3
6	8	4	7	1	5	2	3
8	6	7	4	5	1	3	2
8	7	6	5	4	3	1	2

← C.O. = 53124687.

← C.O. = 53214687.

This however is not allowed by the conditions of the Group of Methods we are considering, in which the Hunt must have an uninterrupted plain hunting path.

Therefore, if the Hunt is engaged in no other movement than that of the Primary Principle, (and of course its Cyclical path in Courring order), the Extreme Hunts and the Court Hunts are the only possible Constructional Hunts.

But it is possible for the Hunt to be engaged as an Extreme Bell in secondary movements within the Lead, and yet retain its plain hunting path; and by means of those secondary movements to change positions with one or more bells Courring behind it. As a Hunt it can change positions with only one Extreme Bell at a time. As an Extreme Bell in a secondary movement, it must change positions with all the Hunts of that movement, whether they be one or more than one.

Fig M.

2	8	7	6	5	4	3	1
2	7	8	5	6	3	4	1
2	7	5	8	3	6	1	4
2	5	7	3	8	1	6	4
2	5	3	7	1	8	4	6
2	3	5	1	7	4	8	6
2	3	1	5	4	7	6	8
2	1	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	4	6	1	8	3	7	5
2	6	4	8	1	7	3	5
2	6	8	4	7	1	5	3
2	8	6	7	4	5	1	3
2	8	7	6	5	4	3	1

Fig. M. is a Course in which 2 is the Hunt, and 1345678 are Extreme Bells (see page 119). The Extreme Bells keep the same Coursing Order among themselves, but the Hunt changes positions with each in due order.

If 2 omitted to change positions in Coursing Order with any one of the Extreme Bells, the

result would be that at the end of the Course those two bells would be transposed in Coursing Order; and also that the Extreme Bell would plain Hunt from back to front.

If the Course is continuously repeated and this particular Extreme Bell omits to change positions in Coursing Order with the Hunt of each of the repetitions, it will have a continuous

repeated plain hunting path and become
 the Hunt of a great Course. Each
 step of its cyclical path in Counting
 Order will consist of the omission
 to make, as an Extreme Bell, the step
 in the smaller Course.

1	<u>2</u>	3	4	5	6	7	8	← C.O. = 53124687.
2	1	4	3	6	5	8	7	
2	4	1	6	3	8	5	7	
2	4	6	1	8	3	7	5	
2	6	4	8	1	7	3	5	
2	6	8	4	7	1	5	3	
2	8	6	7	4	5	1	3	
2	8	7	6	5	4	3	1	
2	7	8	5	6	3	4	1	
2	7	5	8	3	6	4	1	
2	5	7	3	8	6	4	1	
2	5	3	7	8	4	6	1	
2	3	5	7	4	8	6	1	
2	3	7	5	4	7	6	1	
2	3	4	5	6	7	8	1	
1	2	4	3	6	5	8	7	← C.O. = 53 <u>2</u> 14687.
4	<u>2</u>	6	3	8	5	7		
4	1	6	2	8	3	7	5	
4	6	1	8	2	7	3	5	

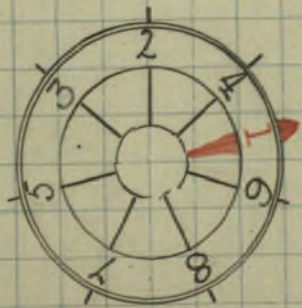
ONE-BELL SLOW WORK SHUNT PLAIN PRINCIPLE.

COURSING ORDER
SMALL CYCLE MAIN CYCLE

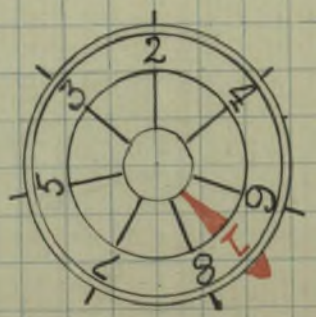
1 2 3 4 5 6 7 8	←	12468753
2 1 4 3 6 5 8 7	←	24687531
2 4 1 6 3 8 5 7	←	42687531
2 4 6 1 8 3 7 5	←	46287531
2 6 4 8 1 7 3 5	←	46287531
2 6 8 4 7 1 5 3	←	46287531
2 8 6 7 4 5 1 3	←	46827531
2 8 7 6 5 4 3 1	←	46827531
2 7 8 5 6 3 4 1	←	46872531
2 7 5 8 3 6 1 4	←	46872531
2 5 7 3 8 1 6 4	←	46875231
2 5 3 7 1 8 4 6	←	46875231
2 3 5 1 7 4 8 6	←	46875321
2 3 1 5 4 7 6 8	←	46875321
2 1 3 4 5 6 7 8	←	21468753
1 2 4 3 6 5 8 7		



1 4 2 6 3 8 5 7	←	21468753
4 1 6 2 8 3 7 5	←	46875321
4 6 1 8 2 7 3 5	←	64875321
4 6 8 1 7 2 5 3	←	68475321
4 8 6 7 1 5 2 3	←	68475321
4 8 7 6 5 1 3 2	←	68745321
4 7 8 5 6 3 1 2	←	68745321
4 7 5 8 3 6 2 1	←	68754321
4 5 7 3 8 2 6 1	←	68754321
4 5 3 7 2 8 1 6	←	68754321
4 3 5 2 7 1 8 6	←	68753421
4 3 2 5 1 7 6 8	←	68753421
4 2 3 1 5 6 7 8	←	68753241
4 2 1 3 6 5 8 7	←	68753241
4 1 2 6 3 8 5 7	←	24168753
1 4 6 2 8 3 7 5		



6	4	8	2	7	3	5	←	24168753	
6	8	4	7	2	5	3	←	68753241	
6	8	7	4	5	2	3			
6	8	7	1	5	4	3	←	86753241	
6	7	8	5	1	3	4	2		
6	7	5	8	3	1	2	4	←	87653241
6	5	7	3	8	2	1	4		
6	5	3	7	2	8	4	1	←	87563241
6	3	5	2	7	4	8			
6	3	2	5	4	7	1	8	←	87536241
6	2	3	4	5	1	7	8		
6	2	4	3	1	5	8	7	←	87532641
6	4	2	3	8	5	7			
6	4	1	2	8	3	7	5	←	87532461
6	1	4	8	2	7	3	5	←	24618753
6	8	4	7	2	5	3			



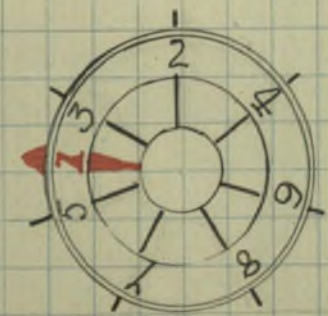
8	6	7	4	5	2	3	←	24618753	
8	7	6	5	4	3	2	←	87532461	
8	7	1	5	6	3	4	2		
8	7	5	1	3	6	2	4	←	78532461
8	5	7	3	1	2	6	4		
8	5	3	7	2	1	4	6	←	75832461
8	3	5	2	7	4	1	6		
8	3	2	5	4	7	6	1	←	75382461
8	2	3	4	5	6	7	1		
8	2	4	3	6	5	1	7	←	75328461
8	4	2	6	3	1	5	7		
8	4	6	2	1	3	7	5	←	75324861
8	6	4	2	7	3	5			
8	6	4	7	2	5	3	←	75324681	
8	6	7	4	5	2	3	←	24681753	
8	7	6	5	4	3	2			



7	8	5	6	3	4	2	←	24681753	
7	5	8	3	6	2	4	←	75324681	
7	5	3	8	2	6	4			
7	5	3	1	2	8	4	6	←	57324681
7	3	5	2	1	4	8	6		
7	3	2	5	4	1	6	8	←	53724681
7	2	3	4	5	6	1	8		
7	2	4	3	6	5	8	1	←	53274681
7	4	2	6	3	8	5			
7	4	6	2	8	3	5	1	←	53247681
7	6	4	8	2	3	5			
7	6	8	4	2	5	3	1	←	53246781
7	8	6	4	5	2	3			
7	8	1	6	5	4	3	2	←	53246871
7	1	8	5	6	3	4	2	←	24687153
7	5	8	3	6	2	4			



5	7	3	8	2	6	4	←	24687153.	
5	3	7	2	8	4	6	←	53246871.	
5	3	1	2	7	4	8	6		
5	3	2	1	4	7	6	8	←	35246871
5	2	3	4	1	6	7	8		
5	2	4	3	6	1	8	7	←	32546871
5	4	2	6	3	8	1	7		
5	4	6	2	8	3	7	1	←	32456871
5	6	4	8	2	7	3			
5	6	8	4	7	2	1	3	←	32465871
5	8	6	7	4	2	3			
5	8	7	6	1	4	3	2	←	32468571
5	7	8	6	3	4	2			
5	7	1	8	3	6	2	4	←	32468751
5	1	7	3	8	2	6	4	←	24687513.
5	3	7	2	8	4	6			



TWO BELL SLOW WORK SHUNT

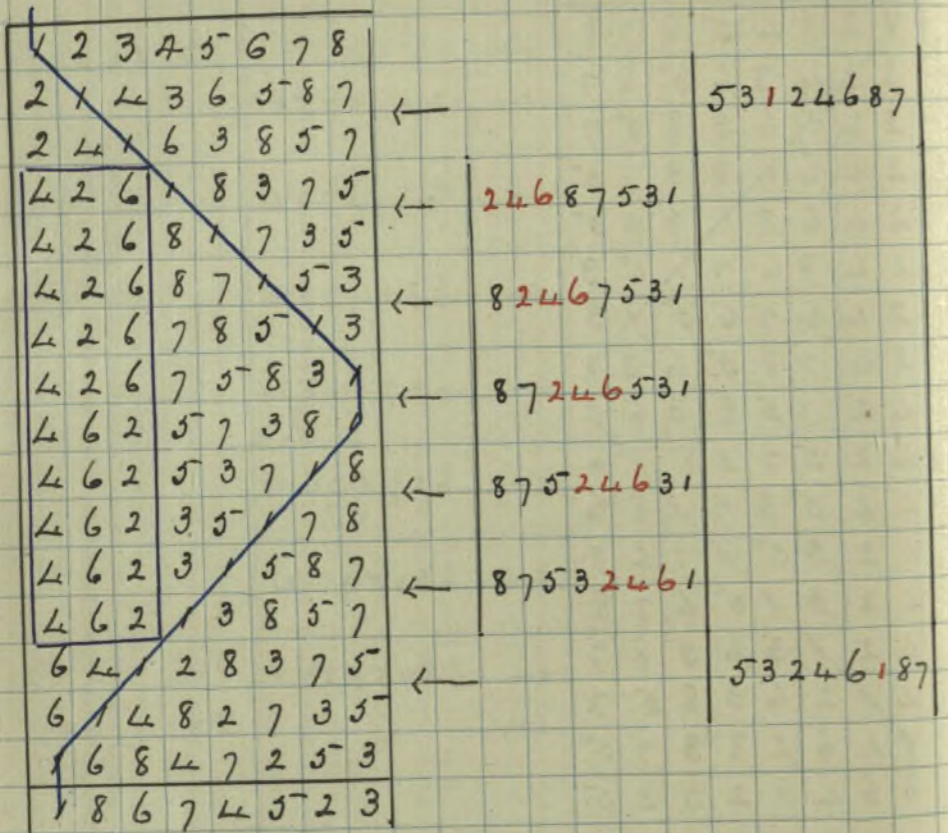
1	3	5	2	7	4	8	6	←		24687513
3	1	2	5	4	7	6	8	←	3	2468751
3	2	1	4	5	6	7	8	←		
3	2	4	1	6	5	8	7	←	2	3468751
3	4	2	6	1	8	5	7	←		
3	4	6	2	8	1	7	5	←	2	4368751
3	6	4	8	2	7	1	5	←		
3	6	8	4	7	2	5	1	←	2	4638751
3	8	6	7	4	5	2	1	←		
3	8	7	6	5	4	1	2	←	2	4683751
3	7	8	5	6	1	4	2	←		
3	7	5	8	1	6	2	4	←	2	4687351
3	5	7	1	8	2	6	4	←		
3	5	1	7	2	8	4	6	←	2	4687531
3	1	5	2	7	4	8	6	←		24687531
1	2	3	4	5	6	7	8			



1	2	3	4	5	6	7	8	←		53124687
2	1	4	3	6	5	8	7	←	24	687531
2	4	1	6	3	8	5	7	←		
2	4	6	1	8	3	7	5	←	6	2487531
2	4	6	8	1	7	3	5	←		
2	4	8	6	7	1	5	3	←	6	8247531
2	4	8	7	6	5	1	3	←		
2	4	7	8	5	6	3	1	←	6	8724531
4	2	7	5	8	3	6	1	←		
4	2	5	7	3	8	1	6	←	6	8752431
4	2	5	3	7	8	6	1	←		
4	2	3	5	1	7	6	8	←	6	8753241
4	2	3	1	5	6	7	8	←		
4	2	1	3	6	5	8	7	←	6	8753241
4	1	2	6	3	8	5	7	←		53241687
4	6	2	8	3	7	5	1	←		
1	6	4	8	2	7	3	5			

COURSING ORDER.	1st. Lead End.	
		1 2 4 6 8 7 5 3
		2 4 1 6 8 7 5 3
2nd.	do	2 4 6 8 1 7 5 3
3rd.	do	2 4 6 8 7 5 1 3
4th.	do	2 1 4 6 8 7 5 3
5th.	do	2 4 6 1 8 7 5 3
6th.	do	2 4 6 8 7 1 5 3
7th.	do	1 2 4 6 8 7 5 3

THREE BELL SLOW WORK SHUNT

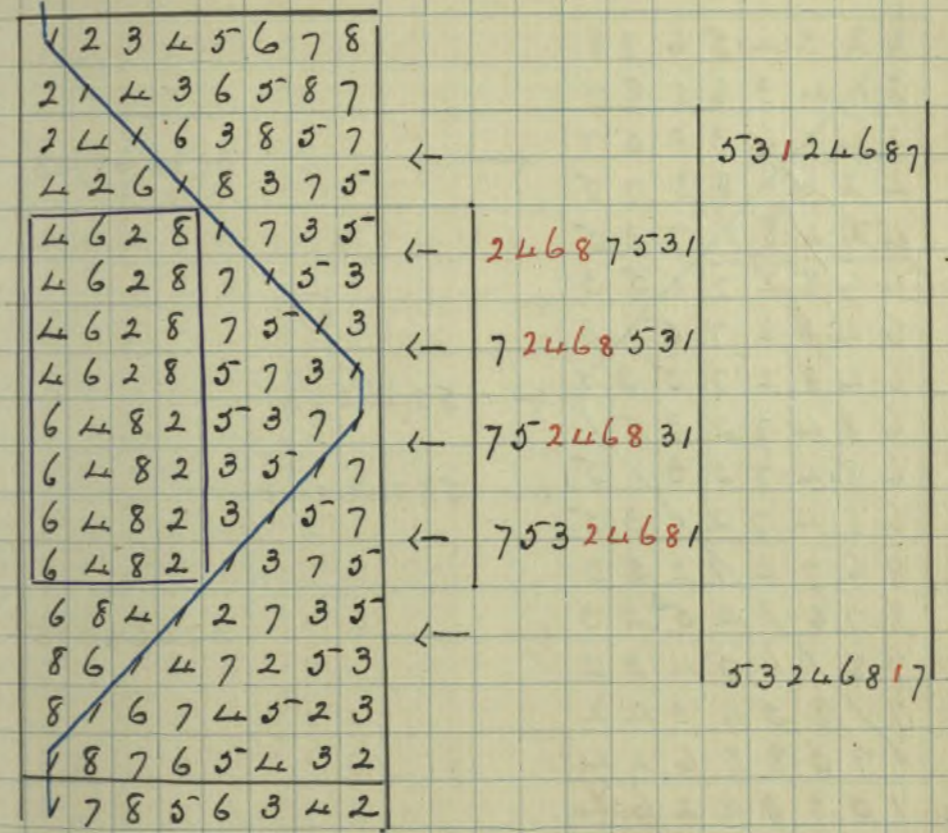


COURSING ORDER.

1st. Lead. End.
2nd do
3rd do
4th do
5th do
6th do
7th do

1 2 4 6 8 7 5 3
2 4 6 1 8 7 5 3
2 4 6 8 7 5 1 3
2 4 1 6 8 7 5 3
2 4 6 8 7 1 5 3
2 1 4 6 8 7 5 3
2 4 6 8 1 7 5 3
1 2 4 6 8 7 5 3

FOUR BELL SLOW WORK SHUNT

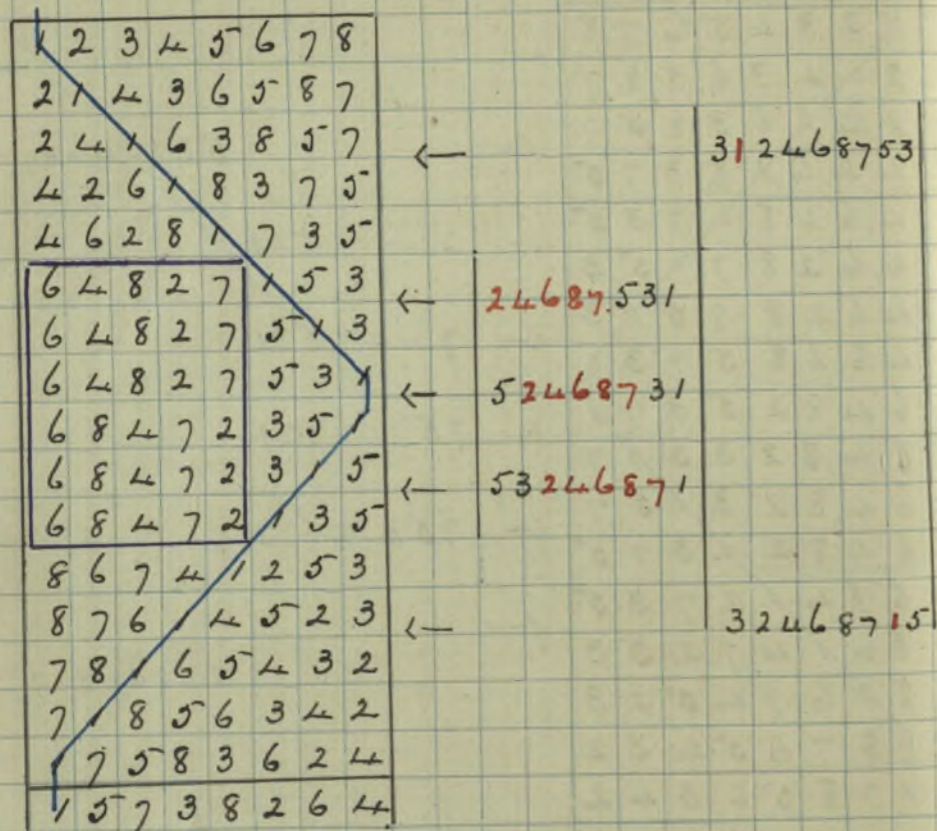


COURSING ORDER.

1st. Lead. End.
2nd do
3rd do
4th do
5th do
6th do
7th do

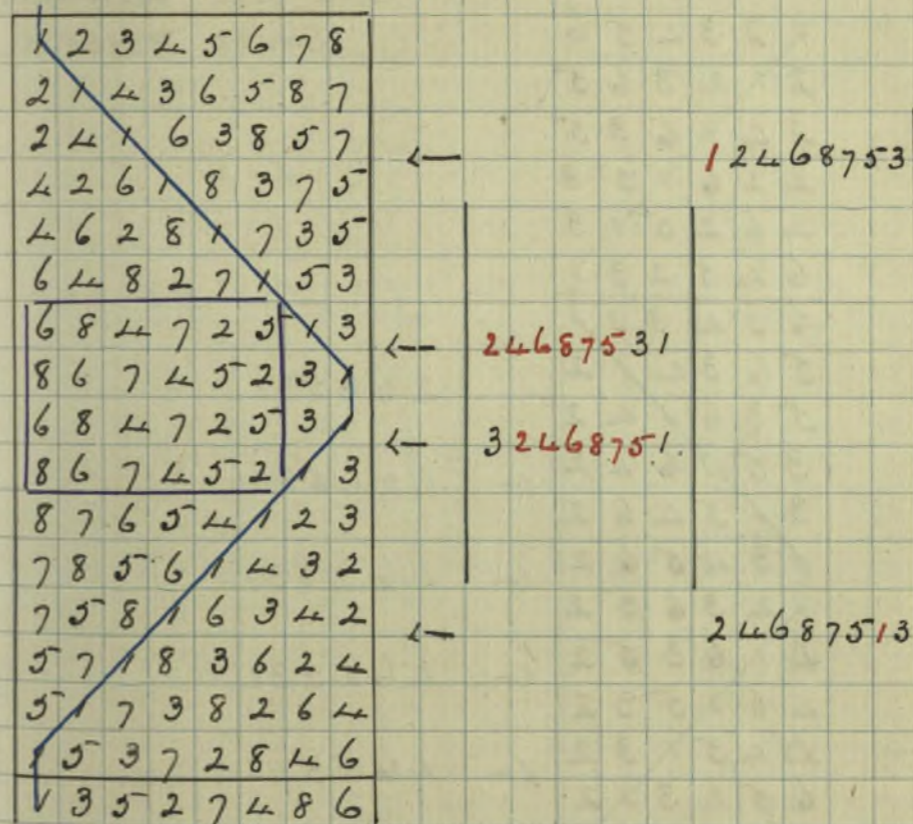
1 2 4 6 8 7 5 3
2 4 6 8 1 7 5 3
2 1 4 6 8 7 5 3
2 4 6 8 7 1 5 3
2 4 1 6 8 7 5 3
2 4 6 8 7 5 1 3
2 4 6 1 8 7 5 3
1 2 4 6 8 7 5 3

FIVE BELL SLOW WORK SHUNT.



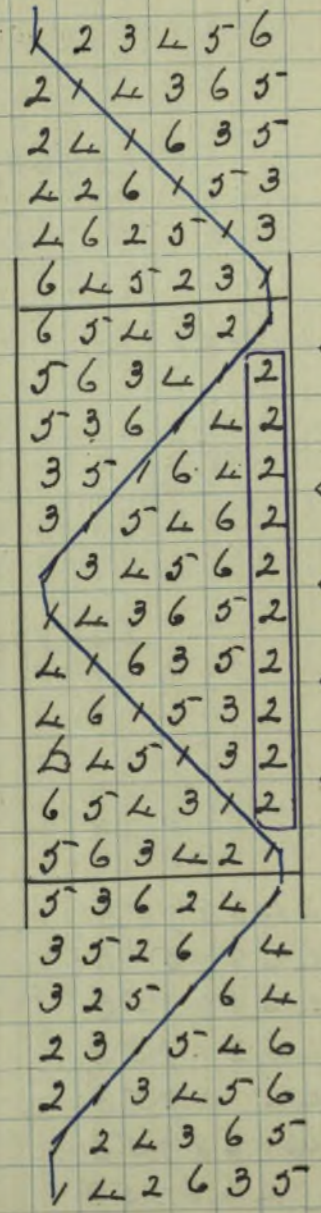
- 1st Lead End 1 2 4 6 8 7 5 3
- 2nd do 2 4 6 8 7 1 5 3
- 3rd do 2 4 6 8 7 5 1 3
- 4th do 2 4 6 8 7 5 1 3
- 5th do 2 4 6 8 1 7 5 3
- 6th do 2 4 1 6 8 7 5 3
- 7th do 1 2 4 6 8 7 5 3

SIX BELL SLOW WORK SHUNT



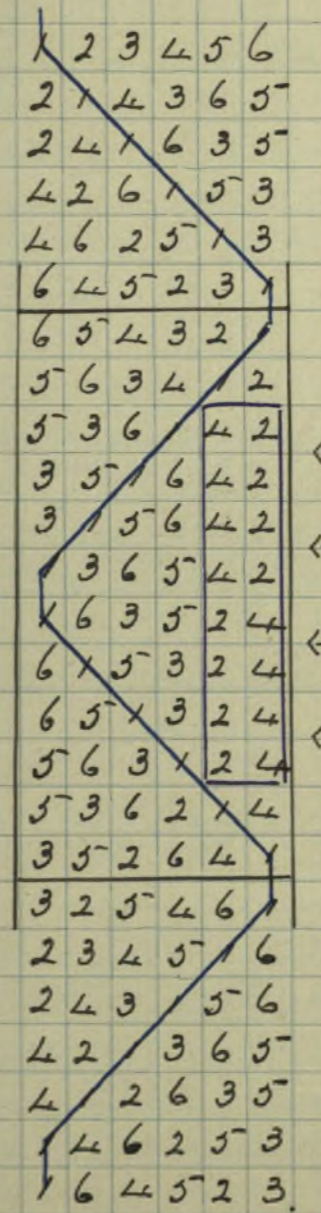
- 1st Lead End 1 2 4 6 8 7 5 3
- 2nd do 2 4 6 8 7 5 1 3
- 3rd do 2 4 6 8 7 1 5 3
- 4th do 2 4 6 8 1 7 5 3
- 5th do 2 4 1 6 8 7 5 3
- 6th do 2 1 4 6 8 7 5 3
- 7th do 1 2 4 6 8 7 5 3

ONE BELL SLOW WORK
SHUNT REVERSE.



← 531246
 ← 246531
 ← 426531
 ← 462531
 ← 465231
 ← 465321
 ← 532146

TWO BELL SLOW WORK
SHUNT REVERSE.



← 312465
 ← 246531
 ← 624531
 ← 652431
 ← 653241
 ← 324165

If the number of Extreme Bells = $x-y$.
 Then the possible number of Slow Work
 Shunts = $x-y-1$.

The $x-y-1$ Bell Shunt is the same as an
 Extreme. See Example (6-Bell Row
 Work Shunt with seven Extreme Bells)
 on page 181.

The Extremes, the Court Shunts, and the
 Slow Work Shunts are the only means
 by which the Shunt in any method
 on the Plain Principle can change its
 position in Coupling Order. They are
the only possible Constructional Shunts.

Each one of the Extreme Shunts, or of
 the different varieties of Court Shunts,
 puts the Shunt one position forward
 in Coupling Order.

Therefore as many of these Shunts
 as there are Extreme Bells, or any
 multiple of that number, will complete
 the Shunt's Cyclical path in Coupling
 Order, and will bring the bells
 back to the Row from which they
 originally started. This will be

	1	2	3	4	5	6
	2	1	4	3	6	5
	2	4	1	3	5	6
Rd. A2	4	2	3	1	6	5
	2	4	3	6	1	5
	4	2	6	3	5	1
	4	6	2	5	3	1
R Single cl. B1	6	4	5	2	3	1
	4	6	5	1	2	3
	6	4	1	5	3	2
	6	4	3	5	2	1
	6	3	4	2	5	1
	1	3	6	2	4	5
	3	1	2	6	5	4
	3	2	1	5	6	4
B2	2	3	5	1	4	6
	3	2	5	4	1	6
Ex.	2	3	4	5	6	1
	3	2	5	4	6	1
	2	3	4	5	1	6
C1	2	4	3	5	6	1
	2	4	1	3	6	5
	2	1	4	6	3	5
	2	4	3	6	5	1
	1	2	3	4	5	6

A1 Rcl.

R Single cl. B1

B2

Ex.

C1

C2 Rcl.

Ex.

entirely irrespective of whether the Shunts are arranged in any symmetrical order or no; or whether the Block is divided into equal Leads or no.

See Example in which there are five Exclamation Marks and the following Shunts

Exclamation Marks = 2

R. Count

Shunts = 1.

P. Count

Shunts = 1.

Reverse Single

Count Shunts = 1.

Total. 5

But in any method that conforms to the conditions generally required by the Exercise,

it is necessary that they should be

arranged so that (1) every Lead is alike and (2) that each Lead should be symmetrical about a line drawn through the Points whole pull behind when there is one Point; or midway between the Points' whole pull behind where there are five Points.

On page 321-9, I give a formula which gives all possible arrangements of these Points on all numbers of Cells under these conditions.

Not all these arrangements are suitable for use as practical methods, but all can be used as the foundations of methods.

Each single one of these Points - Extremes or Count Points - put the Point one position forward in Counting Order and therefore each will produce the Lead End 13527486-----

To get the Lead End when there are five or more Points in the Lead, transpose the preceding Lead End by 13527486----- as many times as there are Points.

Thus if a Lead containing five Count Points and one Extreme, follow

16 4 2 3 5 7 8 The Lead End produced
 will be 6 4 2 3 5 7 8 * (3 5 2 7 4 8 6) =
 7 8 3 5 4 2 6.

3 5 5

1	6	4	2	3	5	7	8
6	1	2	4	5	3	8	7
6	2	1	5	4	8	3	7
2	6	5	1	8	4	7	3
2	5	6	8	1	4	3	7
5	2	8	6	4	1	7	3
2	5	6	8	4	7	1	3
5	2	8	6	7	4	3	1
2	5	6	8	4	7	3	1
5	2	8	6	7	4	3	1
2	5	6	8	7	1	4	3
5	2	8	6	1	7	3	4
5	8	2	6	7	4	3	1
8	5	2	7	6	3	4	1
8	5	7	2	3	6	4	1
8	7	5	3	2	4	6	1
7	8	3	5	4	2	6	1

← C.O. = 4 1 6 2 5 8 7 3.

A1 R.C.

A2.

← C.O. = 1 4 6 2 8 7 5 3

Ex.

← C.O. = 4 6 2 8 7 5 1 3

B2.

B1 R.C.

← C.O. = 4 6 2 8 7

A Slow Work Shift puts the Hunt
 backward in Counting Order as many
 positions as there are bells in the Shift.
 Therefore a 1 Bell Slow Work Shift will

produce from rounds the Lead End
 $14263857 \dots$

To find the Lead End produced by
 any Slow Work Skunt, transpose the
 preceding Lead End by $14263857 \dots$
 as many times as there are bells in
 the Skunt.

Thus from the Lead End 16423578
 a 3-Bell Slow Work Skunt will give
 the following Lead End $6423578 \times (14263857)^3$
 $= 80572364$.

As the movement of an Excieme or
 a Court skunt is + and the movement
 of a Slow Work Skunt is -, in any
 Block containing these Skunt mixed,
 the bells will come round when the
 sum of the Skunts = 0 or any
 multiple of the number of Excieme
 Bells. This will happen quite
 irrespective of whether the Skunts
 are arranged symmetrically, or whether
 the Block is divided into similar
 Leads.

Thus, with seven Excieme Bells,
 3 Excieme Skunts, 10 Court Skunts,
 1 4-Bell Slow Work Skunt and 1 2-Bell
 Slow Work Skunt ($3+10-4-2$) will bring

the bells back to the Row from which they originally started.

To comply with the accepted standards of symmetry, only one kind of Slow Work Shunt can be used in any one method.

Slow Work Shunts in their natural form, are not suitable for use in methods for practical ringing; but by means of Additional Points their disadvantages can be removed, while at the same time their Constitutional work and value are fully retained.

On page 321. I give a formula which will produce every possible Slow Work Shunt on all numbers and also on page 329, a formula giving all the combinations of Extremes Coult Shunts and Slow Work Shunts.

For purely practical purposes Reverse Coult Shunts and Reverse Slow Bell Shunts are of little value.

Chapter IX

Methods which are founded
on Hunts and Extreme Bells.
(Continued)

Additional Shunts.

Additional Shunts are cyclical movements made by two or more of the Extreme Bells of the main movement of the Constructional Shunts, the number of bells involved being less than the total number of Extreme Bells.

They do not differ in nature from the Constructional Shunts. By the nature of cyclical movement they must consist of Hunts and Extreme Bells, with the three characteristic cyclical movements. It is convenient to treat them as either Hunting Courses or Dodging Movements on certain bells, and to leave the Hunts and their cyclical path in Coursing Order to be implied.

Constructional ^{Shunts} settle the main

Construction of the Course, the length of the Course, the number of the Leads, and the Natural Lead Ends.

Additional Shunts do not affect these things. Their uses are to introduce fresh work into the Method, to remove blemishes left by the Constructional Shunts, and in the case of the Treble Bob and other Principles, to counteract the natural falseness of those Principles.

Additional Shunts fall into two groups -

(a) Those which are wholly made within one Lead, and

(b) Those whose operation extends to five or more Leads.

Methods which have the second kind of Additional Shunt are not, now a days, considered to reach the standard required for practical ringing.

Fig. M.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	6	5	8	7
2	4	3	6	1	5	7	8
4	2	6	3	5	1	8	7
2	4	3	6	5	8	1	7
4	2	6	3	8	5	7	1
2	4	3	6	5	8	7	1
4	2	6	3	8	5	1	7
2	4	3	6	8	1	5	7
4	2	6	3	1	8	7	5
2	4	6	3	8	5	7	1
4	2	6	8	3	7	5	1
4	2	6	3	8	5	7	1
4	6	2	8	3	7	5	1
1	6	4	8	2	7	3	5

Let Fig M. be the Lead of any Course, produced by Constitutional Points.

In any Change in M let a number of the Extreme Bells (less than the total) take a step in the opposite direction to that they are taking in M.

Let the Bells be 2, 3, 4, 6 and the Change the fifth.

		instead of	
2	4	3	6
2	3	4	6
4	2	6	3

This introduces a fresh Courning Order of the total number of Extreme Bells. The original Courning Order must be regained before the bells can return to the same row from which they started. This can only be done as follows.

(a) The four bells can complete the Hunting Course movement they have started;

- (b) The four bells can make a Dodging Movement among themselves.
 - (c) The Courning Order can be regained by a series of cyclical movements.
- Pr: The Courning Order cannot be regained by any movement which is not complete cyclical

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	6	5	8	7
2	4	3	6	1	5	7	8
2	3	4	6	5	1	8	7
3	2	6	4	5	8	1	7
3	6	2	4	8	5	7	1
6	3	4	2	5	8	7	1
6	4	3	2	8	5	1	7
4	6	2	3	8	5	7	1
4	2	6	3	1	8	7	5
2	4	6	1	3	8	5	7
4	2	1	6	8	3	7	5
4	1	2	6	3	8	5	7
4	6	2	8	3	7	5	1
4	6	4	8	2	7	3	5

In this Example a Complete Hunting Course has been made on 2346.

2	4	3	6
2	3	4	6
3	2	6	4
3	6	2	4
6	3	4	2
6	4	3	2
4	6	2	3
4	2	6	3

and at its completion the Courning order of M is regained

1	2	3	4	5	6	7	8	9	0
2	1	4	3	6	5	8	7	0	9
2	4	1	3	5	6	7	8	9	0
4	2	3	1	6	5	8	7	0	9
2	4	3	6	1	5	7	8	9	0
2	3	4	6	5	1	8	7	0	9
3	2	6	4	5	8	1	7	9	0
2	3	4	6	8	5	7	1	0	9
2	4	3	6	5	8	7	0	1	9
4	2	6	3	8	5	0	7	9	1
2	4	3	6	5	8	7	0	9	1
4	2	6	3	8	5	0	7	1	9
4	6	2	3	5	8	0	7	9	1
6	4	3	2	8	5	0	9	7	1
4	6	2	3	8	1	5	0	7	9
4	2	6	3	1	8	0	5	9	7
2	4	6	1	3	8	5	0	7	9
4	2	1	6	8	3	0	5	9	7
4	1	2	6	3	8	5	0	7	9
1	4	6	2	8	3	0	5	9	7
1	6	4	8	2	0	3	9	5	7

In this Example a dodging movement is made on 2436 in the first Half Lead; and another similar, but quite independent one, in the second Half Lead.

2	4	3	6
2	3	4	6
3	2	6	4
2	3	4	6
2	4	3	6

In both the foregoing Examples the movement of the Additional Stunt is begun in one Change and completed without

interruption in the following successive Changes. In the next Example the Stunt is begun at the beginning of the Lead and not completed till the end.

THE CONSTRUCTIONAL SHUNTS

ADDITIONAL SHUNT ON 5-6.

COSLANY C.B. MAJOR

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	5	7	6	8
2	4	3	5	1	7	8	6
2	3	4	5	7	1	6	8
3	2	5	4	7	6	1	8
2	3	4	5	6	7	8	1
2	4	3	6	5	8	7	1
4	2	6	3	8	5	1	7
2	4	3	6	8	1	5	7
2	3	4	6	1	8	7	5
3	2	4	1	6	8	5	7
2	3	1	4	6	5	8	7
2	1	3	4	5	6	7	8
1	2	4	3	6	5	8	7
1	4	2	6	3	8	5	7

1	2	3	4	5	6	7	8
2	1	4	3	5	6	8	7
2	4	1	3	6	5	7	8
4	2	3	1	6	7	5	8
2	4	3	6	1	7	8	5
2	3	4	6	7	1	5	8
3	2	6	4	7	5	1	8
2	3	4	6	5	7	8	1
2	4	3	5	6	8	7	1
4	2	5	3	8	6	1	7
2	4	3	5	8	1	6	7
2	3	4	5	1	8	7	6
3	2	4	1	5	8	6	7
2	3	1	4	5	6	8	7
2	1	3	4	6	5	7	8
1	2	4	3	6	5	8	7
1	4	2	6	3	8	5	7

The Slow Work Shunts in their natural form are not suitable for use in practical methods. The elements may be removed by Additional Shunts, as follows:-

TWO BELL SLOW WORK SHUNT.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
2	4	6	1	8	3	7	5
2	4	6	8	1	7	3	5
2	4	8	6	7	1	5	3
2	4	8	7	6	5	1	3
2	4	7	8	5	6	3	1
4	2	7	5	8	3	6	1
4	2	5	7	3	8	1	6
4	2	5	3	7	1	8	6
4	2	3	5	1	7	6	8
4	2	3	1	5	6	7	8
4	2	1	3	6	5	8	7
4	2	6	3	8	5	7	1
4	6	2	8	3	7	5	1
1	6	4	8	2	7	3	5

COLLEGE MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	6	8	1	7	3	5
4	2	8	6	7	1	5	3
2	4	8	7	6	5	1	3
4	2	7	8	5	6	3	1
2	4	7	5	8	3	6	1
4	2	5	7	3	8	1	6
2	4	5	3	7	1	8	6
4	2	3	5	1	7	6	8
2	4	3	1	5	6	7	8
4	2	1	3	6	5	8	7
4	2	6	3	8	5	7	1
4	6	2	8	3	7	5	1
1	6	4	8	2	7	3	5

FOUR BELL SLOW WORK SHUNT

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
4	6	2	8	7	1	5	3
4	6	2	8	7	5	1	3
4	6	2	8	5	7	3	1
6	4	8	2	5	3	7	1
6	4	8	2	3	5	1	7
6	4	8	2	3	1	5	7
6	4	8	2	3	7	5	1
6	8	4	2	7	3	5	1
8	6	4	7	2	5	3	1
8	6	7	4	5	2	3	1
1	8	7	6	5	4	3	2
1	7	8	5	6	3	4	2

KENT COLLEGE MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
4	6	2	8	7	5	1	3
6	4	8	2	5	7	3	1
4	6	2	8	5	3	7	1
6	4	8	2	3	5	1	7
4	6	2	8	3	1	5	7
6	4	8	2	3	7	5	1
6	8	4	2	7	3	5	1
8	6	4	7	2	5	3	1
8	6	7	4	5	2	3	1
1	8	7	6	5	4	3	2
1	7	8	5	6	3	4	2

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	5	7	6	8
2	4	3	5	1	7	8	6
2	3	4	5	7	1	6	8
3	2	5	4	7	6	1	8
2	3	4	5	6	7	8	1
3	2	5	4	7	6	8	1
2	3	4	5	6	7	1	8
3	2	5	4	6	1	7	8
3	5	2	4	1	6	8	7
5	3	2	1	4	6	7	8
3	5	1	2	4	7	6	8
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
4	3	5	2	7	4	8	6

1	2	3	4	5	6	7	8	A1
2	1	4	3	5	7	6	8	
2	4	1	3	7	5	8	6	A2
4	2	3	1	5	7	6	8	
2	4	3	5	1	7	8	6	B1
4	2	5	3	7	1	6	8	
2	4	3	5	7	6	1	8	B2
2	3	4	5	6	7	8	1	
3	2	5	4	7	6	8	1	C2
3	5	2	4	6	7	1	8	
5	3	4	2	6	1	7	8	E1
3	5	2	4	1	6	8	7	
5	3	2	1	4	6	7	8	D2
3	5	1	2	4	7	6	8	
3	1	5	2	7	4	8	6	D1
1	3	2	5	4	7	6	8	
4	3	5	2	7	4	8	6	

In this example four bells 5678 in the first change make one step backward instead of forward. In the third change the same bells make one step forward instead of backward, the two making a complete dodging movement. Three other similar additional permutations, each independent of the others, are made

within the Lead.

If to any Lead produced by Constructive Shuntis, a number of Additional Shuntis is added, a fresh Lead is produced which has the same Lead End as the first Lead.

To this fresh Lead further Additional Shuntis may be added, which will produce a third Lead, with the same Lead End.

The movement of the bells will be the result of the Principle, the Constructive Shuntis and the various Additional Shuntis. One step of any one Bell may be the result of several Cyclical movements, + movement Counteracting - movement.

It follows, that to show the different Cyclical movements that go to make up some of the more complex methods, two or more Leads must be written out.

The following are Examples of these overlapping Additional Shuntis.

1. THE PLAIN PRINCIPLE
ONE EXTREME CONSTRUCTIONAL
SHUNT. BOB, TRIPLES.

1	2	3	4	5	6	7
2	1	4	3	6	5	7
2	4	1	6	3	7	5
4	2	6	1	7	3	5
4	6	2	7	1	5	3
6	4	7	2	5	1	3
6	7	4	5	2	3	1
7	6	5	4	3	2	1
7	5	6	3	4	1	2
5	7	3	6	4	2	1
5	3	7	1	6	2	4
3	5	1	7	2	6	4
3	1	5	2	7	4	6
1	3	2	5	4	7	6
1	3	5	2	7	4	6

2. ADDITIONAL SHUNTS
ON 5-6, and 4-7.

1	2	3	4	5	6	7
2	1	4	3	5	6	7
2	4	1	5	3	7	6
4	2	5	1	7	3	6
4	5	2	7	1	6	3
5	4	7	2	6	1	3
5	4	7	6	2	3	1
4	5	6	7	3	2	1
4	5	6	3	7	1	2
5	4	3	6	1	7	2
5	3	4	1	6	2	7
3	5	1	4	2	6	7
3	1	5	2	4	7	6
1	3	2	5	4	7	6
1	3	5	2	7	4	6

3. ADDITIONAL SHUNTS
ON 6-7 and 4-5

1	2	3	4	5	6	7
2	1	4	3	5	7	6
2	4	1	5	3	6	7
4	2	5	1	6	3	7
4	5	2	6	1	7	3
5	4	6	2	7	1	3
4	5	6	7	2	3	1
5	4	7	6	3	2	1
4	5	7	3	6	2	1
5	4	3	7	1	6	2
5	3	4	1	7	2	6
3	5	4	2	7	6	1
3	5	2	4	6	7	1
1	3	2	5	4	7	6
1	3	5	2	7	4	6

4. ADDITIONAL SHUNTS
ON 3-4 and 2-5.

1	2	3	4	5	6	7
2	1	3	4	5	7	6
2	3	1	5	4	6	7
3	2	5	1	6	4	7
3	2	5	6	1	7	4
2	3	6	5	7	1	4
3	2	6	7	5	4	1
2	3	7	6	4	5	1
3	2	7	4	6	1	5
2	3	4	7	1	6	5
2	3	4	1	7	5	6
3	2	1	4	5	7	6
3	2	5	4	6	7	1
1	3	2	5	4	7	6
1	3	5	2	7	4	6

5. ADDITIONAL SHUNTS
ON 4-5 and 2-3.
NEW BOB, TRIPLES.

1	2	3	4	5	6	7
2	1	3	5	4	7	6
2	3	1	4	5	6	7
3	2	4	1	6	5	7
2	3	4	6	1	7	5
3	2	6	4	7	1	5
2	3	6	7	4	5	1
3	2	7	6	5	4	1
2	3	7	5	6	1	4
3	2	5	7	1	6	4
2	3	5	1	7	4	6
3	2	5	4	7	6	1
1	3	2	5	4	7	6
1	3	5	2	7	4	6

1. The PLAIN PRINCIPLE
EXTREME CONSTRUCTIONAL
SHUNT.

BOB MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	7	2	8	4	6	1
3	1	5	2	7	4	8	6
3	2	5	4	7	6	8	1
1	3	5	2	7	4	8	6

2. ADDITIONAL SHUNTS
ON 2-6 and 3-7.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	2	6	8	1	3	7	5
2	4	8	6	3	1	5	7
2	8	4	3	6	5	1	7
8	2	3	4	5	6	7	1
8	3	2	5	4	7	6	1
3	8	5	2	7	4	1	6
3	5	8	7	2	1	4	6
5	3	7	8	1	2	6	4
5	3	7	1	8	2	6	4
3	5	7	2	8	4	6	1
3	1	5	2	7	4	8	6
3	2	5	4	7	6	8	1
1	3	5	2	7	4	8	6

3. ADDITIONAL SHUNTS
ON 3-4 5-6 2-5 4-7.

1	2	3	4	5	6	7	8
2	1	3	4	5	6	8	7
2	3	1	5	4	8	6	7
3	2	5	1	8	4	7	6
3	2	5	8	1	4	7	6
2	3	8	5	4	1	6	7
2	8	3	4	5	6	1	7
8	2	3	4	5	6	7	1
8	3	2	5	4	7	6	1
3	8	2	5	4	7	1	6
3	2	8	4	5	1	7	6
2	3	4	8	1	5	6	7
2	3	4	1	8	5	6	7
3	2	1	4	5	8	7	6
3	1	2	5	4	7	8	6
3	2	5	4	7	6	8	1
1	3	5	2	7	4	8	6

4. ADDITIONAL SHUNTS
ON 4-5 (twice) 2-3 6-7

BIRMINGHAM. BOB MAJOR.

1	2	3	4	5	6	7	8
2	1	3	5	4	6	8	7
2	3	1	4	5	8	6	7
3	2	4	1	8	5	7	6
2	3	4	8	1	5	6	7
3	2	8	4	5	1	7	6
3	8	2	5	4	7	1	6
8	3	2	4	5	7	6	1
8	2	3	5	4	6	7	1
2	8	3	4	5	6	1	7
2	3	8	5	4	1	6	7
3	2	5	8	1	4	7	6
2	3	5	1	8	4	6	7
3	2	1	5	4	8	7	6
3	1	2	4	5	7	8	6
3	2	5	4	7	6	8	1
1	3	5	2	7	4	8	6

(First produced and named
by Henry Johnson)

Additional Shunts do not affect the main Construction of the Course which is the Concern of the Constructional Shunts; and when they are made each wholly within one Lead, they do not affect the Lead Ends. It is also obvious that if an Additional Shunt is begun in one Lead and completed in another, since it is a cyclical movement on a given number of bells, it will not affect the main Construction of the Course. It will differ from one made wholly within one Lead only in the fact that it obscures the Lead Ends produced by the Constructional Shunts.

The following Example shows:-

1. A Course produced by 2 Extremes and 4 R Count Shunts in each Lead, (= Double Oxford Major)
2. A 4-BELL Additional Shunt made wholly within one lead.
3. A Similar 4 BELL Additional Shunt made partly in one Lead and partly in another.
4. A Combination of 2 and 3.

DOUBLE BOB MAJOR.

DOUBLE CANTERBURY
PLEASURE MAJOR.

3	2	5	7	4	8	6	
2	3	5	4	7	6	8	
2	3	4	5	6	7	8	
2	4	3	6	5	8	7	
2	3	4	5	6	7	8	
2	4	3	6	5	8	7	
2	4	6	3	8	5	7	
4	2	6	8	3	7	5	
4	6	2	8	7	3	5	
6	4	8	2	7	5	3	
6	8	4	7	2	5	3	
8	6	7	4	5	2	3	
6	8	4	7	2	5	3	
8	6	7	4	5	2	3	
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	7	3	8	2	6	4	
5	3	7	2	8	4	6	
5	7	3	8	2	6	4	
5	1	3	7	2	8	4	6
5	3	1	2	7	4	8	6

3	2	5	7	4	8	6	
2	3	5	4	7	6	8	
2	3	4	5	6	7	8	
2	3	4	6	5	8	7	
2	4	3	5	6	7	8	
2	4	3	6	5	8	7	
2	4	6	3	8	5	7	
4	2	6	8	3	7	5	
4	6	2	8	7	3	5	
6	4	8	2	7	5	3	
6	8	4	7	2	5	3	
8	6	7	4	2	5	3	
6	8	4	7	5	2	3	
8	6	7	4	5	2	3	
8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	7	3	8	2	6	4	
5	7	3	8	2	6	4	
5	3	7	2	8	4	6	
5	3	7	2	8	4	6	
5	3	1	2	7	4	8	6

In the Examples I have given the Additional Shuntis made partly in one Lead and partly in another, are yet made continuously and in Consecutive Changes. Additional Shuntis made in parts which are separated from each other, or Additional Shuntis which overlap each other, will not, in other respects, be different in nature from these Examples.

The Constitution of every possible Method on the Plain Principle whether symmetrical or not, whether good or bad according to any standard, is produced by some form of the Shuntis I have described in the last five Chapters.

Chapter X

Methods which are founded
on Shunts and Extreme Bells
(Continued)

Methods on the Treble Bob Principle

The Treble Bob Principle consists of the Cyclical movement of the Plain Principle, with the addition of certain Dodging Movements arranged symmetrically. It produces exactly the same Rows as the Plain Principle, and in the same order, but with repetitions.

It follows that every Shunt, and every Combination of Shunts, which will work on the Plain Principle, can be applied to the forward movement of the Treble Bob Principle, and will give exactly the same results and produce the same Rows. But since no Method may contain repetition of Rows further Shunts must be introduced to clear the natural falseness of the Principle.

These Shuntis will in the majority of cases (but not always) be additional Shuntis, and their nature and uses can best be explained by Examples.

TREBLE BOB, PRINCIPLE
ONE EXTREME SHUNT.

KENNINGHALL T.B. MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1

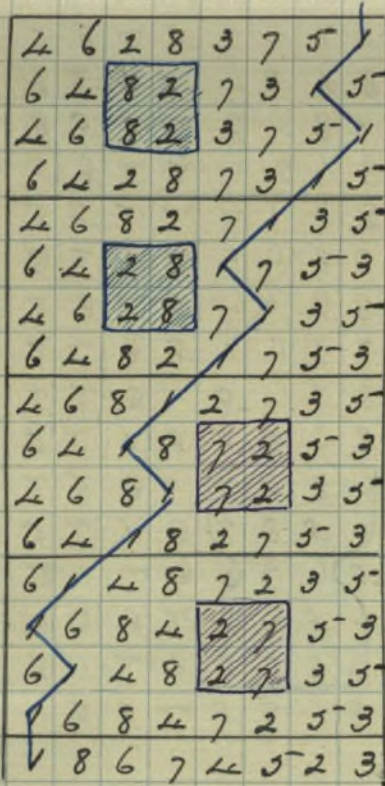
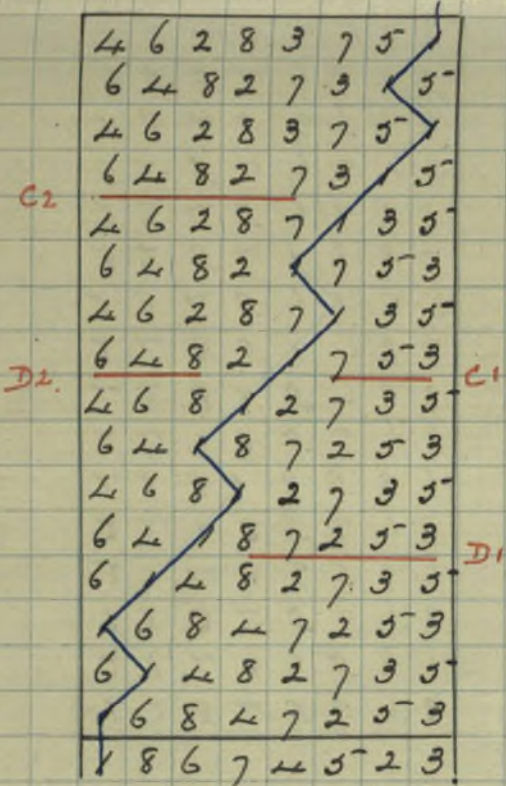
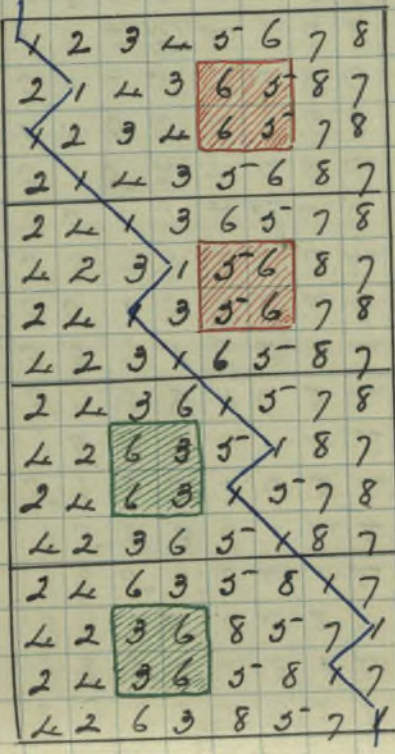
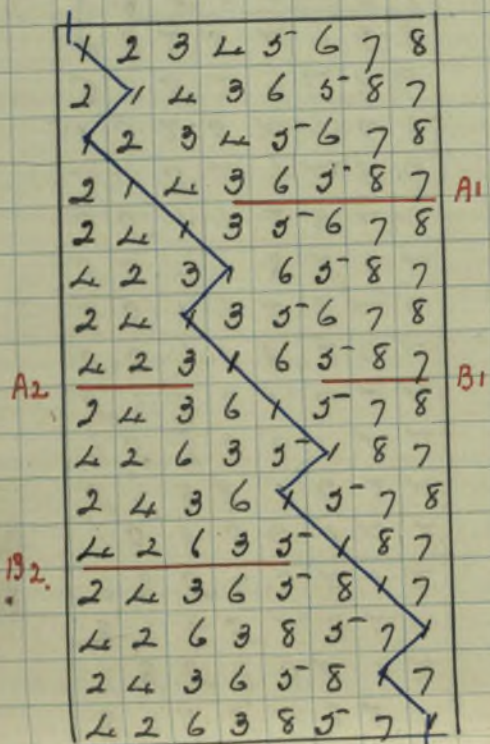
1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
1	2	4	3	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	2	8	7	1	5	3
4	6	2	8	1	7	3	5
6	4	2	8	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1

8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	5	2	7	4	8	6	1
3	2	5	4	7	6	8	1
3	5	2	7	4	8	6	1
3	2	5	4	7	6	8	1
1	3	5	2	7	4	8	6

8	7	6	5	4	3	2	1
7	8	5	6	4	3	1	2
8	7	6	5	3	4	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	5	2	7	4	8	6	1
3	2	5	4	7	6	8	1
3	5	2	7	4	8	6	1
3	2	5	4	7	6	8	1
1	3	5	2	7	4	8	6

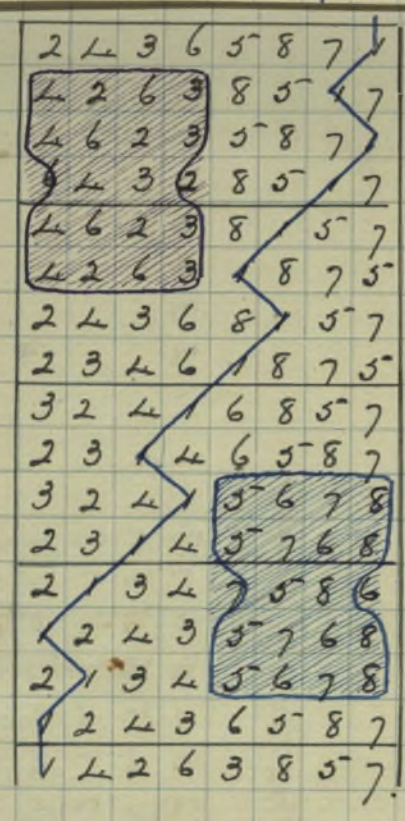
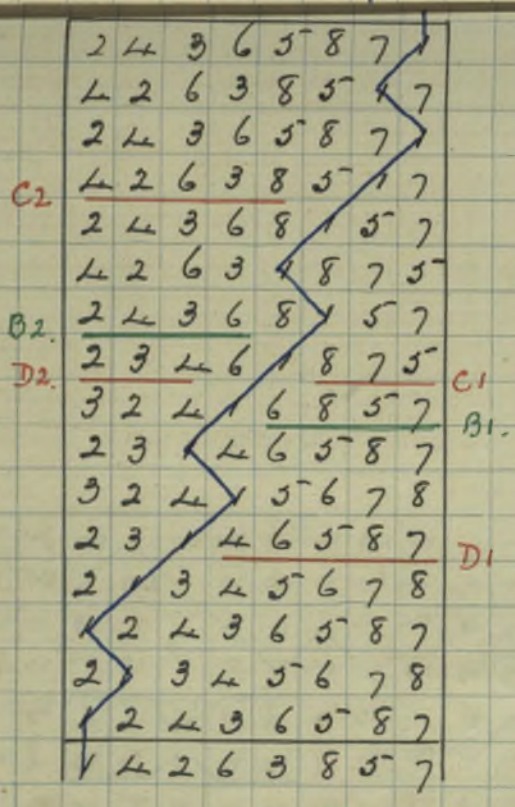
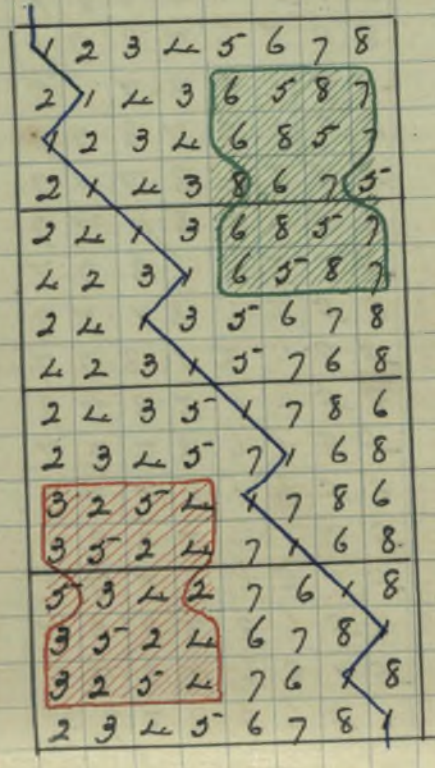
T. B. PRINCIPLE
FOUR. TR. COURT. SHUNTS.

NORFOLK S. MAJOR.



T. B. PRINCIPLE.
 FOUR. R. COURT SHUNTS.
 TWO. T. COURT SHUNTS.

BRISTOL S. MAJOR.



T. B. PRINCIPLE.

FOUR R. COURT SHUNTS.

As page 208.

TWO P. COURT SHUNTS.

THETFORD S MAJ.

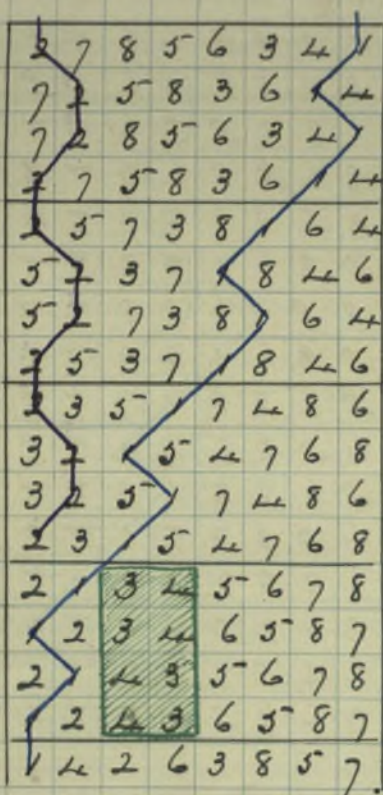
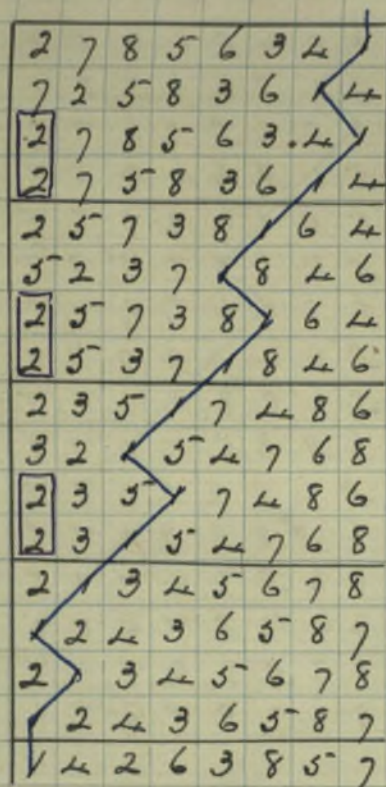
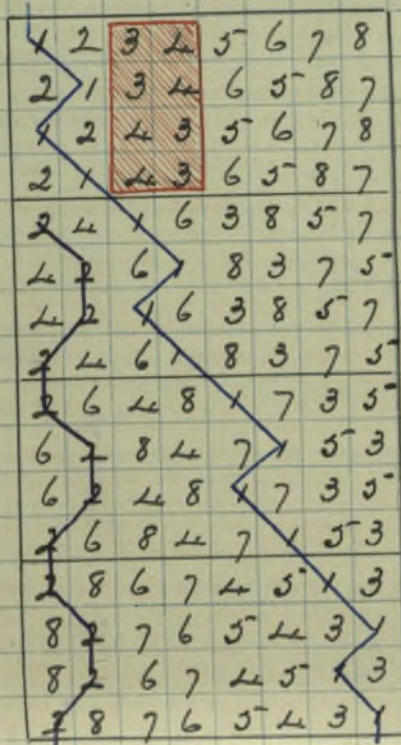
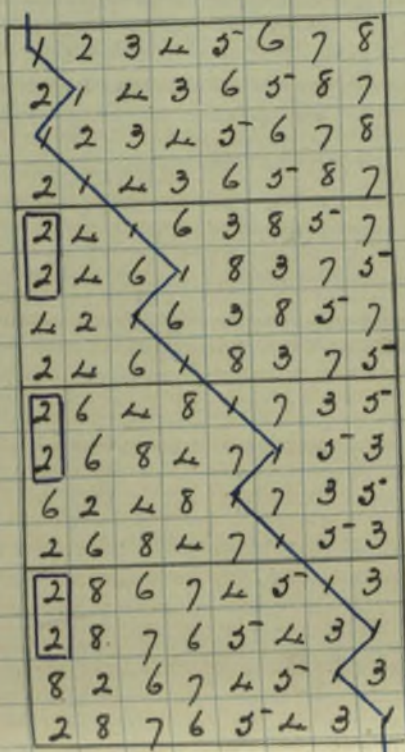
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	6	5	7	8
2	1	4	3	5	6	8	7
2	4	1	3	6	5	7	8
4	2	3	1	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	5	7	6	8
2	4	3	5	1	7	8	6
2	3	4	5	7	1	6	8
3	2	5	4	1	7	8	6
2	3	5	4	7	1	6	8
3	2	4	5	7	6	1	8
2	3	5	4	6	7	8	1
3	2	5	4	7	6	1	8
2	3	4	5	6	7	8	1
2	4	3	6	5	8	7	1

1 2 3 4 5 6 7 8

T. B. PRINCIPLE

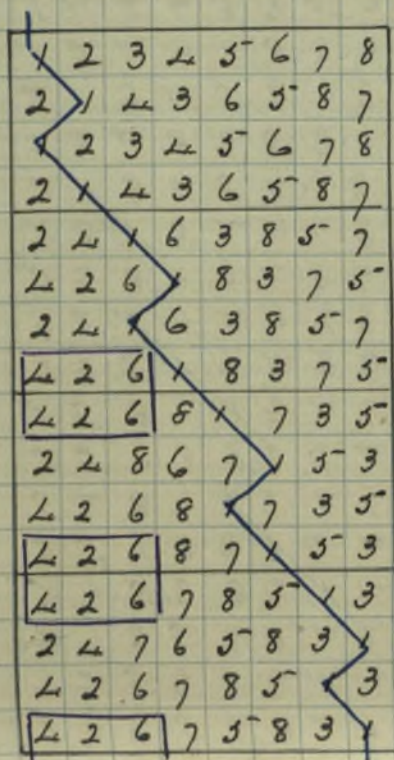
ONE BELL SLOW WORK SHUNT.
See Page 176.

KENT. T. B. MAJOR.

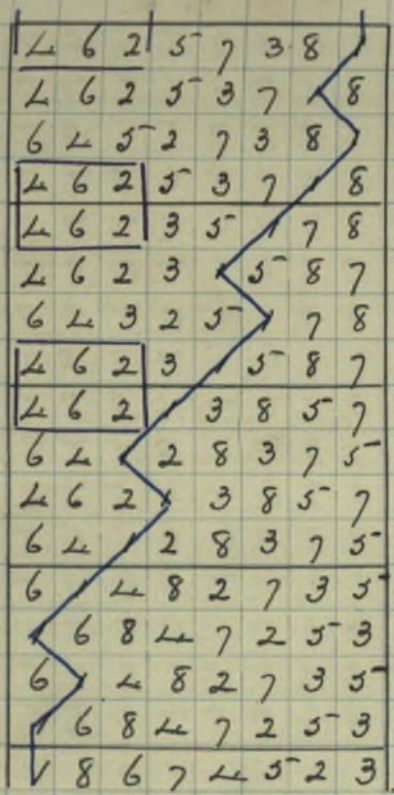
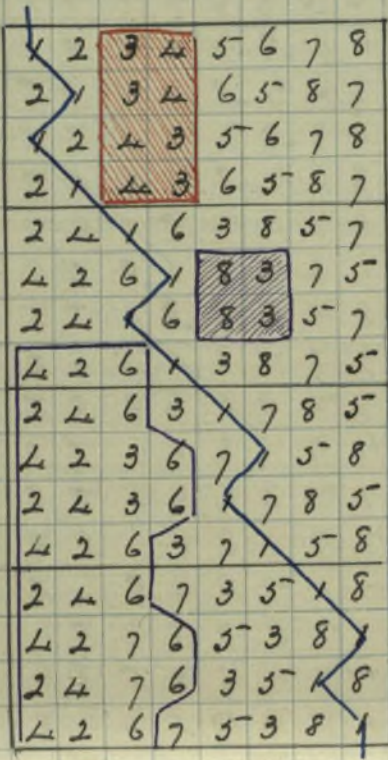


T. B. PRINCIPLE

THREE BELL SLOW WORK SHUNT
(See Page 180)

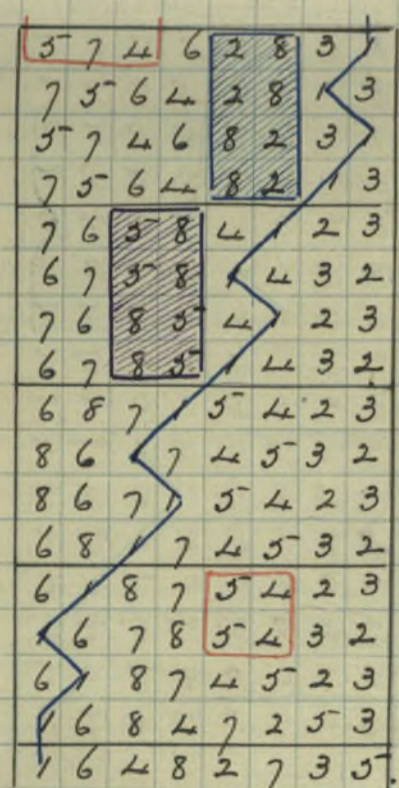
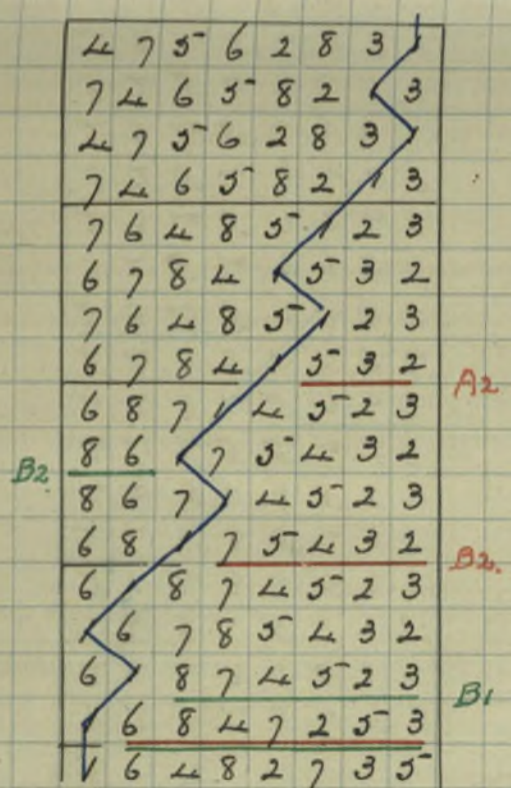
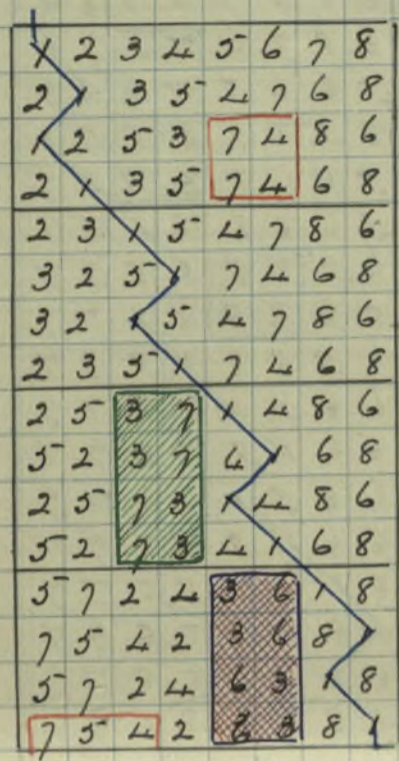
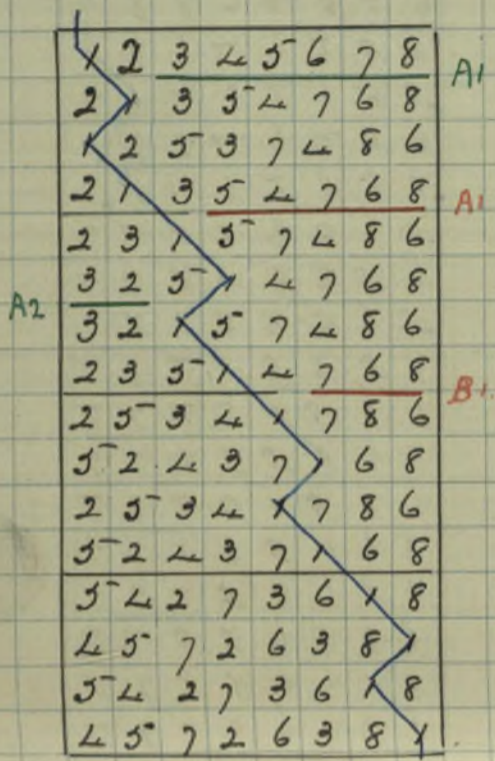


DISS D. MAJOR.



T. B. PRINCIPLE.

TWO . P. COURT SHUNTS.
 TWO . R. SINGLE COURT SHUNTS
 ONE EXTREME SHUNT.

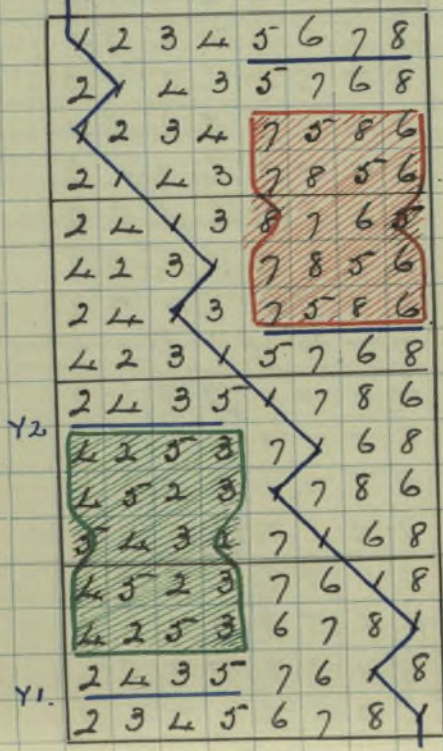
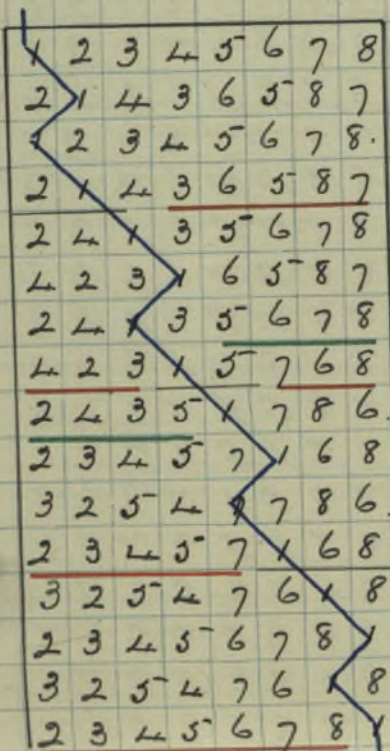


T. B. PRINCIPLE

FOUR R. COURT SHUNTS

TWO P COURT SHUNTS

TWO EXTREME SHUNTS.

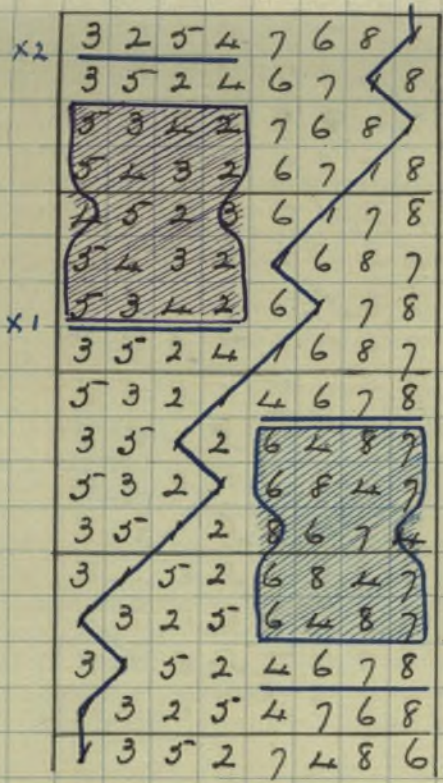
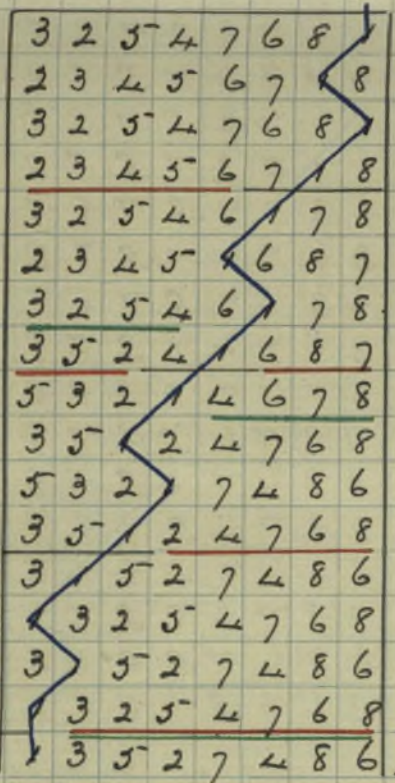


Z2 See Page 196

Z1.

Y2.

Y1.



W1

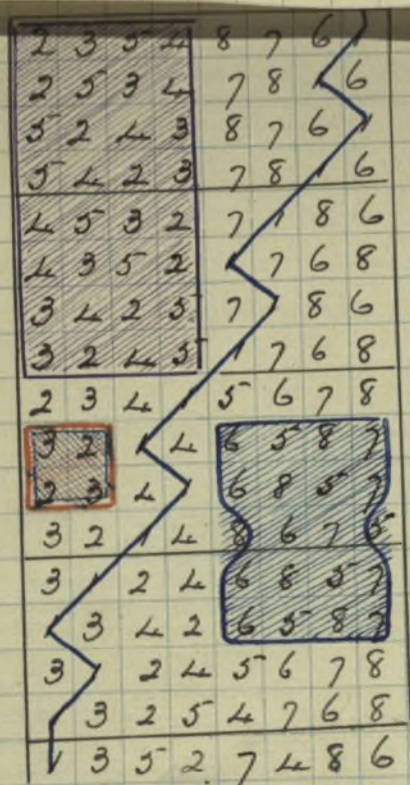
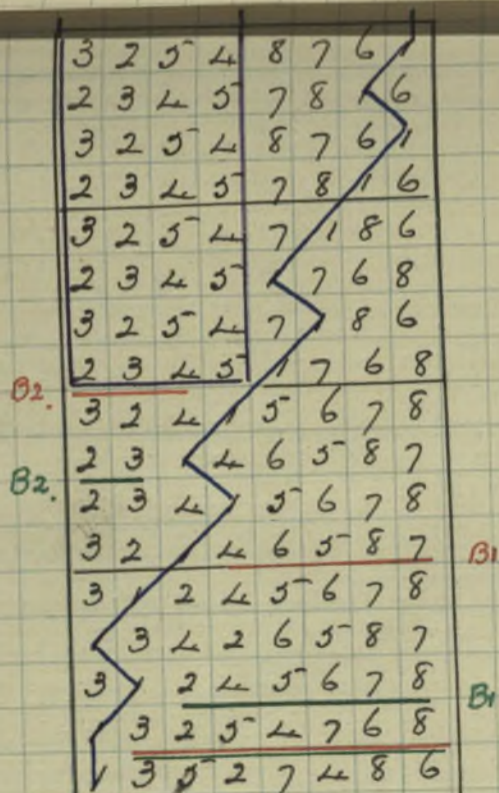
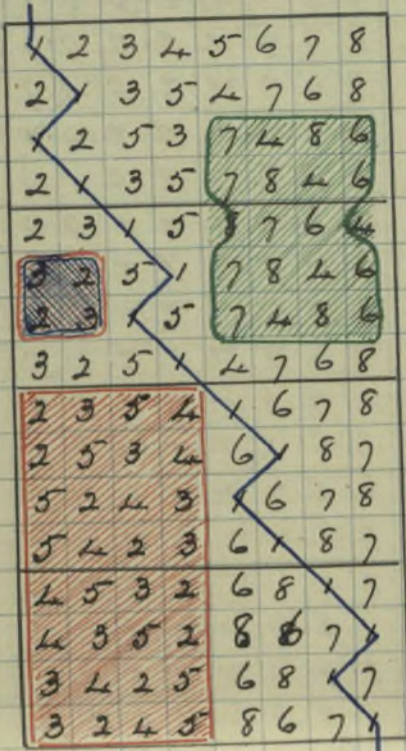
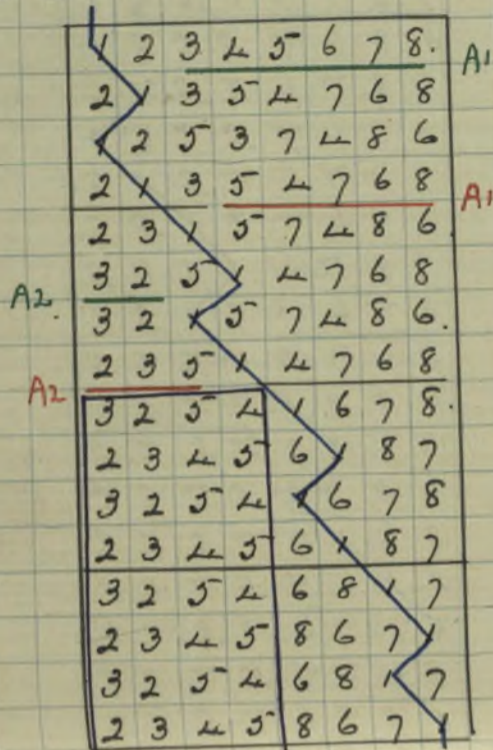
W2

TREBLE BOB PRINCIPLE

TWO R COURT SHUNTS

TWO P COURT SHUNTS.

ONE FOUR BELL SLOW WORK SHUNT
ONE EXTREME SHUNT.



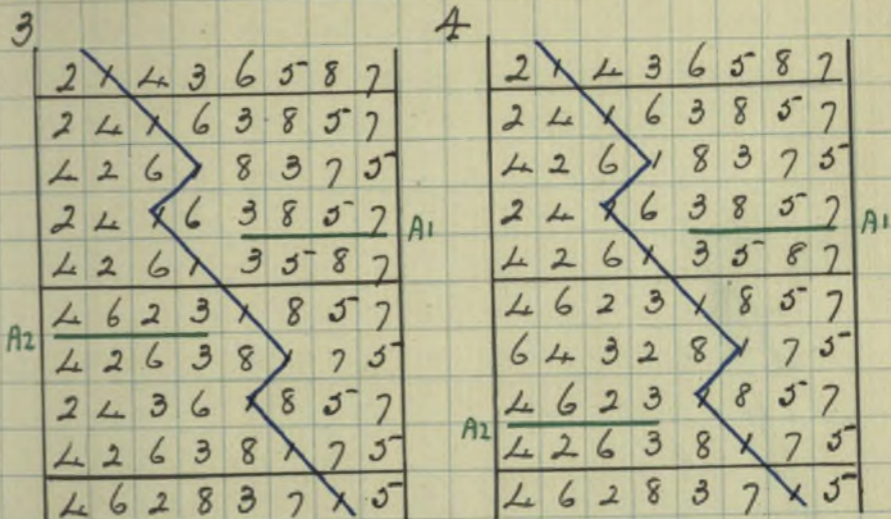
The Extreme Shunt and the R Count Shunt are made at a point in the movement of the Principle which is not repeated. Therefore their number and positions are exactly the same in the Treble P.S. Principle as in the Plain Principle. But the P. Count Shunt are made in positions which are re-duplicated by the Treble P.S. dodging. Therefore there are alternative positions in which they may be made. A P. Count Shunt can take one of the following forms.

1.

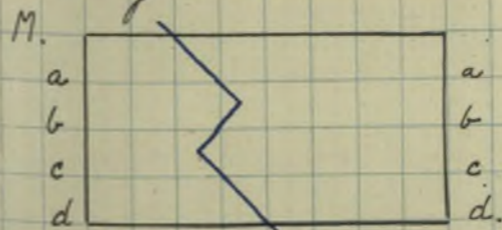
2	x	4	3	6	5	8	7
2	4	x	6	3	8	5	7
4	2	6	x	3	5	8	7
2	4	x	6	5	3	7	8
4	2	6	x	3	5	8	7
4	6	2	3	x	8	5	7
4	2	6	3	8	x	7	5
2	4	3	6	x	8	5	7
4	2	6	3	8	x	7	5
4	6	2	8	3	7	x	5

2.

2	x	4	3	6	5	8	7
2	4	x	6	3	8	5	7
4	2	6	x	3	5	8	7
2	4	x	6	5	3	7	8
4	2	6	x	3	5	8	7
4	6	2	3	x	8	5	7
6	4	3	2	8	x	7	5
4	6	2	3	x	8	5	7
4	2	6	3	8	x	7	5
4	6	2	8	3	7	x	5



And similarly with every other section of the Principle; there are four alternative positions in which a P Count Shunt may be made.

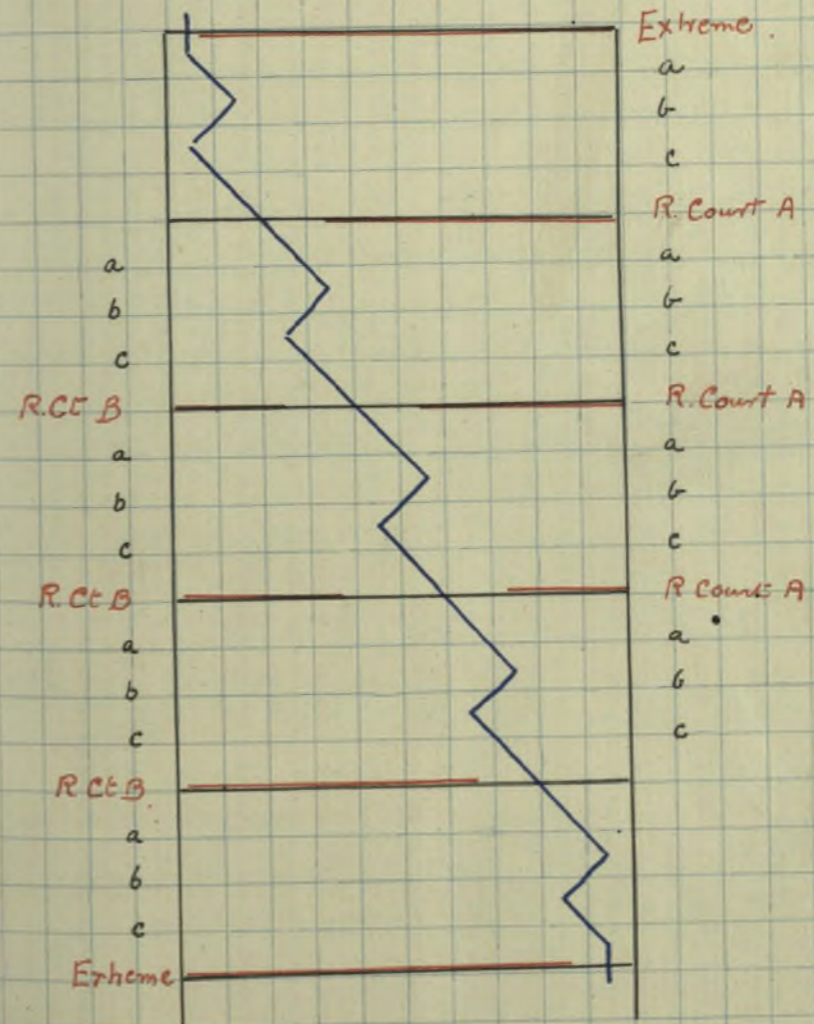


Let M be any one section of the Treble Bob Principle. The Change d.d. belongs to the Forward Hunting

Course part of the movement. It is here that Extremes and R. Count Shunts are made.

The Change b.b. belongs to the Dodging

Positions in the Treble Bob Principle
in which Extreme and Court Shunts can
be made.



Movement exclusively, and therefore the

Shunts of the Plain Principle cannot be reproduced there.

Either (a) or (c) can belong to the Forward Hunting Course; and therefore at either the corresponding Shunts of the Plain Principle can be reproduced.

But both (a) and (c) cannot, at the same time, belong to the Forward Hunting Course; and therefore the Shunts of the Plain Principle cannot be reproduced, at the same time, at both (a) and (c).

It follows that there are two positions in each Section in which Constitutional Shunts can be made which are peculiar to the Trelle Box Principle, -

viz. (b)
and (a) when (c) is taken for a P Court Shunt.

Shunts made at (b) I call B.S. Court Shunts

Shunts made at (a) when a P Court Shunt is made at (c) I call H.S. Court Shunts.

An H.S. Court Shunt (being made when the movement of the Principle is

forward) is very similar to the P Court Shunt. The only difference is in the position in which the second part of the Shunt is made

1	2	3	4	5	6	7	8
2	1	3	5	4	7	6	8
1	2	5	3	7	4	8	6
2	1	5	7	3	8	4	6
2	5	1	3	7	4	8	6
A2.	5	2	3	4	7	6	8
	3	2	1	3	7	4	8
	2	5	3	4	7	6	8

H.S. Court Shunt. (incomplete)

P. Court Shunt A1.

In a P Court Shunt all the bells above the Shunt make one step backward; the place making bell

crosses the Shunt's path, and at once all the bells below the Shunt make one backward step

In a H.S. Court Shunt, the first part of the Shunt is immediately followed by the first part of a P Court Shunt. This prevents the place making bell of the first Shunt, from crossing the Shunt's path; and therefore the bells below the Shunt are not in the proper position to make the second part of the Shunt. Nor will they fall into such a position during

The Lead unless they happen to do so as the result of other Constitutional or Additional Shunts. H.S. Court Shunts, therefore, cannot be used independently of other Shunts.

2 4 6 3 8 5 7	H.S. Court Shunt (incomplete)
4 2 6 3 5 8 7	
2 4 6 5 3 7 8	P. Court Shunt. A1
4 2 6 5 7 3 8	
4 6 2 5 3 7 8	
A2. 4 2 6 5 3 8 7	
2 4 5 6 3 7 8	
4 2 6 5 3 8 7	

In the Example on page 218 to complete the Shunt 2 and 4³ must make each a backward step.

In the above Example. 4 2 6 3 must each make a backward step to complete the Shunt.

Thus.

$$\begin{array}{r} 4 6 2 3 \\ \hline 4 2 6 3 \end{array}$$

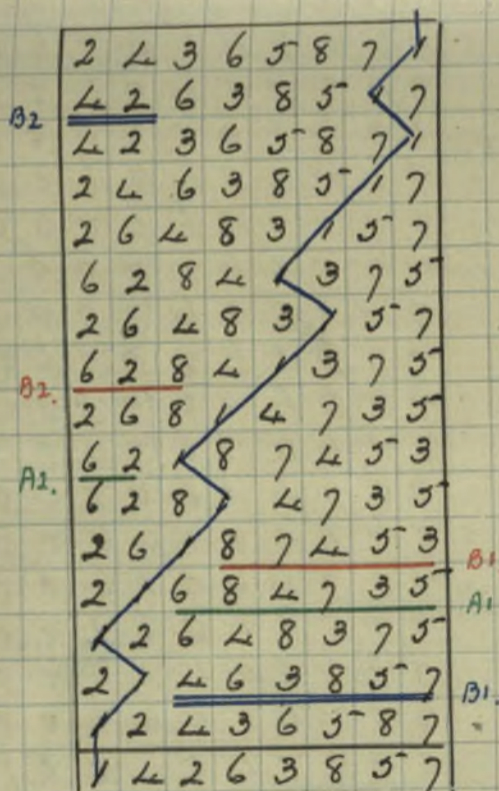
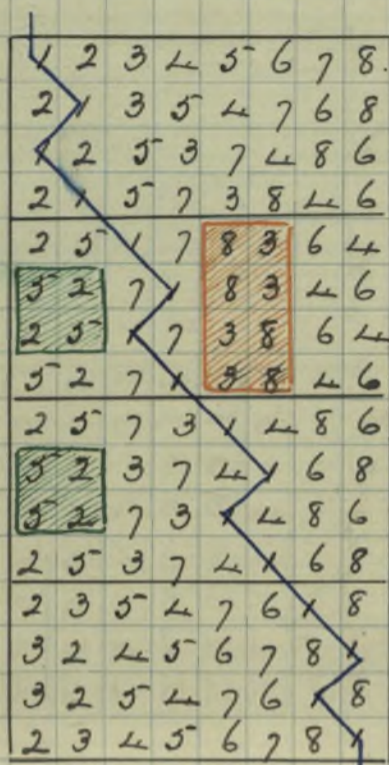
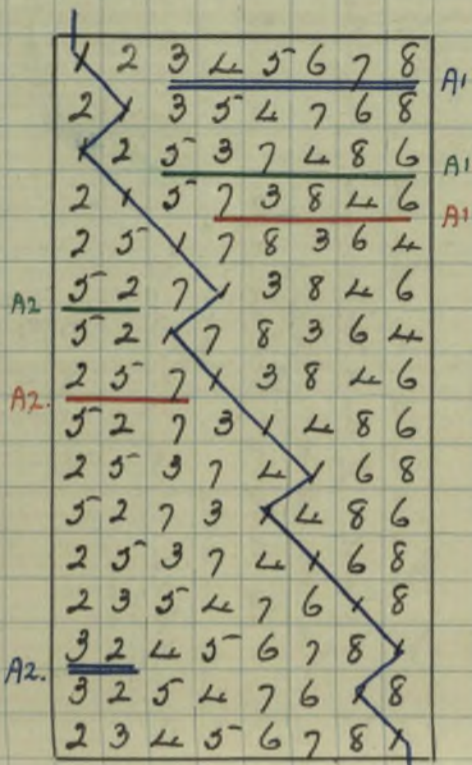
The following are Methods containing H.S. Court Shunts. -

T. B. PRINCIPLE.

TWO R. COURT SHUNTS

Two P do do

Two H.S. do do.



	1	2	3	4	5	6	7	8	9	0		
	2	1	3	5	4	7	6	9	8	0	A1	
	1	2	5	3	7	4	9	6	0	8	A1	
	2	1	5	7	3	9	4	0	6	8	A1	
	2	5	1	7	9	3	0	4	8	6	B1	
A2	5	2	7	1	9	0	3	8	4	6		
	5	2	7	1	9	0	9	8	3	6	4	B1
A2	2	5	7	1	0	8	9	6	3	4	B1	
B2	5	2	7	0	1	8	6	9	4	3		
	5	7	2	0	8	1	9	6	3	4		
B2	7	5	0	2	1	8	6	9	4	3		
	7	0	5	2	1	8	1	9	6	3	4	
	0	7	2	6	8	9	1	3	6	4		
	7	0	5	2	9	8	3	1	4	6		
	7	5	0	2	8	9	1	3	6	4		
D2	5	7	2	0	9	8	3	1	4	6		
	5	2	7	0	9	3	8	4	1	6		
	2	5	0	7	3	9	8	4	6	1		
B2	5	2	7	0	9	3	4	8	1	6		
Ex.	5	7	2	0	3	9	8	4	6	1		

	1	2	3	4	5	6	7	8	9	0	
	2	1	3	4	6	5	7	9	8	0	A2
	1	2	4	3	5	6	9	7	0	8	
	2	1	4	3	6	5	7	9	8	0	
	2	4	1	6	3	7	5	8	9	0	
	4	2	6	1	7	3	8	5	0	9	
	2	4	6	1	7	3	8	0	5	9	
	4	2	6	1	7	3	8	0	5	9	A1
	4	6	2	7	1	3	8	0	5	9	
	6	4	7	2	3	1	8	5	0	9	
	4	6	2	7	1	3	5	8	9	0	A1
A2	6	4	7	2	3	1	5	9	8	0	B1
	4	6	2	7	3	5	1	9	0	8	
A2	4	2	6	3	7	5	9	1	8	0	
	2	4	3	6	5	7	1	9	0	8	
A1	2	3	4	5	6	7	9	1	8	0	
B1	3	2	5	4	7	6	9	8	1	0	
	2	3	5	4	6	7	8	9	0	1	
	3	2	4	5	7	6	9	8	1	0	
	2	3	4	5	6	7	8	9	0	1	

	7	5	0	2	9	3	4	8	6	
C2	7	0	5	2	3	9	8	4	1	6
	0	7	2	5	9	3	4	8	6	
A2	7	0	5	2	3	9	4	8	6	
	7	5	0	2	3	4	9	1	8	6
	5	7	2	0	4	3	9	6	8	
	5	2	7	0	3	4	9	1	8	6
	3	5	0	1	4	3	9	6	8	
C2	5	2	7	0	4	3	6	9	8	
	5	7	2	0	4	6	3	8	9	
C2	7	5	0	2	4	3	6	9	8	
	7	0	5	2	4	6	3	8	9	
D2	0	7	5	2	4	3	6	9	8	
	7	0	5	2	3	4	9	6	8	
D2	7	0	5	3	2	9	4	8	6	
	0	7	5	3	9	2	8	4	6	
	0	7	5	9	3	8	2	6	4	
	0	7	9	5	8	3	6	2	4	
	0	9	7	8	5	6	3	4	2	
	0	9	8	7	6	5	4	3	2	
	0	8	9	6	7	4	5	2	3	

	3	2	5	4	7	6	9	8	0	
	2	3	5	4	6	7	8	9	0	
	3	2	4	5	7	6	9	8	0	
	2	3	4	5	6	7	8	9	0	
C2	3	2	5	4	7	6	8	1	9	0
B1	3	5	2	7	4	6	1	8	0	9
	5	3	7	2	6	4	8	1	9	0
B2	5	9	3	6	2	4	1	8	0	9
D2	7	5	6	3	2	4	8	9	0	
	5	7	3	6	1	2	4	9	8	0
	7	5	6	3	2	1	9	4	0	8
	5	7	3	6	1	2	9	0	4	8
	5	3	7	1	6	2	0	9	8	4
	3	5	7	2	6	9	0	4	8	
	5	3	7	1	6	2	9	4	0	8
	3	5	7	2	6	4	9	8	0	
	3	5	2	7	4	6	8	9	0	
	3	5	2	4	7	8	6	0	9	
	3	2	5	7	4	6	8	9	0	
	3	2	5	4	7	6	9	8	0	
B2	3	5	2	7	4	9	6	0	8	

B.S. Court Shunts are made in the changes of the Principle when the movement is backward. The first part of the Shunt consists of the Extreme Bells on one side of the Hunt, changing the backward movement for forward movement. To complete the Shunt the place making bell must cross the Hunt's path and join the rest of the Extreme Bells. These bells then make one step forward instead of one step backward.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	6	3	8	5	7
2	1	6	4	8	3	7	5
2	6	1	8	4	7	3	5
6	2	8	1	7	4	5	3
2	6	1	8	7	5	4	3
6	2	8	1	5	7	3	4
6	8	2	5	1	3	7	4

B.S. Court Shunt. Incomplete

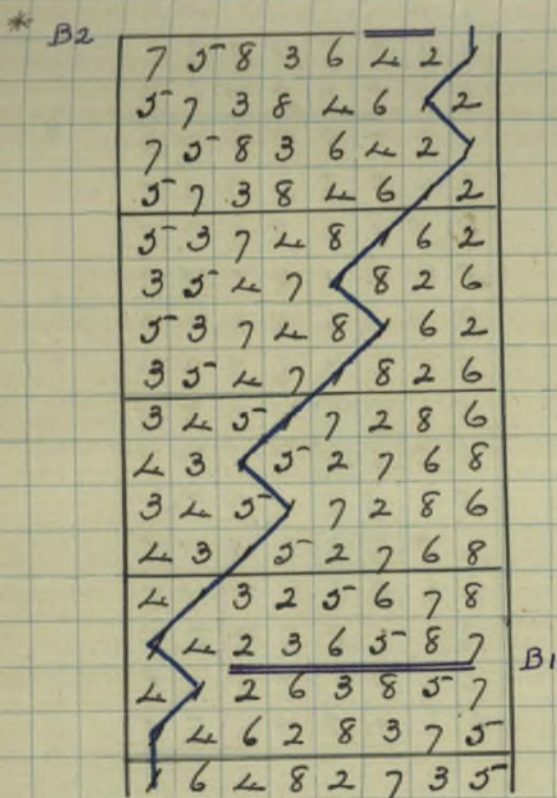
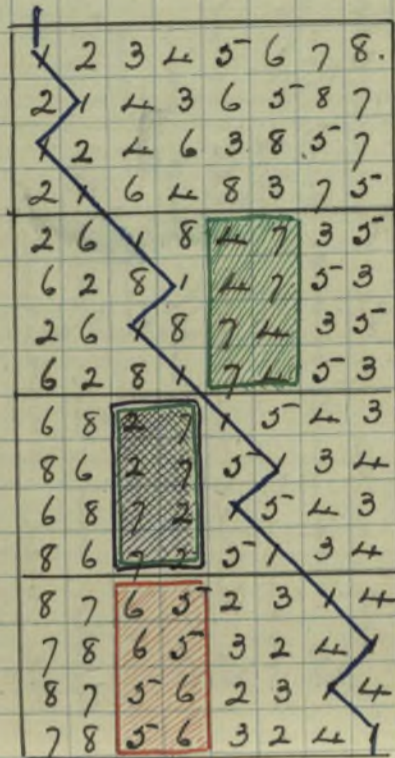
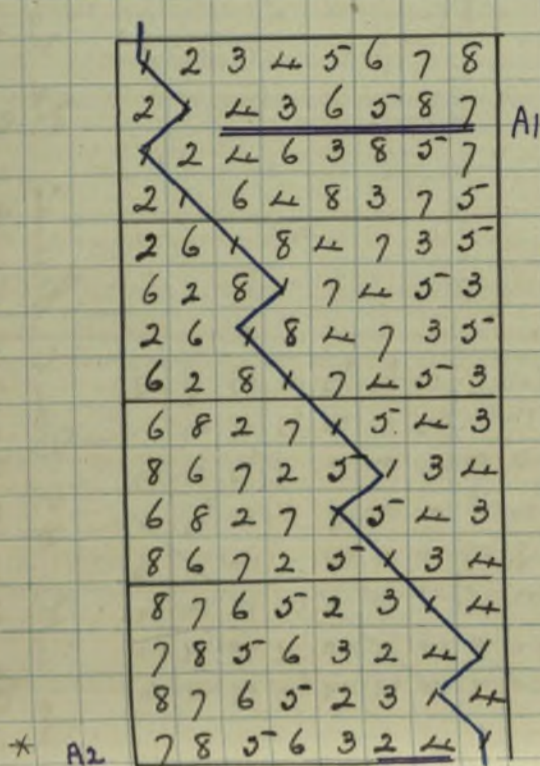
B.S. Court Shunt. Incomplete

As with H.S. Court Shunts the position of the second part of the B.S. Court Shunt depends on other Contradictional and Additional Shunts.

T.B. PRINCIPLE.

TWO B.S. COURT SHUNTS

SOHAM. T.B. MAJOR.



No Add!
Shunt here
ESP.

* Both Shunts A and B require movement on 2-4 and the double movements cancel each other.

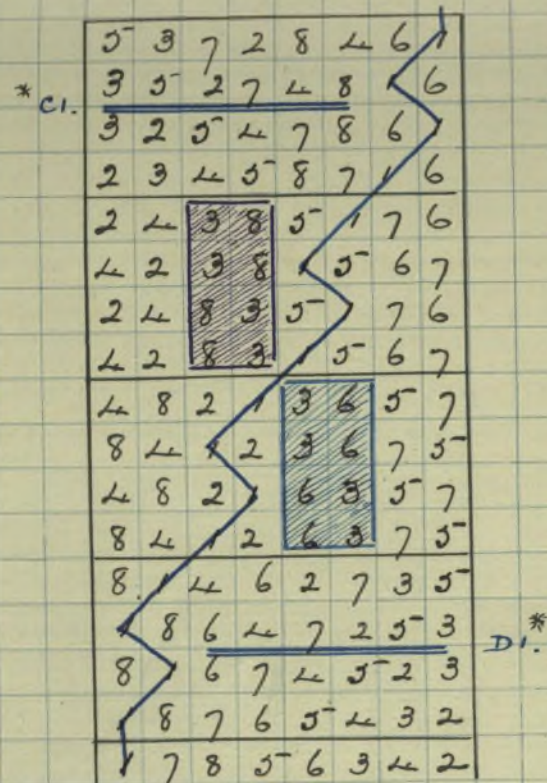
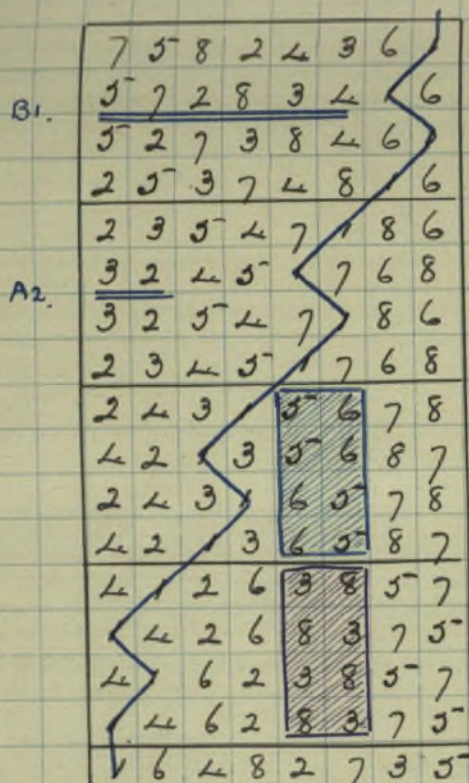
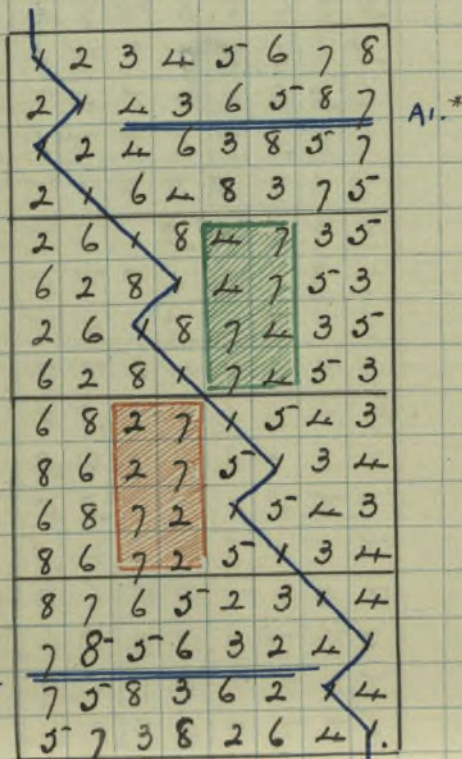
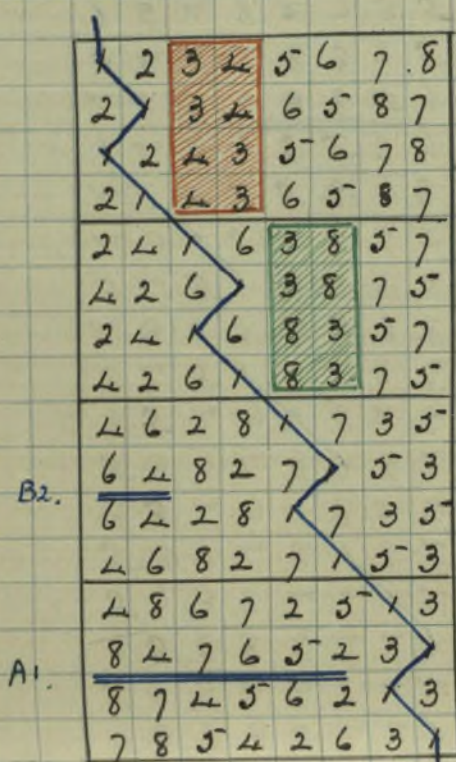
T. B. PRINCIPLE

TWO B-S COURT SHUNTS.

FOUR B-S COURT SHUNTS

WISBACH T.B. MAJOR.

SUTTERTON T.B. MAJOR.



* A1. and B2 each requires movement on 2-4 to complete the shunt. These cancel each other. Similarly C' and D' each requires movement on 8-6. These cancel each other.

2/4

H.S. Court Shuntis (being made when the movement of the Principle is forward) have the effect of changing the positions of the Hunt and the bell next before it in Coursing Order. The Hunt makes one step forward in its cyclical path through the Coursing Order of the Extreme Bells.

B.S. Court Shuntis (being made when the movement of the Principle is backward) have the effect of changing the positions of the Hunt and the bell next after it in Coursing Order. The Hunt makes one step backward in its cyclical path through the Coursing Order of the Extreme Bells.

B. Slow Work Shuntis As in the case of the Court Shuntis, the Treble Bell Principle admits of variations of the Slow Work Shuntis which will not run on the Plain Principle. The following are examples -

T. B. PRINCIPLE.

B. SLOW WORK SHUNT

BLÉCOURT. S. MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	6	5	8	7
2	4	1	3	5	6	7	8
4	2	3	1	6	5	8	7
2	4	3	6	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	3	1	8	5	7
6	4	3	2	8	1	7	5
4	6	3	8	2	7	1	5
6	4	8	3	7	2	5	1
6	8	4	3	2	7	1	5
8	6	3	4	7	2	5	1

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	6	5	7	8
2	1	4	3	5	6	8	7
2	4	1	3	6	5	7	8
4	2	3	1	5	6	8	7
2	4	1	3	5	6	7	8
4	2	3	1	6	5	8	7
2	4	3	6	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	3	1	8	5	7
6	4	3	2	8	1	7	5
4	6	3	8	2	7	1	5
6	4	8	3	7	2	5	1
6	8	4	3	2	7	1	5
8	6	3	4	7	2	5	1

6	8	3	7	4	5	2	1
8	6	7	3	5	4	1	2
8	7	6	3	4	5	2	1
7	8	3	6	5	4	1	2
8	7	3	5	6	1	4	2
7	8	5	3	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	3	1	8	2	6	4
5	7	3	1	2	8	4	6
7	5	3	1	8	2	6	4
5	7	1	3	2	8	4	6
5	1	7	3	8	2	6	4
5	3	7	1	2	8	4	6
5	1	7	3	8	2	6	4
1	3	5	2	7	4	8	6

6	8	3	7	4	5	2	1
8	6	7	3	5	4	1	2
8	7	6	3	4	5	2	1
7	8	3	6	5	4	1	2
8	7	3	5	6	1	4	2
7	8	5	3	1	6	2	4
7	5	8	3	6	1	4	2
5	7	3	8	1	6	2	4
7	5	3	1	8	2	6	4
5	7	3	1	2	8	4	6
7	5	3	1	2	8	6	4
5	7	1	3	8	2	4	6
5	1	7	3	2	8	6	4
5	3	7	1	8	2	4	6
5	1	7	3	8	2	6	4
1	3	5	2	7	4	8	6

T.B. PRINCIPLE

B. SLOW WORK SHUNT

EPINOY. MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	3	5	7
6	4	8	2	3	1	7	5
4	6	2	8	1	3	5	7
6	4	8	2	3	1	7	5
4	6	2	8	3	7	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	3	1	5
8	6	7	4	3	2	5	1

1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
1	2	3	4	5	6	7	8
2	1	3	4	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	3	5	7
6	4	8	2	3	1	7	5
4	6	2	8	1	3	5	7
6	4	8	2	3	1	7	5
4	6	2	8	3	7	1	5
6	4	8	2	7	3	5	1
6	8	4	7	2	3	1	5
8	6	7	4	3	2	5	1

6	8	4	7	5	2
8	6	7	4	5	3
8	7	6	5	4	3
7	8	5	6	3	4
8	7	6	5	3	4
7	8	5	6	3	4
8	7	6	5	3	4
7	8	5	6	3	4
7	5	8	1	6	4
5	7	8	3	6	2
7	5	8	6	3	4
5	7	8	3	6	2
5	7	3	8	2	6
5	3	7	2	8	4
5	7	3	8	2	6
5	3	7	2	8	4
1	3	5	2	7	4

6	8	4	7	3	5
8	6	7	4	5	3
8	7	6	5	4	3
7	8	5	6	3	4
8	7	6	5	3	4
7	8	5	6	3	4
8	7	6	5	3	4
7	8	5	6	3	4
7	5	8	6	3	4
5	7	8	6	3	2
7	5	8	3	6	4
5	7	8	3	6	2
5	7	3	8	2	6
5	3	7	2	8	4
5	7	3	8	2	6
5	3	7	2	8	4
1	3	5	2	7	4

1	2	3	4	5	6	7	8	9	0	A1 P.Count.
2	1	3	5	4	7	6	9	8	0	
1	2	5	3	7	4	9	6	0	8	
2	1	3	5	4	7	9	6	8	0	A1 R.Count.
2	3	1	5	7	4	6	9	0	8	
3	2	5	1	4	7	6	9	8	0	
2	3	1	5	7	4	9	6	0	8	B1 P.Count.
3	2	5	1	7	9	4	0	6	8	A2.
2	3	5	7	1	9	0	4	8	6	A2.
2	3	7	5	9	1	4	0	6	8	
3	2	5	7	1	9	0	4	8	6	B2.
3	5	2	7	9	1	4	0	6	8	
5	3	7	2	9	4	1	6	0	8	
3	5	2	7	4	9	6	1	8	0	
3	2	5	4	7	9	6	0	8		
2	3	4	5	9	7	6	1	8	0	
3	2	5	4	9	6	7	8	1	0	
2	3	4	5	6	9	8	7	0	1	
2	4	3	6	5	9	7	8	1	0	
4	2	6	3	9	5	8	7	0	1	

1	2	3	4	5	6	7	8	9	0	
2	1	3	6	5	7	9	8	0		
1	2	3	4	5	6	9	7	0	8	
2	1	4	3	6	5	9	0	7	8	A1
2	4	1	3	5	6	0	9	8	7	
4	2	3	1	6	5	0	8	9	7	
2	4	1	3	5	6	8	0	7	9	
4	2	3	1	6	5	8	7	0	9	
2	4	3	6	1	5	7	8	9	0	
2	4	6	3	5	1	8	7	0	9	
4	2	3	6	1	5	7	8	9	0	
4	2	6	3	5	1	8	7	0	9	
2	4	3	6	5	8	1	0	7	9	
4	2	6	3	8	5	0	1	9	7	
4	6	2	8	3	0	1	0	7	9	
6	4	8	2	3	3	0	1	9	7	
4	6	2	8	5	0	3	9	1	7	
6	4	8	2	0	3	9	3	7	1	
6	8	4	0	2	5	3	9	7		
8	6	0	4	5	2	9	3	7	1	

2	4	3	6	9	8	5	0	7		
4	2	6	3	8	9	0	5	7		
4	6	2	8	3	9	5	0	7	1	
6	4	8	2	9	3	0	5	7		
4	6	2	8	9	0	3	1	5	7	
6	4	8	2	0	9	1	3	7	5	
6	8	4	0	2	9	3	1	5	7	
8	6	0	4	9	2	1	3	7	5	
6	8	4	0	9	1	2	7	3	5	C2.
6	4	8	0	9	7	2	5	3		
4	6	0	8	9	1	2	7	3	5	D2.
4	6	8	0	9	7	2	5	3		B2.
6	4	8	0	9	2	7	3	5		
4	6	1	8	0	2	9	3	7	5	C1. P.Count.
6	4	8	1	2	0	3	9	5	7	
4	6	1	8	0	2	3	9	7	5	B1. R.Count.
4	6	8	2	0	9	3	5	7		
4	8	6	0	2	9	3	7	5		
4	6	8	2	0	3	9	5	7		D1. P.Count.
4	6	2	8	3	0	5	9	7		Extreme
4	2	6	3	8	5	0	7	9		

6	8	4	0	5	9	2	7	3		
8	6	0	4	9	5	7	2	3		
8	0	6	9	4	5	2	7	3		
0	8	9	6	3	4	7	2	3		
8	0	6	9	5	7	4	2	3		
0	8	9	6	7	0	1	3	2		
0	9	8	7	6	0	4	2	3		
9	0	7	8	5	6	1	4	3	2	
0	9	8	7	5	6	3	4	2		
0	9	7	8	0	5	3	6	2	4	
9	0	8	7	5	6	3	4	2		
9	0	7	8	5	6	3	4	2		
0	9	7	1	8	5	6	3	4	2	
9	0	7	5	8	6	4	3	2		
0	9	7	1	8	5	4	2	6	3	
9	0	7	5	8	4	2	6	3		B1
9	0	7	8	5	2	4	3	6		
9	7	0	5	8	2	3	4	6		
9	7	0	7	8	5	3	2	6	4	
9	7	0	5	8	3	6	2	4		
9	0	7	8	5	6	3	4	2		

The B Slow Work Bell is the Bell which in the Principle, is the bell immediately next before the treble in Coursing Order. This bell becomes a Skunt, and makes a cyclical path through the Coursing Order of the other bells; but it does not change positions in C.O. with the treble. The result is that the Coursing Order of the Principle is altered by the positions of the treble and Slow Work Bell being reversed. The treble makes one step forward in its cyclical path in Coursing Order.

If the Coursing Order of the bells is 5 3 1 2. etc, and 5 is made a B Slow Work bell (not completing its cyclical path so far as 1-2-3 are concerned), the Coursing Order will be altered to 3 1 2 5. A further Skunt on 3 2 5 will produce the Coursing Order 5 1 3 2. The whole operation produces one step forward in Coursing Order by the treble; and is therefore a Constructive Skunt.

We saw, in the case of the Slow Work Shunt, that the Plain or Treble Bob Path of the Treble may be the result of two movements one + and one -
 The following is a further Example of this. In it the movements are all completed within the Lead and therefore take no part in the Constitutional Shunt.

A. is a Block produced by Hunt and Extreme Bells. 4-5 are the Hunt 1-2-3-6-7-8 are the Extreme Bells.*

B. is the same as A, with four Dodging movements inserted to give the Treble an unbroken Treble Bob Path.

C. is the same as B, with the addition of (a) Four Additional Shunts

5 3 8 7	instead	5 3 8 7	and
3 5 7 8		5 8 3 7	three
5 3 8 7	?	8 5 7 3	others
5 8 3 7		5 8 3 7	similar

(b) One Additional Shunt on 4-5.

E. is C with two Extremes added.

* See page 134.

Dir C

A.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	6	3	5	7	8
2	1	6	4	5	3	8	7
2	6	1	4	5	8	3	7
6	2	4	1	8	5	7	3
2	6	4	8	1	5	3	7
6	2	8	4	5	1	7	3
6	8	2	4	5	7	1	3
8	6	4	2	7	5	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	4	5	3	2	1

B

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	6	3	5	7	8
2	1	6	4	5	3	8	7
2	6	1	4	5	8	3	7
6	2	4	1	8	5	7	3
2	6	4	8	1	5	3	7
6	2	4	1	8	5	7	3
2	6	4	8	1	5	3	7
6	2	8	4	5	1	7	3
2	6	4	8	1	5	3	7
6	2	8	4	5	1	7	3
6	8	2	4	5	7	1	3
8	6	4	2	7	5	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	4	5	3	2	1

C.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	6	3	5	7	8
2	1	6	4	5	3	8	7
2	6	1	4	5	8	3	7
6	2	4	1	8	5	7	3
2	6	4	8	1	5	3	7
6	2	4	1	8	5	7	3
2	6	4	8	1	5	3	7
6	2	8	4	5	1	7	3
6	8	2	4	1	5	3	7
8	6	4	2	5	1	7	3
6	8	2	4	5	7	1	3
8	6	4	2	7	5	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	4	5	3	2	1

D

SUPERLATIVE. S MAJOR.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
1	2	4	6	3	5	7	8
2	1	6	4	5	3	8	7
2	6	1	4	3	5	7	8
6	2	4	1	5	3	8	7
2	6	4	8	1	5	3	7
6	2	4	1	8	5	7	3
2	6	4	8	1	5	3	7
6	2	8	4	5	1	7	3
6	8	2	4	1	5	3	7
8	6	4	2	5	1	7	3
6	8	2	4	5	7	1	3
8	6	4	2	7	5	3	1
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
6	8	4	7	2	5	3	1

Two points must be noted about all Shuntis

1. It is not possible to tell from one Change alone to what Shunt or kind of Shunt the movement in that Change belongs

1	2	3	4	5	6	7	8
2	3	5	4	7	6	8	
2	5	3	7	4	8	6	
2	5	7	3	8	4	6	

The movement in the first Change may be part of a Round Block on 345678. It may be part of a H.S. Court Shunt; or it may be part of a Combination of additional Shunts. It is only when we discover how the cycle (or cycles) is completed that we can state the constitutional value of the movement.

2. Two or more different sets of cyclical movement may produce the same Rows.

In certain cases a Slow Work Shunt produces the same Rows as an Extreme, as for instance a 6 BELL Slow Work Shunt

When there are seven Extreme Rells. The
Constructions however are really distinct
and not merely two names for the
same thing.

Chapter XI

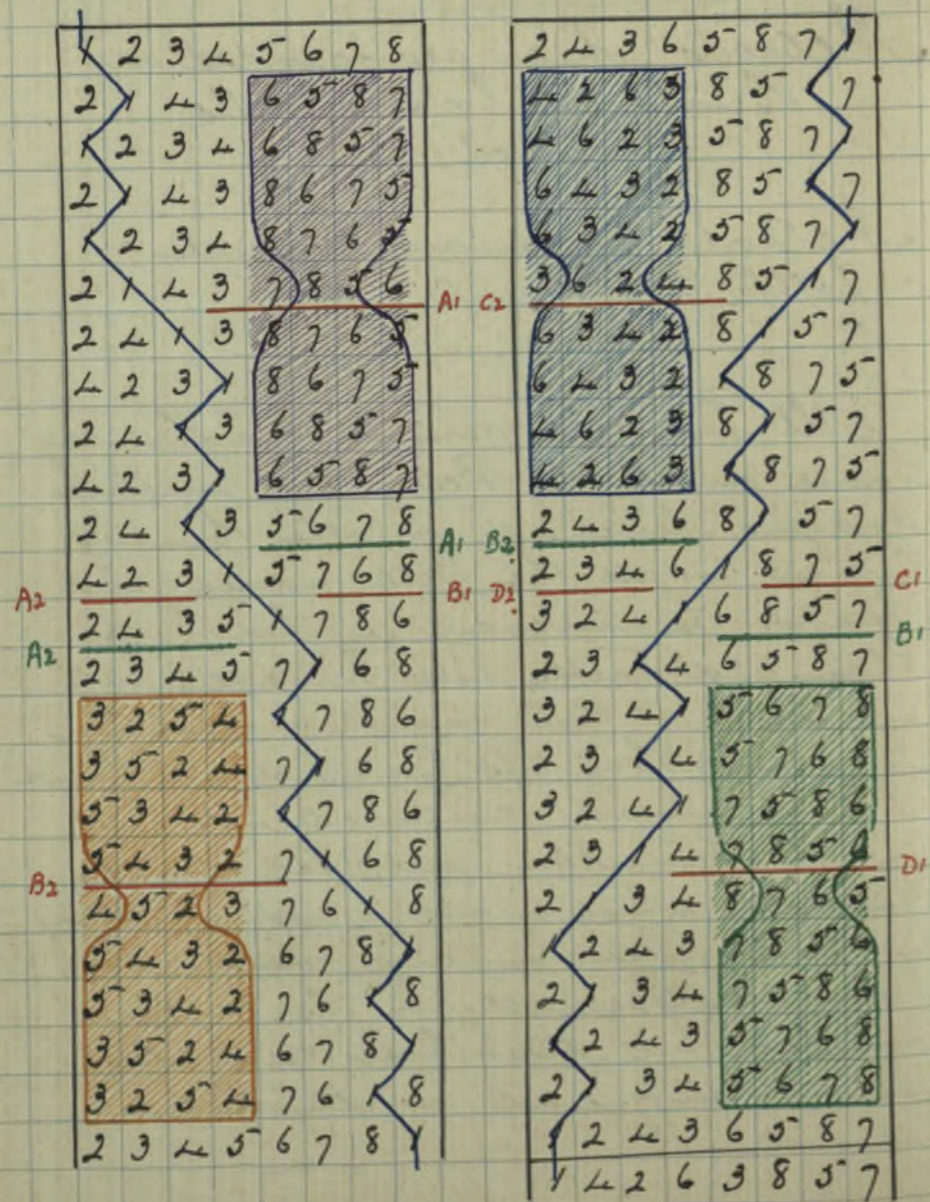
Methods which are founded on
Hunts and Extreme Bells.
(continued)

Methods on various Principles;
Little Bob Hunts; etc.

All Principles consist of a Hunting
Course on all the Bells, with sometimes
Dodging Movements or other Hunting
Courses on all the Bells added, and
therefore the movement is that of the
Plain and Treble Bob Principles, with
a greater or less amount of repetition.
It follows that the Constitutional Hunts
I have already explained will run
on all Principles and that none is
possible which is not a reduplication
of those. An immense variety is
possible especially on the higher
numbers, but five or three examples
will be sufficient as illustrations.

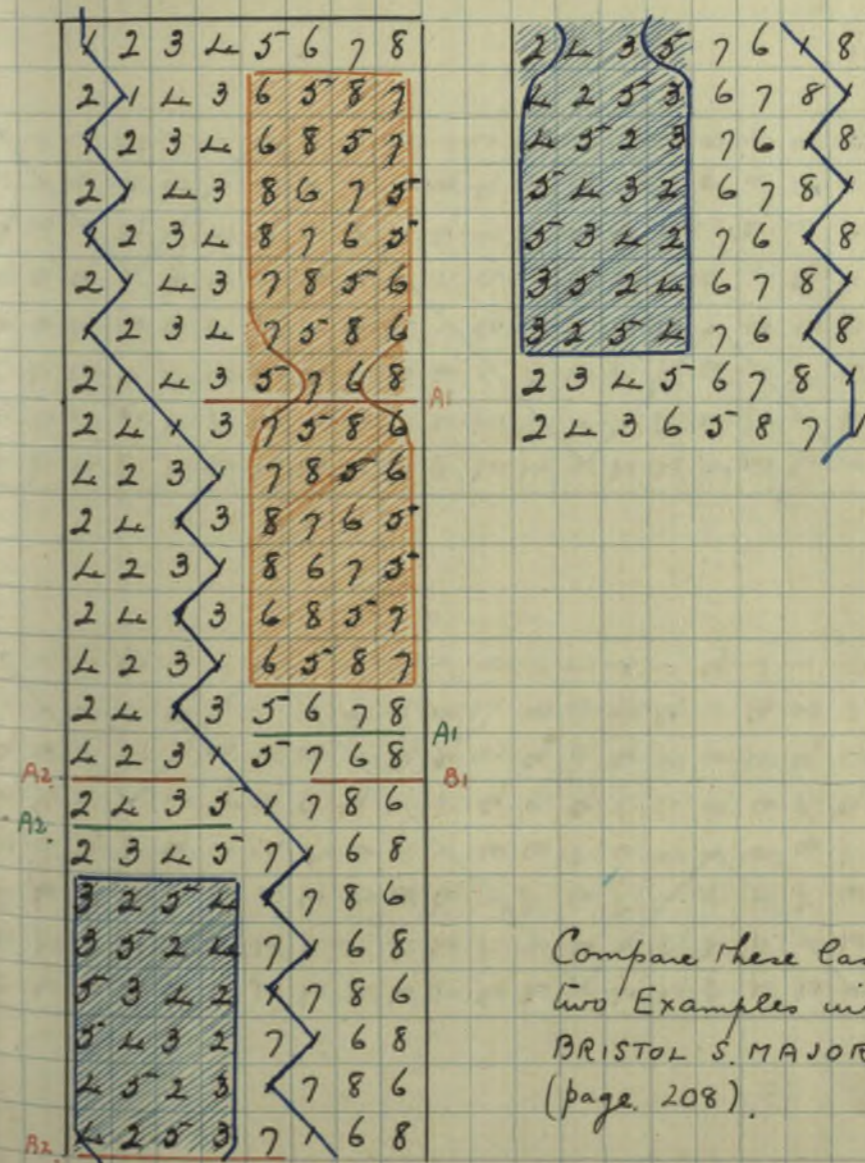
DOUBLE DODGING PRINCIPLE.

FOUR R. COURT. TWO P. COURT CONSTRUCTIONAL SHUNTS.



TRIPLE DODGING PRINCIPLE.

FOUR R. COURT TWO P. COURT CONSTRUCTIONAL SHUNTS.

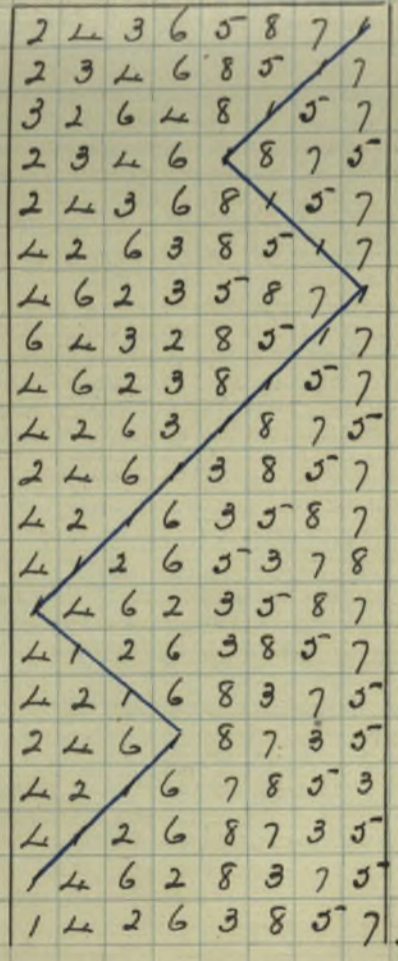
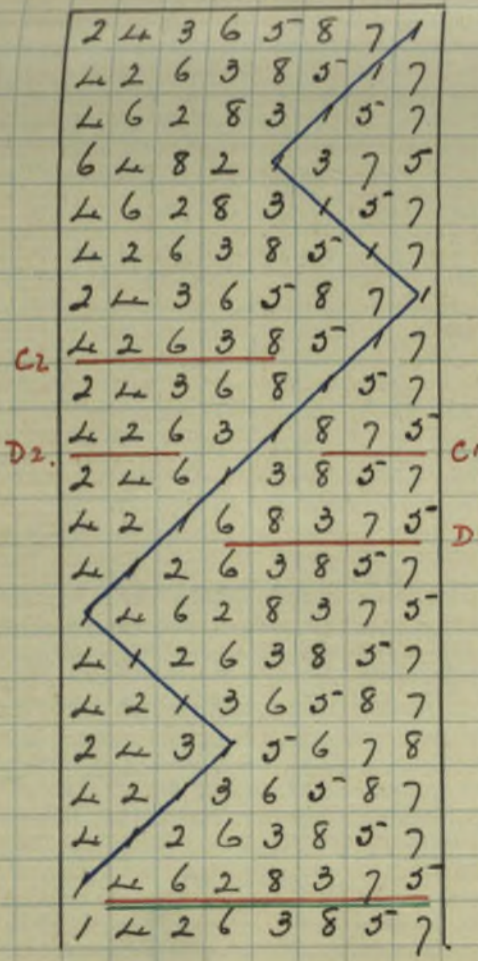
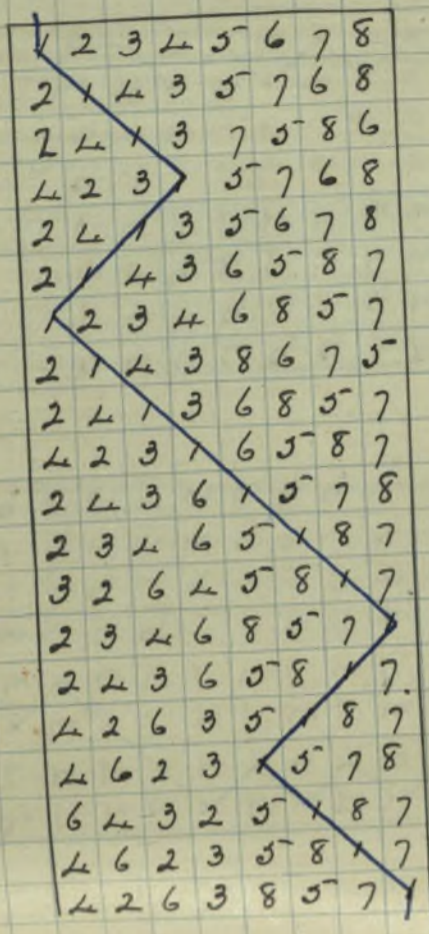
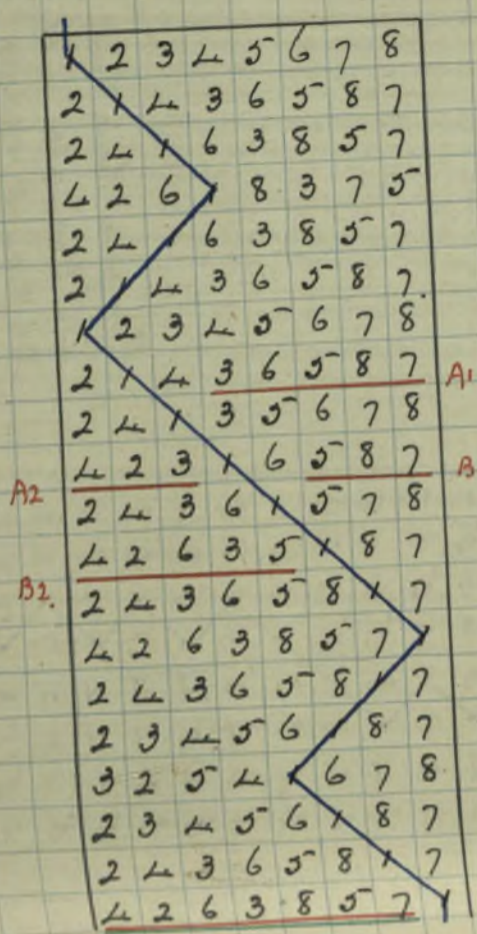


Compare these last two Examples with BRISTOL S. MAJOR (page 208).

GIANT HUNT PRINCIPLE.

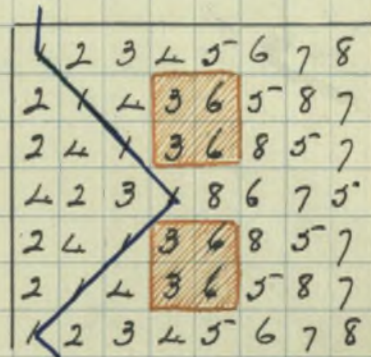
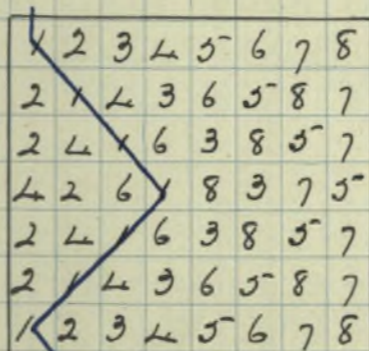
4 R. COURT 2. EXTREME SHUNTS.

NORTHALLERTON. MAJOR.

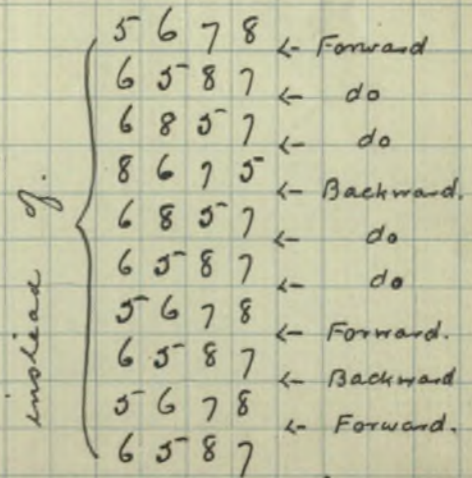
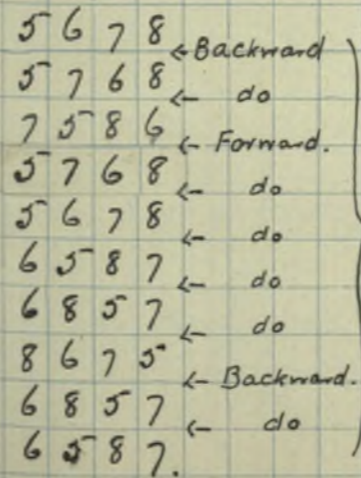


The Additional Stunts of NORTHALLERTON MAJOR. are.

1. a 2 BELL Stunt on 3-6.



2. The five steps of forward movement and four steps of backward movement of 5-6-7-8 are arranged in a different order.

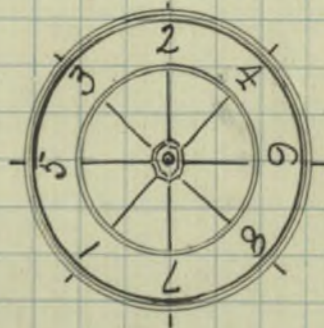
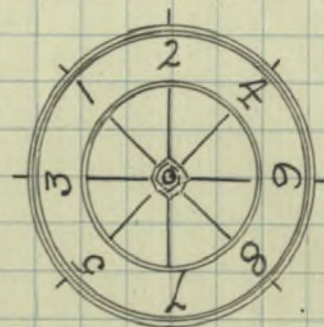


involved

The Little Bob Skunts. If in any change of a Principle where the movement is forward, a number of the Bells make one step backward, a secondary cycle is begun, part of the Bells being Hunts and the rest Extreme Bells.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3

6	8	4	7	2	1	3	5
8	6	7	4	1	2	5	3
8	7	6	1	4	5	2	3
7	8	1	6	5	4	3	2
7	1	8	5	6	3	4	2
1	7	5	8	3	6	2	4



In this example 24687 are Hunts and 135 Extreme Bells. The Coursing Order of the Extreme Bells is (5) 1, 3 and

The result of the shunt is that the Horns are put one position forward in Counting Order. from between 1 and 5 to between 3 and 1. I.E. 1 and the Horns 2-4-6-8-7 have changed positions in Counting Order.

The movement thus begun could be completed by the Horns finishing their Cyclical path and changing positions with 1, 3 and 5 in turn.

But there is an alternative way of considering this shunt. 1 has changed positions with 2-4-6-8-7; it has therefore made five steps in a cyclical path and, if it completes the cycle, the bells will return to the Row from which they started.

The cycle may be completed by other similar shunts, or by a combination of these shunts and other Constitutional shunts.

The Little Bob Shunt consists of the Horn (or Horns) making a Place in its upward path and returning to the Lead without going behind. The result is that it is put backward in Counting Order as many positions

as there are bells below it when it makes the Place.

The Row Bell in Oxford and Kent is a form of this Hunt; which gives one more illustration of the fact that all these Constructional Hunts are essentially the same in nature, and differ only in the circumstances in which they are made.

The following Block gives examples of Little Bob Hunts. In three cases the Hunt is full backward in Coursing Order five positions; in two cases the Hunt is full backward three positions in Coursing Order.

$$(3 \times 5) + (3 \times 2) = 21.$$

21 is a multiple of 7, the number of Extreme Bells; and therefore the Hunt completes its cyclical path in Coursing Order; the original Coursing Order of all the bells is regained; and the bells return to the Row from which they started.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	1	3	5
8	6	7	4	1	2	5	3
8	7	6	1	4	5	2	3
7	8	1	6	5	4	3	2
7	1	8	5	6	3	4	2
1	7	5	8	3	6	2	4
1	5	7	3	8	2	6	4
5	1	3	7	2	8	4	6
5	3	1	2	7	4	8	6
3	5	2	1	4	7	6	8
3	2	5	1	7	4	8	6
2	3	1	5	4	7	6	8
2	1	3	4	5	6	7	8
1	2	4	3	6	5	8	7
1	4	2	6	3	8	5	7
4	1	6	2	8	3	7	5
4	6	1	8	2	7	3	5
6	4	8	1	7	2	5	3
6	8	4	7	1	5	2	3
8	6	7	4	5	1	3	2

3 1 2 4 6 8 7 5

← The Hunt is put 5 positions backward in Co.

3 2 4 6 8 7 1 5

← The Hunt is put 3 positions backward in Co.

3 2 1 4 6 8 7 5

8	7	6	5	4	1	2	3
7	8	5	6	1	4	3	2
7	5	8	1	6	3	4	2
5	7	1	8	3	6	2	4
5	1	7	3	8	2	6	4
1	5	3	7	2	8	4	6
1	3	5	2	7	4	8	6
3	1	2	5	4	7	6	8
3	2	1	4	5	6	7	8
2	3	4	1	6	5	8	7
2	4	3	6	1	8	5	7
4	2	6	3	8	1	7	5
4	6	2	8	3	1	5	7
6	4	8	2	1	3	7	5
6	8	4	1	2	7	3	5
8	6	1	4	7	2	5	3
8	6	7	4	5	2	3	1
1	8	7	6	5	4	3	2
1	7	8	5	6	3	4	2
7	1	5	8	3	6	2	4
7	5	1	3	8	2	6	4
5	7	3	1	2	8	4	6
5	3	7	1	8	2	6	4
3	5	1	7	2	8	4	6
3	1	5	2	7	4	8	6
1	3	2	5	4	7	6	8
1	2	3	4	5	6	7	8

← The Hunt is put 5 positions backward in Co.

3 2 4 6 8 7 5 1

← The Hunt is put 5 positions backward in Co.

3 2 4 6 8 1 7 5

← The Hunt is put 3 positions backward in Co.

A similar result is got if the Hunt makes a Place in its downward path and returns to behind without going to the front.

1	2	3	4	5	6	7	8
2	1	4	3	6	5	8	7
2	4	1	6	3	8	5	7
4	2	6	1	8	3	7	5
4	6	2	8	1	7	3	5
6	4	8	2	7	1	5	3
6	8	4	7	2	5	1	3
8	6	7	4	5	2	3	1
8	7	6	5	4	3	2	1
7	8	5	6	3	4	1	2
7	5	8	3	6	1	4	2
5	7	3	8	6	2	4	1
7	5	8	3	1	2	6	4
5	7	3	8	2	1	4	6
5	3	7	2	8	4	1	6
3	5	2	7	4	8	6	1
3	2	5	4	7	6	8	1
2	3	4	5	6	7	8	1
2	4	3	6	5	7	8	1

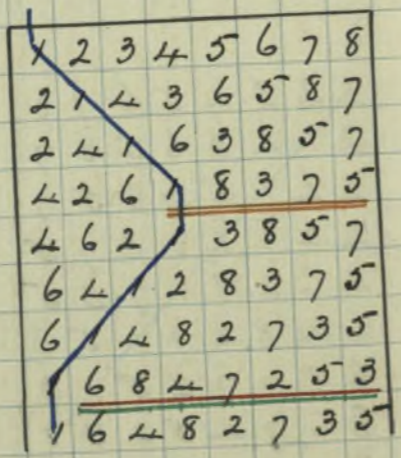
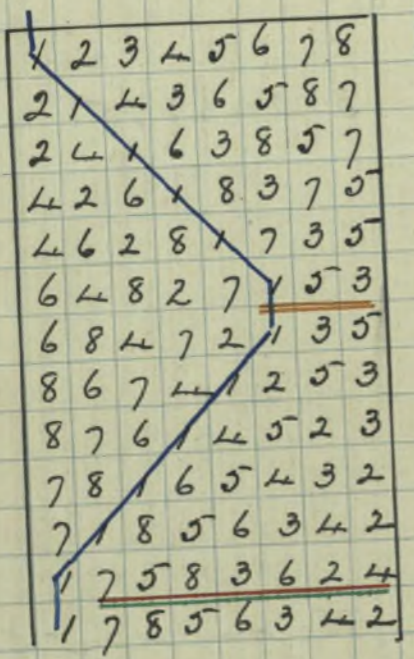
3 1 2 4 6 8 7 5.

← The Hunt is put 3 positions backward in Coursing Order.

3 2 4 6 1 8 7 5.

PLAIN PRINCIPLE.

LITTLE BOB SHUNT AND EXTREME



PLAIN PRINCIPLE

T.B. PRINCIPLE.

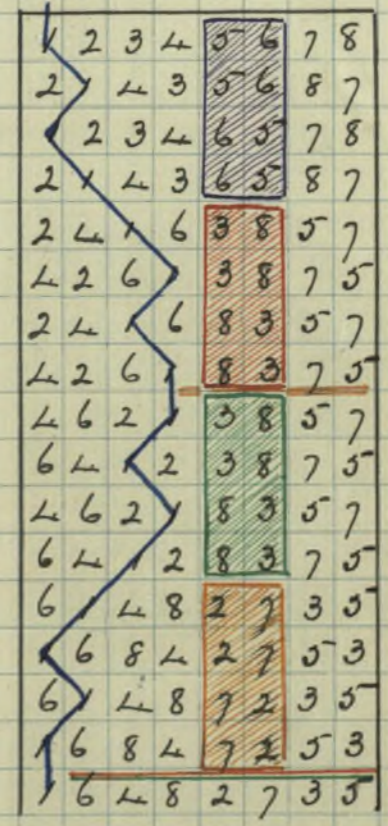
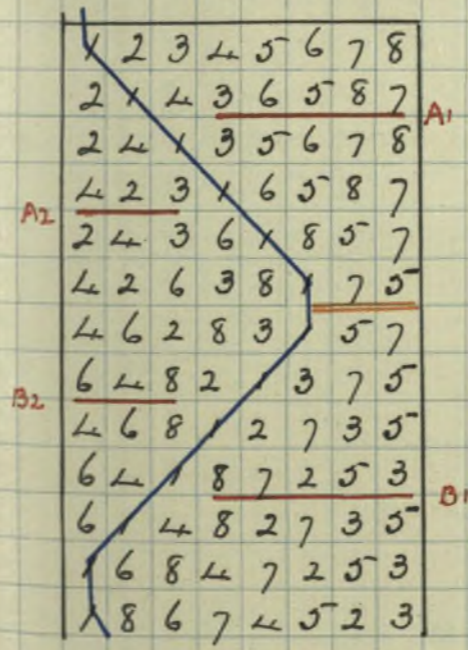
LITTLE BOB SHUNT

LITTLE BOB SHUNT.

TWO R. COURT SHUNTS.

EXTREME

2-BELL ADDITIONAL SHUNTS.



2 3 4 5 6 7 8
 3 2 5 4 7 6 8
 3 5 2 7 4 8 6
 5 3 7 2 8 4 6
 5 7 3 8 2 6 4
 7 5 8 3 6 2 4
 7 8 5 6 3 4 2

B

8 7 6 5 4 3 2
 7 8 6 4 5 2 3
 8 7 4 6 2 5 3
 8 4 7 2 6 3 5
 4 8 2 7 3 6 5
 4 2 8 3 7 5 6
 2 4 3 8 5 7 6
 2 3 4 5 8 6 7
 3 2 5 4 6 8 7
 3 5 2 7 4 7 8

W

5 3 6 2 7 4 8
 3 5 6 7 2 8 4
 5 3 7 6 8 2 4
 5 7 3 8 6 4 2
 7 5 8 3 4 6 2
 7 8 5 4 3 2 6
 8 7 4 5 2 3 6
 8 4 7 2 5 6 3

M.

4 8 2 7 6 5 3
 4 2 8 6 7 3 5
 2 4 6 8 3 7 5
 4 2 6 3 8 5 7
 2 4 3 6 5 8 7
 2 3 4 5 6 7 8

Compare the work
 of the Sixth in the families
 Touch of Bob Major
 (B.W.M.) with the
 Hunt in a Little Bob
 Skunt.

Also the work of the
 Second in M.B.W of
 Kent or London.

1	2	3	4	5	6
2	1	3	4	6	5
2	1	4	3	5	6
2	1	4	3	6	5
2	4	1	6	3	5
4	2	1	6	5	3
2	4	6	1	3	5
4	2	6	1	5	3
4	6	2	5	1	3
6	4	5	2	3	1
4	6	5	2	3	1
6	4	2	5	3	1
4	6	5	2	3	1
6	4	2	5	3	1
4	6	2	5	3	1
6	4	5	2	3	1
6	5	4	1	2	3
5	6	4	1	3	2
6	5	1	4	2	3
5	6	1	4	3	2
5	1	6	3	4	2
5	1	6	3	2	4
5	1	3	6	4	2
5	1	3	6	2	4
1	3	5	2	6	4

Ex.

In the case of ordinary Plain and Treble Bob Methods in which the Treble preserves its plain or dodging hunting uninterupted throughout, all Additional Shunts are made on the Extreme Bells only. Additional Shunts can be made so as to involve the field as well as the Extreme Bells.

The adjoining Example is on the Treble Bob Principle. The Constrictional Shunt is the Extreme when the field is behind.

There are also five Additional Shunts, each on five bells, in five of which the field is involved.

Similarly very many other Methods may be had with the field's path more or less irregular. All Group I Methods (see

Chapter VI can be turned into Group II Methods by making Constitutional Shunts; the Course in the first case becoming the Lead in the second case.

1	2	3	4	5	6
2	4	3	6	5	
2	4	6	3	5	
4	2	6	5	3	
4	1	2	5	6	3
1	4	5	2	3	6
1	5	4	3	2	6
5	1	3	4	6	2
5	3	6	4	2	
3	5	6	2	4	
3	1	5	2	6	4
1	3	2	5	4	6
1	3	5	2	6	4

It is possible by using Additional Shunts to put another bell temporarily into the position of the Horn.

So far as the main Constitution is concerned the work of the Horn will be done for the time by the Bell which is temporarily in its position.

Bobs and Singles, and all Special Calls are Shunts (similar in nature to Additional Shunts) which are begun in one Course and completed in one or more other Courses.

The sum of the whole matter is that every possible block of Rows on all

numbers of Bells must be, the result
of a number of distinct complete Cyclical
Movements.

Some of these Movements will be shared
in by all the Bells, and during them
the same Coursing Order is kept.

Others will be made by part of the
bells only, in which case we have the
Construction consisting of Hunts and
Extreme Bells.

Irregular Blocks, written down haphazardly
and without any apparent design, will
conform to this Law equally with those
divided into equal Leads and Courses.
The difference is merely a question
of the more or less symmetrical
Arrangement of the different Movements.

Since Ringing is essentially Movement
of the Bells to understand the Constructions
of any Method, or Peal, or Block, it
is necessary to find out the various
Cyclical Movements that produce that
Method, Peal, or Block.

The same Run may be produced by few
or more distinct combinations of Movements.

Chapter XII Standards of Excellence.

At the moment that Ringing began by "two bells removing into each others place," the Art was definitely fixed in its essential nature, in its scope, and in its limitations. It required only a process of evolution to produce everything it is capable of. No more rules and no imported "Conventions" are needed to give Change Ringing. The Cyclical movement, which is the result of this simple fundamental idea, implies and involves every essential rule except that of non-Repetition of Rows.

But ringers quickly found out that some methods of ringing are better than others. Better, that is, from the point of view of the ringers themselves. And so gradually, certain methods were marked out among the rest as those which are best suited for practical ringing. These Standard

Methods are the survival of the fittest, and are the result of a process that took quite a long time. This is not the place to find and trace why these methods should be esteemed more than others. The fact is so. And not only so, but the Exercise has increasingly confined itself to methods which share certain well defined characteristics of these Standard Methods. Thus, first the old Plain Changes were dropped, then such Cross Deals as did not divide into Leads and Courses, then such of the latter as did not still closely adhere to the standard.

The result is that there has grown up first a number of Rules which the general experience of the Exercise says should be observed in all methods that are practised; and second a number of standards which although not held ^{to be} absolutely essential to a method, are yet held to be the things that mark the best methods.

The Rules are as follows:-

1. In Group I Methods, the Plain

Course should be divided into as many Divisions as there are Bells; the work within the Divisions to be the same in each Case.

In Group II Methods, ^{the Plain Course} should be divided into as many Leads as there are Working Bells, the work in all the Leads to be exactly alike.

2. Each Division in Group I Methods to be symmetrical about a line drawn midway between Division Head and End.

Each Lead in Group II Methods to be symmetrical about a line drawn midway between Lead Head and Lead End.

3. No bell to lie more than five consecutive blows in any one position.

4. In any plain Course of Group II Methods, the Working Bells to be in the same Coursing Order at every Lead Head and End.

These are Rules which the general

Except that you may not have repetition of Rows. Even this applies, I think, only to Peals. Personally, I have no hesitation in calling false short punches

experience of the Exercise has adopted; but it is well that we should not misunderstand their value and position. They have not been imposed by any central authority, the Central Council for instance. They are not essentially restrictive rules, as so many of the rules of sport are. There is no analogy between them and, say, the rule in Cricket that the bowler may not throw. The reason for this latter is to preserve due balance between bowler and batsman, and the man who breaks it is guilty of unfairness. It is part of the competitive nature of sport. But Competition enters little into ringing as such, and we require no rules to regulate it. A band may break any of these Rules without any suspicion of unfairness or of doing anything which is not perfectly within their rights. As I have already said, there is no rule in Ringing which you may not freely break* if the result justifies it. But, and this is the whole point, the general experience of the Exercise warns you that, if you want to get the best out of ringing, you

⑤ The Law of Truth and all the important and interesting problems which belong to it lie outside the scope of this present enquiry.

Had better keep within them.

The one Rule which may be said to be restrictive and which may not in any case be broken is the Law of Truth.[Ⓢ]

None of these Rules is arbitrary or capricious. Each is based on an important truth which lies at the foundation of ringing. All have a definite constitutive value, and lay stress on some feature which men value in ringing.

I have already briefly noticed the Rules of Symmetry and Division into Leads.

The rule that a bell may not lie more than five consecutive blows in any one position is a practical recognition of the fact that movement is the one essential thing in ringing. We saw that in theory a bell may lie quite a large number of consecutive blows in any one position, and at the same time share movement equally with the rest of the bells. But this, though perfectly just, is just a little difficult to realise, and we can easily understand why in practical ringing the Exercise rejects it as

being contrary to the idea of movement. Some men have tried to justify this and other rules on musical grounds. I do not think that music has had very much to do with settling any of the main rules of ringing. In selecting touches and peals for performance, men no doubt, of later years, have been guided by musical considerations to a large extent. But if we investigate the things which have from the first, and always, made up the interest in ringing, I do not think we should find music very prominent among them.

The fourth rule is that which says that Methods should have what are commonly known as Bob Major Lead Ends. Nothing in theoretic ringing has been more hotly debated than this rule. Nothing has been more utterly misunderstood on both sides. It does indeed seem unreasonable and absurd, at first sight, to say that all Methods should have the same Lead Ends.

④ "BELL NEWS"

March. 1914.

* "Lead Ends" by REV. C. D. P. DAVIES MA. FRAS.
1918.

244.

Sir Arthur Heywood expressed himself as "patiently amused at earnest endeavours to stamper composition into conformity with quite arbitrary and wholly questionably axiomatic rules." * Mr. C. D. P. Davies in addition to speeches at the Central Council and long articles in the Bell News has published a pamphlet to show that these Lead Ends are not only not superior but are even inferior to other Lead Ends.* And yet all the new methods of late years, and nearly all the methods from the beginning that have been rung, have these P.D. Major Lead Ends.

The above eminent gentlemen, and the majority of other people, have quite misunderstood what is the Constitutional value of Lead Ends. They assume that a Lead is a certain amount of work the total result of which is to produce the Lead End. If the Lead End will repeat the required number of times you have a Course. If not, you have not a Course. Everything depends on

whether the Lead End will repeat the required number of times, and therefore any Lead End that will do so is of equal value.

But we have seen that the number of Leads in a Course does not depend in any way on the particular Lead End. It depends entirely on the number of steps made by the Hunt in its Cyclical path through the Coursing Order of the Extreme Bells. The Lead Ends need not be in a progression at all, though if every Lead is alike they will be so. Only Constitutional Shunts (i.e. the Hunt's Cyclical path in Coursing Order) have to do with the number of Leads and the length of the Course. Additional Shunts do not affect those things. But Constitutional Shunts leave the Extreme Bell in the same Coursing Order and therefore produce Bob Major Lead Ends. If an Additional Shunt is made partly in one Lead and partly in another, the Bob Major Lead Ends are hidden, but they remain the

"natural" Lead Ends of all Methods.
 It does not seem at all clear why
 Additional Stunts should always
 be made entirely within a Lead, and
 why the natural Lead Ends should
 not be hidden. But the general
 Experience of the Exercise is pretty
 definite on the point, and we have
 here a real practical, if unconscious,
 recognition of the fact that all
 Construction consists of the Cyclical
 path of Stunts, which keep their own
 Coursing Order, through Extreme Bells
 which keep their own Coursing Order.

Some men hold the opinion that it
 should be a Rule that only those
 Methods are legitimate which have the
 minimum number of Places and consequently
 the regular succession of the nature
 of the Rows (odd and even). There is
 a good deal to be said for this opinion
 but directly we hang it to the only
 really important test, it is shown
 to be fallacious. Does the general
 experience of the Exercise show that
 such a Rule would be good or bad

in working? There is no doubt what
 ever of the answer. Kent, Cambridge,
 London, and Bristol break the Rule,
 and the Exercise cannot afford to
 lose them, or to have a Rule which
 joss of the ten Standard Methods
 sets at naught. Some men would
 make this Rule operative for odd
 bell methods only, mainly because
 we call them Doubles, Triples, Caters,
 and Cinques. You can't have a
 Triples Method, they say, unless your
 Changes are all triple changes.
 This does not seem a very convincing
 argument. It makes the name of
 the thing more important than the
 thing itself. At the same time
 the Exercise has never taken kindly
 to any odd bell method which
 breaks this Rule.

There are other Standards by which
 men judge methods, many of them
 important, all of them interesting, but
 they need not detain us here, since
 our object is not to show what is
 a good method, but to explain the

Laws of Construction of all Methods.

These Rules and Standards are important and have value but their value is ^{not} entirely selective. They have nothing to do with the construction of methods; they differentiate between methods of different values from a practical point of view.

Chapter XIII
The Extension of Methods

Of all outstanding problems of the Science of Ringing none has aroused greater interest than that of Extension. The Exercise has made up its mind definitely as to what are the correct extensions of many of the methods in general use, but the correct ten and twelve bell variations of such methods as London, and Bristol, Surprise Major, and indeed whether such variations are possible, are still an open question. Double Norwich and Superlative Major have traditional extensions, but they are not accepted as correct by all. Many men, most of them of ability and knowledge, have set themselves to supply these extensions, but it is remarkable and significant that, though each man backs his version with copious argument, the results are almost always different. And, as they all work on pretty much the

same lines, we shall not be far wrong if we come to the conclusion that the problem of Extension as a whole has not properly been understood.

Ringers found no difficulty in getting the correct extensions of the early simple methods. Given Plain Bob Minor, Plain Bob Major, Royal and Maschiusus are quite obvious. So too are Plain Bob Triples, Gates, and Cinques. Grandone, Kent, Oxford, and Stedman extend equally easily. No detailed arguments are necessary to show that these extensions are correct; they pass the only really vital test—the experience of the ringer in the tower.

In addition to the above there are a few other methods the correct extensions of which are not in dispute. These are Original, Duffield, Forward, Double Oxford, and Cambridge Surprise, and the whole serve as models of what a correct extension should be. Men do not fully recognize this, but, unfortunately, directly you come to methods outside this group, you have no longer any

obvious and unmistakable extensions, even in cases where the construction of the method is quite simple and obvious.

Double Count Minor is almost as simple in construction as Plain Bob Minor, and quite as simple as Kent Treble Bob Minor. In early days it was one of the most popular ring bell methods.

Naturally ringers tried to extend it to eight bells, but almost every band which rang Count Bob Major rang a different version. There were rung in at least three quite distinct methods and each was rung as simply Count Bob Major. Two of these methods became popular, and the Exercise avoided confusion by treating them, not as extensions, but as fresh and distinct methods and calling them after the places where they were first practised - Norwich Count Bob and London Count Bob.*

Interest in Extensions seems then to have died out. The Exercise had quite as many methods as it had any practical use for, and the general opinion grew up that outside the

* See The Clavis

* Duffied. Sir A. P. Heywood. p. 5.

group of methods I have mentioned, there can be no such thing as real Extension. This was probably the opinion of the Exercise for a hundred and fifty years down to the end of the nineteenth Century.*

Two notable exceptions there were. The one really original contribution that Shipway made to the science of ringing, was to show the relationships between different variations of a method. He gave the Single, Double, and Reverse variations of most of the methods then in use. He showed how any even bell method on the Plain Principle can be turned into an odd bell method by adding a bell in the Hunt. And in the Cases of Double Oxford and Superlative he attempted a fine extension of a method on 6, 8 and 10 bells. Unlike other men, his work was not experimental. He worked on a general principle and his conclusions are thoroughly sound.

In the North a band discovered that an apparently complex method like Cambridge shall extend as readily

as Plain Ps. or Kent. Whether as the result of experiment, or of logical deduction, there is no means of knowing.

Neither of these cases had any effect on the general opinion of the Exercise. The figures of the Cambridge Royal were not published in any ringing book and were virtually lost. And the Exercise did not grasp or understand Shipways investigations.

This was the state of opinion in the closing years of the nineteenth Century when the advance of practical ringing proved a keen interest in Method Constitution. New methods were produced on all hands, and the question of Extension became again a live one. Even then it was felt that Composers showed far more zeal than knowledge, and the real idea at the bottom of the appointment of the Method Committee was an attempt to devise some means of curbing their exuberance.

Why men should try and get extensions of popular methods is easily understood. There is a prestige belonging to a method like London Surprise, which no new

one can ever possess. Every one would admit that a peal of London Surprise Royal is an outstanding performance. A peal in the same method under another name would pass almost unnoticed.

But in trying to produce these Extensions Composers had little knowledge to guide them. They had the simple methods as models, but they did little more than show, apparently, that extension of a complex method like London, or Superlative, or Bristol is a different thing altogether to extension of Plain Bob or Redman or Kent. Composers were therefore reduced to working by experiment. They took an eight bell method, analysed it, found what they considered its important features, and then tried to reproduce them as nearly as possible on ten bells. Of course they were prepared to justify their results by much argument. They could give abundant reasons for everything in their extensions. But it is quite fair, I think, to say that in all cases.

The figures were got first, and the arguments afterwards.

The proof of a pudding is in the eating. Not only has the experimental method of working failed to show how methods as a whole extend; it has utterly failed to produce one undisputed extension of any single method. In the case of London, each Composer who has tried to extend the method, has produced a different version, most of them have produced more than one. And each version has in its turn been given to us as the one and only correct London Surplice Royal.

The experimental method of working stands then condemned, and we must find out some general law based on the essential nature of all ringing, and therefore applicable to all methods, or failing this, we must come to the conclusion that, outside the few methods I have mentioned, there is no such thing at all as Extension.

Inside the Methods Committee one or two attempts were made to find such a law. The attempts failed because they were based on the assumption

That Places are the important things in Method Construction, and that all else depends on them. Thus, we argued that Plain Bob Minor is produced from the Plain Principle by moving inward an External Place. Plain Bob Triples is produced by adding two fresh Places. Therefore, they are not the same method. But the general experience of the Exercise and the individual experience of all of us in the tower, is that they are the same method; and the one a true extension of the other. Places we saw are not the one essential thing in a method, and we must look elsewhere for the basis of our law.

I'm trying to settle the question of Extension, two questions must be answered at the outset -

1. What, exactly, is it that you are going to extend?
2. What, exactly, do you mean by extension.

1. What is a method? Probably no

term in ringing is, for all practical purposes, less ambiguous, or less liable to be misunderstood than the term Method. It hardly needs a definition. But when we come to a question like the one before us, we must have something much more definite and exact than will serve "for all practical purposes." A Method is not a collection of figures or symbols. It is not an arrangement of Places. It is not a collection of Rows. It is not a particular relationship between a number of Rows. It implies all these things, but essentially it is what its name states a "method of ringing Changes." It is so much work, so much hunting, dodging, and place making. It is so much movement of the bells. You may express this in mathematical or philosophical terms, but for all purposes of the science, as well as the art, of change ringing a Method is nothing else than so much movement. As I have pointed ringing is essentially movement, and movement which must be cyclical in

in form.

Therefore what you have to extend is, not a group of figures; not an arrangement of Places; not a collection of Rows; but a series of Cyclical movements.

And it can hardly be denied that if you can do this, you will have produced just what the practical ringer asks for.

2. What do you mean by Extension?

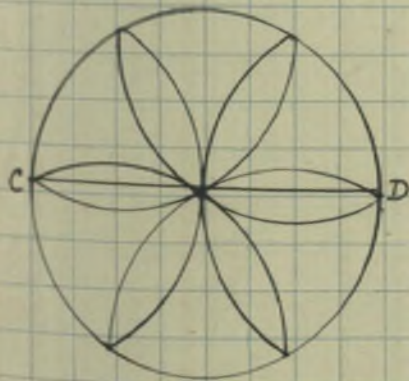
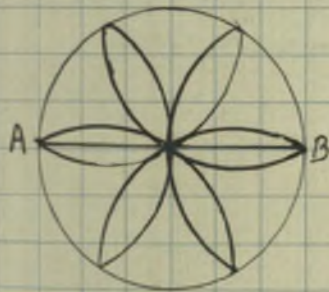
Most men answer this something in this way. In extending a method they say you take it on one number of bells and reproduce the same thing on a larger number. They assume that an extension differs from its original only in scale.

But this is what can never happen. You cannot ^{have} two Rows like 123456 and 12345678 as if they were two lines of different length. If you

have two lines AB and CD of different length; and if on

AB you erect any geometrical figure, you can project that figure on to CD. The figure on CD will be exactly similar

is that on A.B. except that it will be on a larger scale. But you



cannot do a similar thing with two Rows of unequal length. The reason is that a line is made up of an infinity of points, but a Row is made up of a definite number of Bells. Any line can be divided in any proportion, and therefore any two lines can be divided in the same proportion. But no two Rows of unequal length can ever be divided in exactly the same proportion. You

cannot divide a Row which has seven Extreme Bells in the same proportion you can a Row with five Extreme Bells. You could divide into two equal halves, both a row containing eight bells and one containing ten bells; but since the half of one contains an even number of bells, and the half of the other an

* i.e. The 3-Bell Work in the Front which
of course also includes the Quirk Bells

odd number of bells. The division is not
really proportional.

In Stedman Doubles the Slow Work*
occupies $\frac{3}{5}$ of the whole space; in
Stedman Triples it occupies $\frac{3}{7}$ ths; in
Stedman Cinques $\frac{3}{11}$ ths. The result
is, that the work of the bells differs
in many respects. In Doubles a bell
runs straight through from back to
front, and from front to back; it
does not do so on any other number.

Similarly there are ways in which the
features of Kent Major differ from
Kent Minor. You can never get
exactly the same thing on a higher
number that you do on a smaller
number. This is kind of the simplest
method, and quite obvious of the
more complex methods.

Some composers, recognizing this, say
that extension means getting the
nearest possible result on the higher
number. But that won't do. It
is altogether too haphazard. What
one man might consider the nearest
possible, another man would probably
totally dispute. If there is such a

thing as extension at all, there must be a definite mathematical relationship between the different variations. You must be able to say definitely, and without qualification, that such and such is an extension and such and such is not.

Take Rounds on all possible numbers of bells to infinity -

123 - 1234 - 12345 - 123456 - 1234567 →

What is the exact relationship between these Rows? How does 1234 differ from 123? It is not by the addition of anything fresh. Of course in writing out the figures which represent the Row you do add a new figure; and in the tower you add a fresh bell. But so far as the method is concerned which is the added figure or bell? Not the Treble for the Treble on one number is the equivalent of the Treble on all numbers. Not the Tenor, for the Tenor on one number is the equivalent of the Tenor on all numbers. Equally each individual

bell in the Row 123456 is the equivalent
of a bell in the Row 12345.

The only relationship between the Rows
which form this series, is that of a
mathematical progression, and it
follows that if on these Rows, equivalent
Methods are constructed, the relationship
between them will also be a mathematical
progression.

A Method on a given number of Bells
is a series of cyclical movements;

The Extension of that Method will
a progression of the series of cyclical
movements, arranged on a progression
of numbers of Bells.

To understand any progression it
is necessary to state one term and
also the factor of the progression. In
Methods the term must be the
cyclical movement and nothing else,
for these alone are the essential things
of ringing. The factor will vary
in different circumstances but will
be subject to one general law.

Since a progression of Cyclical movements is a progression of the one essential thing in a Method, we shall find that it implies and involves a progression of all other features of any importance. It implies a progression of the Rows, of the Places, and of all the work.

1 2 3 4
2 1 4 3
2 4 1 3
4 2 3 1
4 3 2 1
3 4 1 2
3 1 4 2
1 3 2 4
1 2 3 4

1 2 3 4 5
2 1 4 3 5
2 4 1 5 3
4 2 5 1 3
4 5 2 3 1
5 4 3 2 1
5 3 4 1 2
3 5 1 4 2
3 1 5 2 4
1 3 2 5 4
1 2 3 4 5

1 2 3 4 5 6
2 1 4 3 6 5
2 4 1 6 3 5
4 2 6 1 5 3
4 6 2 5 1 3
6 4 5 2 3 1
6 5 4 3 2 1
5 6 3 4 1 2
5 3 6 1 4 2
3 5 1 6 2 4
3 1 5 2 6 4
1 3 2 5 4 6
1 2 3 4 5 6

Let 12, 123, 1234, 12345, \rightarrow be a progression of Rows to infinity. On each construct a forward Counting Course.

Then since -

a. The starting Rows are in progression;
 b. There is one Cyclical movement on each Row.

c. The movements are in all cases in the same direction (i.e. forward)

∴ The result is a fine Extension

This simple and obvious Extension is the pattern and model of all Extensions just as the all method Construction is implied in the Hunting Course and is a development of it & as all Extension is implied in the above Example

Notice how everything of importance is equally in progression

Coursing Order -

21 - 231 - 2431 - 24531 - 246531 -

Number of Rows -

4 - 6 - 8 - 10 - 12 - 14 - 16 →

Or the Rows themselves. Thus the second Rows are in a progression, -

21. - 213. - 2143. - 21435. - 214365. - 2143657. -

| | | | | | |
|-----------------|-----|------|-------|--------|---------|
| No. of Bells. | 2. | 3 | 4. | 5. | 6. |
| Position of Row | 2. | 3 | 4 | 5. | 6. |
| Row. | 21. | 231. | 4231. | 45231. | 645231. |

Similarly, each individual Row of any any block, on any number, is one of a progression, which runs right through the whole Extension from the lowest number of Bells (2) to infinity.

And this is a general rule of all Extensions, even of the most complex Methods. Each individual Row, on any number, will be one of a progression that runs through all numbers; though in many cases the progression will not be obvious or easy to see.

The one factor in the above Extension is the difference in the number of bells, and extension takes place equally in all features. Thus the relationship between a Hunting Course of Minor and one of Major is in all features that of 6 to 8. The number of bells, the

number of Rows, the number and size of the Cyclical movements, the Counting Order, the Rows themselves, are all strictly in this proportion.

But directly you introduce any Dodging or Secondary Movement, the factor can no longer be the simple one of the difference in the numbers of bells.

| | |
|-------------|-----------------|
| 1 2 3 4 5 6 | 1 2 3 4 5 6 7 8 |
| 2 1 4 3 6 5 | 2 1 4 3 6 5 8 7 |
| 1 2 3 4 5 6 | 1 2 3 4 5 6 7 8 |
| 2 1 4 3 6 5 | 2 1 4 3 6 5 8 7 |
| 2 4 1 6 3 5 | 2 4 1 6 3 8 5 7 |

Take a Block produced by Treble Bob Hunting.

The main forward cyclical movement extends in a progression to infinity, the factor being the difference in the numbers of bells.

The number of inserted dodging movements also expands as the difference in the numbers of bells.

| | |
|--------------------------------------|----------------------------|
| No of Bells. | 4 5 6 7 8 9 10 11 12 13 14 |
| No of Inserted
Dodging Movements. | 4 5 6 7 8 9 10 11 12 13 14 |

But the extent of backward and forward movement in each dodging movement does not extend in the same proportion. On all numbers it is definitely one step backward followed by one step forward.

Of course the total amount of backward and forward movement in the whole Block is increased as the difference in the numbers of bells; but it must be remembered that each dodging movement is complete in itself, and is not constructionally related to any other dodging movement.

The result is that, while a series of Treble Bob Courses on 4, 5, 6, 7 - 7 Bells are in strict progression, the Divisions into which they are divided extend horizontally as the difference in the numbers of Bells; but vertically are constant.

Thus the progression is not a simple one, as in the case of the Hunting Course, but a compound one; and this fact has a profound influence on the extension of Methods.

Or again, take the following -

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 4 | 2 | 6 | 1 | 5 | 3 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 1 | 2 | 3 | 4 | 5 | 6 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |

ad inf.

This series is in strict progression, but the difference in the number of bells is the factor of only the rows themselves. The length by the movement, (three steps forward followed by three steps backward), and the number of Rows are constant.

The following is a further compound progression. The difference in the number of bells is the factor of the

of the Rows themselves. The amount of forward and backward hunting is in the following progression -

| | | | | | | | | | | |
|---|---|---|---|---|----|----|----|----|----|---|
| No of BELLS. | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | → |
| No of STEPS of forward hunting followed by same | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | |
| No of STEPS of backward hunting | | | | | | | | | | |
| No. of Rows. | 3 | 5 | 7 | 9 | 11 | 13 | 15 | 17 | 19 | |

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 2 | 1 | 4 | 3 |
| 1 | 2 | 3 | 4 |

| | | | | |
|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 |
| 2 | 1 | 4 | 3 | 5 |
| 2 | 4 | 1 | 5 | 3 |
| 2 | 1 | 4 | 3 | 5 |
| 1 | 2 | 3 | 4 | 5 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 4 | 2 | 6 | 1 | 5 | 3 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 1 | 2 | 3 | 4 | 5 | 6 |

ad. inf.

This establishes the Law that equal expansion can take place ^{only} within a single Hunting Course; and that when Dodging Movements are introduced expansion is unequal, some features expanding in a different proportion, or remaining constant.

* i.e. the number of bells involved in the particular cycle.

Similarly, expansion in a Block which is constructed by a primary cyclical movement and one or more secondary cycles, is necessarily unequal. Each cycle will expand as the difference in the number of bells*, but as the proportion between the numbers of bells in the primary and the secondary cycles is not constant, but in its progression, the factor of the whole series will be a compound one.

Take the simple example of Plain Bob -

| | |
|--------------------------------|--------------------------------|
| No of Bells. | 4 5 6 7 8 9 10 |
| No of Hunts. | 1 1 1 1 1 1 1 |
| No of Extreme Bells. | 3 4 5 6 7 8 9 |
| No of Rows in Lead | 8 10 12 14 16 18 20 |
| No of Rows in Secondary Cycle. | 6 8 10 12 14 16 18 |
| No of Rows in Course. | 24, 40, 60, 84, 112, 144, 180. |

This is a fine progression, but it is obvious that the factor is not a simple one, and therefore expansion is unequal.

The introduction of other secondary cycles will each bring in a factor of its own, and thus make the progression

still more complex.

The fact that expansion is unequal, and subject to the laws of a fine mathematical progression, has been totally overlooked, and this is largely the cause of so much misunderstanding of what extension really is.

One general law arises from the fact that an extension is a fine progression, which is, that an extension is not confined to a limited number of bells. It goes on to infinity. Thus, if you have a fine extension of London Major to ten bells, you have automatically the fine extension to twelve bells and every number that is in the progression
8 10 12 14 16 →

Conversely, if you have what you call a fine extension from eight bells to ten, and it will not further extend to 12, 14, 16 etc, then that fact is sufficient proof that the extension is not really a fine one, whatever reasons and arguments you may have to think it so.

Further, no one in considering a

mathematical progression and especially a complex one ~~the~~ would think of confining himself to the first two or three terms; and similarly, though for practical purposes we are restricted to twelve bells, and the labour of writing out methods on large numbers is very great, still we must take these higher numbers into consideration. In many cases it is only by so doing that we can appreciate what the extension really is.

A. The Extension of Principles

The Plain Principle consists of the Hunting Course and as we have seen expands in a simple progression, the one factor being the difference in the number of bells.

The Treble Bob Principle consists of a Hunting Course with the addition of certain dodging movements arranged symmetrically. The Hunting Course expands equally as the difference in the number of bells. The number of the dodging.

Movements expands in the same ratio.
Horizontally each Division expands in
the same way; vertically it is constant
on all numbers. I.E. it always comprises
four changes.

The Double Dodging and Triple Dodging
Principles extend in a way similar to
the Triple Bob Principle; and the whole
form examples of the extension of every
symmetrical Principle

On page 274 is an extension of a Principle
in the following progression

| | | | | | | | | |
|-------------------------------------|------|------|------|------|------|------|------|---------|
| No of Bells. - | 6 | 8 | 10 | 12 | 14 | 16 | 18 | |
| No of Hunting Courses | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| Included Oblique Movements | 1 | 3 | 5 | 7 | 9 | 11 | 13 | |
| | pull | pull | pull | pull | pull | pull | pull | |
| No. of Divisions. | 6 | 8 | 10 | 12 | 14 | 16 | 18 | ad Inf. |
| No. of Changes in each
Division. | 4 | 8 | 12 | 16 | 20 | 24 | 28 | |
| No of Changes in Course. | 24 | 64 | 120 | 192 | 280 | 384 | 504 | |

This is a fine progression, and therefore a
fine extension. The factor is not a simple
one, and therefore expansion is unequal,
but there is nothing on any number of

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |

ad Int.

Bells which is not the result of the movement
on six bells expanded in regular ratios.

All other Principles, including those that are asymmetrical, will extend similarly. In most cases more than one factor is possible, and therefore more than one line extension.

B. The Extension of Group I Methods.

The main distinction of Group I Methods is that of the Principle on which they are founded, and therefore the main extension is that of the Principle. It is only necessary to consider how the Additional Shunt's can extend.

Original being identical with the Hunting Course and having no Additional Shunt's expands equally as the difference in the number of bells. This is the only method of which this can be said.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 3 | 4 | 6 | 5 |
| 1 | 2 | 4 | 3 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |

Group I Subdivision B. Methods have the same Division Heads and Ends as the Principle on which they are founded; and, in addition, they have one or more Hunting Courses, on part of the bells, which are wholly within the Division. Forward is typical of these methods and we will now see how Forward can extend.

The Principle is the Treble Bob Principle, and extends in a fine progression, as we have seen, but unequally. The Division expands horizontally, but vertically, is constant.

The Additional Hunt is a complete Hunting Course on two bells made in 3-4. What expansion can take place in this Hunting Course?

A Hunting Course can extend equally as the difference in the number of bells involved in it.

The expansion of the Principle has reduplicated the positions represented by 3-4 on two bells.

Therefore, prima facie, there seem to be four possible ways in which the Hunting Course on two bells, made in 3-4 on

six bells, can be reproduced on the higher numbers.

1. That the Hunting Course should expand in regular ratios as the numbers of bells expand.

2. That it should remain constant in size, in number, and position, i.e. as one Hunting Course on five bells, in 3-4, on all numbers.

3. That it should remain constant in size and number; but that its position should be altered in a regular progression.

4. That it should remain constant in size; but that its number should be increased in a regular progression.

1. Can the Hunting Course expand? The answer is easily seen. It cannot. And for the reason that the extension of the Principle leaves the Division the same size vertically. To whatever number you extend it, the Division always consists of no more than four changes. Four changes suffice for a Hunting Course on five bells. If you expand it to three bells you require six changes. To four bells you require

eight changes. And so on. These increased number of changes are not available; and therefore no expansion can take place within the Hunting Course itself.

All this seems, of course, quite obvious and so need no detailed proof, but we have here an important Law of extension viz that owing to the expansion of the Principle being unequal, the capacity of the Additional Shunt of expansion is very much restricted.

2. The size, position, and number of the Additional Shunt may remain constant

Ex/er:
A.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 3 | 4 | 6 | 5 |
| 1 | 2 | 4 | 3 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 4 | 6 | 5 | 8 | 7 |
| 1 | 2 | 4 | 3 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 3 | 4 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |

This is the traditional and obvious extension. It is a fine progression, but it must be noted that the factor is not a simple one, and therefore expansion is unequal. The relative prominence of the Places which form the Hunting Course steadily decreases with the increase in the numbers of bells. On six bells they occupy a third of the whole Course. On eight but a quarter. And if you produce it to a thousand or more bells they occupy but the finest fraction. Thus, again, shows a general law of extension. Owing to the unequal expansion the relation between different works will alter in a regular ratio. A work which is very prominent on one number, and perhaps seems to dominate the whole Method, will often shrink to insignificance on higher numbers. Thus, because backward hunting seems to be the one prominent feature of London Major, it does not follow that it will be equally prominent when you extend the Method to twelve, fifty, or a hundred bells. Neither does it follow

That because Bristol Purpure Major consists largely of four-bell work, that the extension to higher numbers will also consist of four-bell work.

One further point may be noticed here. Forward Minor is a perfectly double method, but Forward Major is not, and neither is any other of the same extension. Some extensions of some methods are double on all numbers, but this is purely accidental. It is not true to say, as some men say, that because the Major of any method is double, the Royal and the Maximus must also be double.

In complex methods whether a method is double or not, depends very largely on the symmetrical arrangements of the additional stents. In an extension the position of the additional stents relative to the main Cyclical movements may be retained, but the relative position to Before and Behind (which are comparatively unimportant) may be altered. As in the case with Forward.

3. The size and number of the Additional Shunt may remain constant but the position may alter in regular ratio.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |

ad. inf.

The relationship between these Changes is that of a progression. It follows that 3-4 on eight bells is not the only equivalent of 3-4 on six bells; 5-6 is equally the equivalent. Neither 3-4 on eight bells alone, nor 5-6 alone, nor 3-4 and 5-6 together is exactly the same thing as 3-4 on six, but all three, equally, are progressions of it.

It follows that the Additional Shunt may be made as follows -

| | | | | | | |
|-------------------|-----|-----|-----|------|-------|-------|
| No. of Bells. | 6 | 8 | 10 | 12 | 14 | 16 |
| Position of Shunt | 3-4 | 5-6 | 7-8 | 9-10 | 11-12 | 13-14 |

ad. inf.

which will give the following Extension

| | | |
|--------|-------------|-----------------|
| Exten: | 1 2 3 4 5 6 | 1 2 3 4 5 6 7 8 |
| B. | 2 1 3 4 6 5 | 2 1 4 3 5 6 8 7 |
| | 1 2 4 3 5 6 | 1 2 3 4 6 5 7 8 |
| | 2 1 4 3 6 5 | 2 1 4 3 6 5 8 7 |
| | 2 4 1 6 3 5 | 2 4 1 6 3 8 5 7 |

| |
|---------------------|
| 1 2 3 4 5 6 7 8 9 0 |
| 2 1 4 3 6 5 7 8 0 9 |
| 1 2 3 4 5 6 8 7 9 0 |
| 2 1 4 3 6 5 8 7 0 9 |
| 2 4 1 6 3 8 5 0 7 9 |

Again, a further progression is possible. The additional Shanti on six bells occupies the middle position. There is no middle position on eight bells, but only on the numbers in the following progression -
6, 10, 14, 18, 22, 26 ad int.

The additional Shanti will be made in the following positions -
3-4 5-6 7-8 9-10 11-12 13-14 ad int.

| | | |
|--------|-------------|---------------------|
| Exten: | 1 2 3 4 5 6 | 1 2 3 4 5 6 7 8 9 0 |
| C | 2 1 3 4 6 5 | 2 1 4 3 5 6 8 7 0 9 |
| | 1 2 4 3 5 6 | 1 2 3 4 6 5 7 8 9 0 |
| | 2 1 4 3 6 5 | 2 1 4 3 6 5 8 7 0 9 |
| | 2 4 1 6 3 5 | 2 4 1 6 3 8 5 0 7 9 |

L. The size of the Additional Shunt may remain constant, but the number and positions alter in regular ratio.

Not only are 3-4 and 5-6 on eight bells severally the equivalent of 3-4 on six bells, but the two together are the equivalent. This gives us the following Extension.

| | | | |
|--------------------------|-----------|----------|---------------|
| No of Bells. | <u>6.</u> | <u>8</u> | <u>10</u> |
| Positions of Add. Shunt. | 3-4. | 3-4 5-6 | 3-4. 5-6. 7-8 |

| | |
|-------------------|-------------------------|
| <u>12.</u> | <u>14.</u> |
| 3-4 5-6. 7-8 9-10 | 3-4 5-6 7-8 9-10 11-12. |

| | | |
|--------|-------------|-----------------|
| Exten: | 1 2 3 4 5 6 | 1 2 3 4 5 6 7 8 |
| D. | 2 1 3 4 6 5 | 2 1 3 4 5 6 8 7 |
| | 1 2 4 3 5 6 | 1 2 4 3 6 5 7 8 |
| | 2 1 4 3 6 5 | 2 1 4 3 6 5 8 7 |
| | 2 4 1 6 3 5 | 2 4 1 6 3 8 5 7 |

| |
|---------------------|
| 1 2 3 4 5 6 7 8 9 0 |
| 2 1 3 4 5 6 7 8 0 9 |
| 1 2 4 3 6 5 8 7 9 0 |
| 2 1 4 3 6 5 8 7 0 9 |
| 2 4 1 6 3 8 5 0 7 9 |

Thus we have four distinct Extensions, each of which is a perfect progression, each with a different factor. It will be noticed that each is a progression in all its important features; in the Causing Order, in the Rows, and in the work generally. Each is a fine Extension from the strictest point of view of actual ringing; each has one general rule for ringing on all numbers.

A is Treble Bob Hunting except that Places are made when passing through 3-4

B. is Treble Bob Hunting except when passing through the highest dodging position but one.

D. is Treble Bob Hunting in the lowest and highest dodging positions and Place making elsewhere.

C is Treble Bob Hunting except when passing through the middle dodging position.

Musical considerations make A the best Extension, but otherwise they are of equal value.

One further Extension of the Hunt is that produce forward on six bells will

be noticed presently.

I have dealt thus fully with the Extension of Forward Minor because it is a simple example which is thoroughly typical of the Extension of all Methods.

All Group I. Subdivision B. Methods extend in a way similar to Forward.

As Group I Subdivision C Methods are identical in construction to the last class except that the Additional Shunts extend over more than one Division, the extensions will be equally similar.

On page 286 is an example of the extension of these Methods. It will be noticed that expansion is unequal, the Additional Shunts remaining constant in size, but in number and position they are reproduced in a regular progression. On page 287 is a table showing how the progression of Shunts results in a progression of all the other important features of the Method.

B.

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | | |
| 1 | 2 | 3 | 5 | 4 | 6 | 7 | 8 | | |
| 1 | 3 | 2 | 4 | 5 | 7 | 6 | 8 | | |
| 1 | 3 | 2 | 5 | 4 | 7 | 6 | 8 | | |
| 3 | 1 | 5 | 2 | 7 | 4 | 8 | 6 | | |
| 3 | 1 | 5 | 7 | 2 | 4 | 8 | 6 | | |
| 3 | 5 | 1 | 2 | 7 | 8 | 4 | 6 | | |
| 3 | 5 | 1 | 7 | 2 | 8 | 4 | 6 | | |
| 5 | 3 | 7 | 1 | 8 | 2 | 6 | 4 | | |
| 5 | 3 | 7 | 8 | 1 | 2 | 6 | 4 | | |
| 5 | 7 | 3 | 1 | 8 | 6 | 2 | 4 | | |
| 5 | 7 | 3 | 8 | 1 | 6 | 2 | 4 | | |
| 7 | 5 | 8 | 3 | 6 | 1 | 4 | 2 | | |
| 7 | 5 | 8 | 6 | 3 | 1 | 4 | 2 | | |
| 7 | 8 | 5 | 3 | 6 | 4 | 1 | 2 | | |
| 7 | 8 | 5 | 6 | 3 | 4 | 1 | 2 | | |
| 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | | |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 1 | 2 | 3 | 5 | 4 | 7 | 6 | 8 | 9 | 0 |
| 1 | 3 | 2 | 4 | 5 | 6 | 7 | 9 | 8 | 0 |
| 1 | 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 0 |
| 3 | 1 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 |
| 3 | 1 | 5 | 7 | 2 | 9 | 4 | 6 | 0 | 8 |
| 3 | 5 | 1 | 2 | 7 | 4 | 9 | 0 | 6 | 8 |
| 3 | 5 | 1 | 7 | 2 | 9 | 4 | 0 | 6 | 8 |
| 5 | 3 | 7 | 1 | 9 | 2 | 0 | 4 | 8 | 6 |
| 5 | 3 | 7 | 9 | 1 | 0 | 2 | 4 | 8 | 6 |
| 5 | 7 | 3 | 1 | 9 | 2 | 0 | 8 | 4 | 6 |
| 5 | 7 | 3 | 9 | 1 | 0 | 2 | 8 | 4 | 6 |
| 7 | 5 | 9 | 3 | 0 | 1 | 8 | 2 | 6 | 4 |
| 7 | 5 | 9 | 0 | 3 | 8 | 1 | 2 | 6 | 4 |
| 7 | 9 | 5 | 3 | 0 | 1 | 8 | 6 | 2 | 4 |
| 7 | 9 | 5 | 0 | 3 | 8 | 1 | 6 | 2 | 4 |
| 9 | 7 | 0 | 5 | 8 | 3 | 6 | 1 | 4 | 2 |
| 9 | 7 | 0 | 8 | 5 | 6 | 3 | 1 | 4 | 2 |
| 9 | 0 | 7 | 5 | 8 | 3 | 6 | 4 | 1 | 2 |
| 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 1 | 2 |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |

See p. 109.

C CONWAY MAJOR

CONWAY ROYAL

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | | |
| 2 | 1 | 3 | 5 | 4 | 6 | 8 | 7 | | |
| 2 | 3 | 1 | 4 | 5 | 8 | 6 | 7 | | |
| 3 | 2 | 1 | 5 | 4 | 8 | 7 | 6 | | |
| 2 | 3 | 5 | 1 | 8 | 4 | 6 | 7 | | |
| 3 | 2 | 5 | 8 | 1 | 4 | 7 | 6 | | |
| 3 | 5 | 2 | 1 | 8 | 7 | 4 | 6 | | |
| 5 | 3 | 2 | 8 | 1 | 7 | 6 | 4 | | |
| 3 | 5 | 8 | 2 | 7 | 1 | 4 | 6 | | |
| 5 | 3 | 8 | 7 | 2 | 1 | 6 | 4 | | |
| 5 | 8 | 3 | 2 | 7 | 6 | 1 | 4 | | |
| 8 | 5 | 3 | 7 | 2 | 6 | 4 | 1 | | |
| 5 | 8 | 7 | 3 | 6 | 2 | 1 | 4 | | |
| 8 | 5 | 7 | 6 | 3 | 2 | 4 | 1 | | |
| 8 | 7 | 5 | 3 | 6 | 4 | 2 | 1 | | |
| 7 | 8 | 5 | 6 | 3 | 4 | 1 | 2 | | |
| 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | | |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 3 | 5 | 4 | 7 | 6 | 8 | 0 | 9 |
| 2 | 3 | 1 | 4 | 5 | 6 | 7 | 0 | 8 | 9 |
| 3 | 2 | 1 | 5 | 4 | 7 | 6 | 0 | 9 | 8 |
| 2 | 3 | 5 | 1 | 7 | 4 | 0 | 6 | 8 | 9 |
| 3 | 2 | 5 | 7 | 1 | 0 | 4 | 6 | 9 | 8 |
| 3 | 5 | 2 | 1 | 7 | 4 | 0 | 9 | 6 | 8 |
| 5 | 3 | 2 | 7 | 1 | 0 | 4 | 9 | 8 | 6 |
| 3 | 5 | 7 | 2 | 0 | 1 | 9 | 4 | 6 | 8 |
| 5 | 3 | 7 | 0 | 2 | 9 | 1 | 4 | 8 | 6 |
| 5 | 7 | 3 | 2 | 0 | 1 | 9 | 8 | 4 | 6 |
| 7 | 5 | 3 | 2 | 0 | 1 | 9 | 8 | 4 | 6 |
| 7 | 5 | 0 | 3 | 9 | 2 | 8 | 1 | 4 | 6 |
| 7 | 5 | 0 | 9 | 3 | 8 | 2 | 1 | 6 | 4 |
| 7 | 0 | 5 | 3 | 9 | 2 | 8 | 6 | 1 | 4 |
| 0 | 7 | 5 | 9 | 3 | 8 | 2 | 6 | 4 | 1 |
| 7 | 0 | 9 | 5 | 8 | 3 | 6 | 2 | 1 | 4 |
| 0 | 7 | 9 | 8 | 5 | 6 | 3 | 2 | 4 | 1 |
| 0 | 9 | 7 | 5 | 8 | 3 | 6 | 4 | 2 | 1 |
| 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 1 | 2 |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |

The Extension of CONWAY MAJOR.

| | | | | | | | |
|--------------------------------------|--------------------------|---------|----------|----------|----|----|----|
| No. of Bells | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| No of Divisions | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| No of Rows in each Division | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| No of Rows in Course. | 32 | 40 | 48 | 56 | 64 | 72 | 80 |
| C.O. of Principle | 1-3578642 - 1357908642 - | | | | | | |
| Order in which bells come to Lead. | 23587641 - 2357098641 - | | | | | | |
| Total No of Add Shunts | 32 | 40 | 48 | 56 | 64 | 72 | 80 |
| Position of First set of Add. Shunts | 34-67 | 34,89 | 34,1011 | 34 12-13 | | | |
| Position of Second do | 12 7-8 | 12 9-10 | 12 11-12 | 12 13-14 | | | |
| No of pairs of bells dodging. | 1 | 2 | 3 | 4 | 5 | 6 | 7. |

Ad. Int.

Progression of the Rows.

| No of Bells | Position of Row. | Rows. |
|-------------|------------------|---|
| 8 | 5th | 2 3 5 1 8 4 6 7 |
| 10 | 5 | 2 3 5 1 7 4 10 6 8 9 |
| 12 | 5 | 2 3 5 1 7 4 9 6 12 8 10 11 |
| 14 | 5 | 2 3 5 1 7 4 9 6 11 8 14 10 12 13 |
| 16 | 5 | 2 3 5 1 7 4 9 6 11 8 13 10 16 12 14 15 |
| 18 | 5 | 2 3 5 1 7 4 9 6 11 8 13 10 15 12 18 14 16 17. |
| 8 | 12th | 8 5 3 7 2 6 4 1 |
| 10 | 16 | 10 7 5 9 3 8 2 6 4 1 |
| 12 | 20 | 12 9 7 11 5 10 3 8 2 6 4 1 |
| 14 | 24 | 14 11 9 13 7 12 5 10 3 8 2 6 4 1 |
| 16 | 28 | 16 13 11 15 9 14 7 12 5 10 3 8 2 6 4 1 |
| 18 | 32 | 18 15 13 17 11 16 9 14 7 12 5 10 3 8 2 6 4 1. |

The Rows selected for illustration have been taken at random. All other Rows are similarly in progression.

The diagrams of the work of the bells will show that all Hunting Dodging and Place Making are equally in progression.

In the examples I have given, the Divisions of the Principle have expanded horizontally, but vertically have remained constant.

On page 1274 we saw that expansion in the Divisions of a Principle can take place both horizontally and vertically.

This increased expansion will allow the additional Shunt's room to expand in size, and not merely in number and position. We get the following Extension

| | | | | | | |
|--|-----|-----|-----|------|------|------|
| No of Bells. | 6 | 8 | 10 | 12 | 14 | 16 |
| No of Divisions | 6 | 8 | 10 | 12 | 14 | 16 |
| No of Dodging Movements
in each Division. | 1 | 3 | 5 | 7 | 9 | 11 |
| No Rows in Course | 24 | 64 | 120 | 192 | 280 | 384 |
| No of Rows in each Division | 4 | 8 | 12 | 16 | 20 | 24 |
| No of Bells in each Add.
Shunt. | 2 | 4 | 6 | 8 | 10 | 12 |
| Position of Add. Shunt. | 3-4 | 3-6 | 3-8 | 3-10 | 3-12 | 3-14 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 3 | 4 | 6 | 5 |
| 1 | 2 | 4 | 3 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 5 | 4 | 6 | 8 | 7 |
| 1 | 2 | 5 | 3 | 6 | 4 | 7 | 8 |
| 2 | 1 | 5 | 6 | 3 | 4 | 8 | 7 |
| 1 | 2 | 6 | 5 | 4 | 3 | 7 | 8 |
| 2 | 1 | 6 | 4 | 5 | 3 | 8 | 7 |
| 1 | 2 | 4 | 6 | 3 | 5 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 3 | 5 | 4 | 7 | 6 | 8 | 0 | 9 |
| 1 | 2 | 5 | 3 | 7 | 4 | 8 | 6 | 9 | 0 |
| 2 | 1 | 5 | 7 | 3 | 8 | 4 | 6 | 0 | 9 |
| 1 | 2 | 7 | 5 | 8 | 3 | 6 | 4 | 9 | 0 |
| 2 | 1 | 7 | 8 | 5 | 6 | 3 | 4 | 0 | 9 |
| 1 | 2 | 8 | 7 | 6 | 5 | 4 | 3 | 9 | 0 |
| 2 | 1 | 8 | 6 | 7 | 4 | 5 | 3 | 0 | 9 |
| 1 | 2 | 6 | 8 | 4 | 7 | 3 | 5 | 9 | 0 |
| 2 | 1 | 6 | 4 | 8 | 3 | 7 | 5 | 0 | 9 |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 7 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | ET |
| 2 | 1 | 3 | 5 | 4 | 7 | 6 | 9 | 8 | 0 | TE |
| 1 | 2 | 5 | 3 | 7 | 4 | 9 | 6 | 0 | 8 | ET |
| 2 | 1 | 5 | 7 | 3 | 9 | 4 | 0 | 6 | 8 | TE |
| 1 | 2 | 7 | 5 | 9 | 3 | 0 | 4 | 8 | 6 | ET |
| 2 | 1 | 7 | 9 | 5 | 0 | 3 | 8 | 4 | 6 | TE |
| 1 | 2 | 9 | 7 | 0 | 5 | 8 | 3 | 6 | 4 | ET |
| 2 | 1 | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | TE |
| 1 | 2 | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | ET |
| 2 | 1 | 0 | 8 | 9 | 6 | 7 | 4 | 5 | 3 | TE |
| 1 | 2 | 8 | 0 | 6 | 9 | 4 | 7 | 3 | 5 | ET |
| 2 | 1 | 8 | 6 | 0 | 4 | 9 | 3 | 7 | 5 | TE |
| 1 | 2 | 6 | 8 | 4 | 0 | 3 | 9 | 5 | 7 | ET |
| 2 | 1 | 6 | 4 | 8 | 3 | 0 | 5 | 9 | 7 | TE |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | ET |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | TE |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | ET |

This Extension, when tested, will be shown to be a perfect progression in all its features. It is no doubt somewhat difficult at first sight to recognize that the diagram of the Mascinus is a fine extension of that of the Minor. The difficulty largely vanishes when we remember that the two Places in the latter are a complete Hunting Course on five bells, and when we place the methods through the increasing numbers of bells. On eight bells and upwards the identity of the diagram is easily seen.

All these Extensions are progressions, but it must be remembered that progression alone does not make a fine Extension. It must be a progression of Cyclical movements. You could have a fine progression of Places, but that would not necessarily give you a fine Extension of a Method. Men sometimes argue that Places are the essential things in the construction of a Method, therefore in an Extension you must reproduce them in the same relative numbers and positions. Thus-

| | |
|-----|-------------|
| (a) | 1 2 3 4 5 6 |
| | 2 1 3 4 6 5 |

3rd Place (they say) is 3rd from the front;
 4th Place is 3rd from behind. Therefore
 on eight bells they may appear as follows:-

| | |
|-----|-----------------|
| (b) | 1 2 3 4 5 6 7 8 |
| | 2 1 3 5 4 6 8 7 |

But Cyclical movement and not Places
 is the essential thing in the construction
 of a method. (b) will only be the true
 equivalent of (a) if it is part of some
 properly extended Hunting or Dodging
 movement.

| | | | |
|-----|-------------|-----|-----------------|
| (c) | 1 2 3 4 5 6 | (d) | 1 2 3 4 5 6 7 8 |
| | 2 1 3 4 6 5 | | 2 1 3 5 4 6 8 7 |
| | 1 2 4 3 5 6 | | 1 2 5 3 6 4 7 8 |
| | 2 1 4 3 6 5 | | 2 1 5 6 3 4 8 7 |

(d) is not an Extension of (c) because
 in (c) the movements are complete, but
 in (d) they are incomplete.

C. The Extension of Group II Methods.

The Extension of Group II Methods is -

1. The Extension of the Principle;
2. The Extension of the Constitutional Shuntis;
3. The Extension of the Additional Shuntis (if there are any).

(a) Methods on the Plain Principle

The Plain Principle expands equally in regular progression as the difference in the numbers of Bells.

1. The Extreme Constitutional Shuntis.

The Extreme Constitutional Shuntis is a Cyclical movement on part of the total number of Bells.

It divides the Bells into Shuntis and Extreme Bells, and involves -

- (a) A Hunting Course on the Extreme Bells in opposite order to the movement of the Principle;
- (b) A Cyclical path of the Shuntis, through the Counting Order of the Extreme

Bells.

From the nature of movement, both cycles (a) and (b) can expand as the difference in the numbers of Bells involved in them.

The number of Bells comprising either, can expand in regular progression, but as the division into Huntis and Extreme Bells is necessarily in a different ratio from the numbers of Bells in the Principle, expansion will be unequal.

On any number of Bells there are but two positions in which Extreme Huntis can be made - Before and Behind; * and therefore on all numbers there are but three possible combinations A, B and A+B.

Extension of any one of these combinations will be the expansion in regular progression of the number of Huntis Bells, or Extreme Bells, or both. The following formula (page 294) gives every possible Extension from four Bells (the minimum) upwards.

In the symbols the top figure represents the number of Huntis and the bottom the number of Extreme Bells. Thus $\frac{2}{7}$ represents two Huntis and seven Extreme Bells.

* See p. 150.

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 2 | 1 | 4 | 3 |
| 2 | 4 | 1 | 3 |
| 4 | 2 | 3 | 1 |
| 2 | 4 | 3 | |
| 4 | 2 | 3 | |
| 4 | 2 | 3 | |
| 4 | 3 | 2 | |
| 4 | 2 | 3 | |

| | | | | | |
|---|---|---|---|---|---|
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 4 | 2 | 6 | 1 | 5 | 3 |
| 4 | 6 | 2 | 5 | 1 | 3 |
| 6 | 4 | 5 | 2 | 3 | 1 |
| 6 | 5 | 4 | 3 | 2 | |
| 6 | 4 | 5 | 3 | 2 | |
| 6 | 5 | 4 | 1 | 3 | 2 |
| 5 | 6 | 4 | 2 | 3 | |
| 5 | 1 | 6 | 2 | 4 | 3 |
| 1 | 5 | 2 | 6 | 3 | 4 |
| 1 | 2 | 5 | 3 | 6 | 4 |
| 2 | 1 | 5 | 6 | 3 | 4 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 6 | 2 | 8 | 1 | 7 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 1 | 5 | 3 |
| 6 | 8 | 4 | 7 | 2 | 5 | 1 | 3 |
| 8 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 6 | 8 | 4 | 7 | 5 | 3 | 2 | 1 |
| 8 | 6 | 7 | 4 | 3 | 5 | 1 | 2 |
| 8 | 7 | 6 | 3 | 4 | 1 | 5 | 2 |
| 7 | 8 | 3 | 6 | 1 | 4 | 2 | 5 |
| 7 | 3 | 8 | 1 | 6 | 2 | 4 | 5 |
| 3 | 7 | 8 | 2 | 6 | 5 | 4 | |
| 3 | 7 | 2 | 8 | 5 | 6 | 4 | |
| 1 | 3 | 2 | 7 | 5 | 8 | 4 | 6 |
| 1 | 2 | 3 | 7 | 8 | 5 | 6 | 4 |

Example of
Extension from Formula
page 394.

$$\frac{1}{3} - \frac{2}{4} - \frac{3}{5} - \frac{4}{6} - \frac{5}{7} - \frac{6}{8} \rightarrow$$

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 1 | 9 | 3 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 1 | 3 |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| 0 | 8 | 9 | 6 | 7 | 5 | 3 | 4 | 1 | 2 |
| 0 | 9 | 8 | 7 | 6 | 3 | 5 | 1 | 4 | 2 |
| 9 | 0 | 7 | 8 | 3 | 6 | 1 | 5 | 2 | 4 |
| 9 | 7 | 0 | 3 | 8 | 1 | 6 | 2 | 5 | 4 |
| 7 | 9 | 3 | 0 | 1 | 8 | 2 | 6 | 4 | 5 |
| 7 | 3 | 9 | 0 | 2 | 8 | 4 | 6 | 5 | |
| 3 | 7 | 1 | 9 | 2 | 0 | 4 | 8 | 5 | 6 |
| 3 | 1 | 7 | 2 | 9 | 4 | 0 | 5 | 8 | 6 |
| 1 | 3 | 2 | 7 | 4 | 9 | 5 | 0 | 6 | 8 |
| 1 | 2 | 3 | 4 | 2 | 5 | 9 | 6 | 0 | 8 |
| 2 | 1 | 4 | 3 | 7 | 9 | 5 | 0 | 6 | 8 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 1 | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 1 | 9 | 3 | 7 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 1 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 1 | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 0 | T | 8 | E | 6 | 9 | 7 | 5 | 4 | 3 | 2 | 1 |
| T | 0 | E | 8 | 9 | 6 | 5 | 7 | 3 | 4 | 1 | 2 |
| T | E | 0 | 9 | 8 | 5 | 6 | 3 | 7 | 1 | 4 | 2 |
| E | T | 9 | 0 | 5 | 8 | 3 | 6 | 1 | 7 | 2 | 4 |
| E | 9 | T | 5 | 0 | 3 | 8 | 1 | 6 | 2 | 7 | 4 |
| 9 | E | 5 | T | 3 | 0 | 1 | 8 | 2 | 6 | 4 | 7 |
| 9 | 5 | E | 3 | T | 1 | 0 | 2 | 8 | 4 | 6 | 7 |
| 5 | 9 | 3 | E | 1 | T | 2 | 0 | 4 | 8 | 7 | 6 |
| 5 | 3 | 9 | 1 | E | 2 | T | 4 | 0 | 7 | 8 | 6 |
| 3 | 5 | 1 | 9 | 2 | E | 4 | T | 7 | 0 | 6 | 8 |
| 3 | 1 | 5 | 2 | 9 | 4 | E | 7 | T | 6 | 0 | 8 |
| 1 | 3 | 2 | 5 | 4 | 9 | 7 | E | 6 | T | 8 | 0 |
| 1 | 2 | 3 | 4 | 5 | 9 | E | 7 | T | 6 | 0 | 8 |

2. The Court Shunt

A Court Shunt is a cyclical movement on part of the total number of Bells. It divides the Bells into Hunts and Extreme Bells, and involves a cyclical path of the Hunts through the Causing Order of the Extreme Bells. Each member of the cycle on the Extreme Bells is made in two parts.

From the nature of cyclical movement it follows that these cycles will expand as the difference in the number of bells involved in them.

Therefore a Court Shunt can expand

1. By adding to the number of Hunts in a regular progression
2. By adding to the number of Extreme Bells in regular progression.
3. By adding to both Hunts and Extreme Bells.

R Court Shunt and P Court Shunt are essentially the same thing, and in some Extensions an R Court Shunt may become a P Court Shunt, and vice versa. It is however convenient to consider them separately.

Extension by adding to the Hunts is

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 6 | 5 | 4 | 1 | 2 | 3 |
| 5 | 6 | 1 | 4 | 3 | 2 |
| 5 | 6 | 3 | 4 | 2 | 1 |
| 5 | 3 | 6 | 2 | 4 | 1 |
| 1 | 3 | 5 | 2 | 6 | 4 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 2 | 4 | 1 | 3 | 6 | 5 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 2 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 6 | 5 | 4 | 1 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 3 | 2 |
| 5 | 6 | 1 | 4 | 3 | 2 |
| 5 | 6 | 1 | 4 | 3 | 2 |
| 1 | 3 | 5 | 2 | 6 | 4 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 2 | 4 | 1 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 6 | 5 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 6 | 5 | 4 | 1 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 1 | 3 | 5 | 2 | 6 | 4 |

Extension of an R Court Shunt
by adding 10 Hunts.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 2 | 4 | 1 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 6 | 5 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 6 | 5 | 4 | 1 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 1 | 3 | 5 | 2 | 6 | 4 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 2 | 4 | 1 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 6 | 5 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 6 | 5 | 4 | 1 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 5 | 6 | 1 | 4 | 2 | 3 |
| 1 | 3 | 5 | 2 | 6 | 4 |

a matter which concerns all Group II Methods equally, and will be dealt with briefly later.

An R Count Sheet expands in regular ratio as the difference in the numbers of Extreme Bells.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |

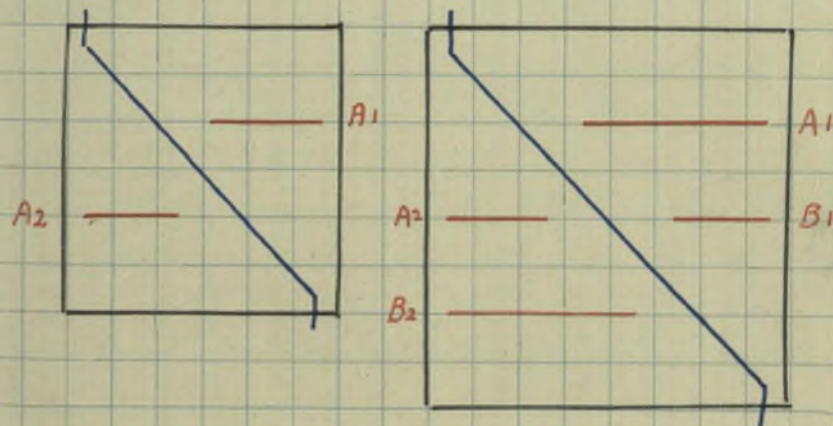
| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 7 |
| 4 | 2 | 6 | 3 | 8 | 1 | 7 | 5 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | 9 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | T | 9 | E |

Owing to the expansion of the Plain Principle, the number of positions in which R Count Shunts can be made increases in regular progression

| | | | | | | | | | |
|---|---|---|---|----|----|----|----|----|---|
| No of Extreme Bells. | 5 | 7 | 9 | 11 | 13 | 15 | 17 | 19 | → |
| No of Positions of
R.C. Shunt's Hunt up? | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | → |
| do do Hunt down. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | → |



Neither A (7 Ex Bells), nor $\frac{B}{7}$, nor $\frac{A+B}{7}$, is exactly the same thing as $\frac{A}{5}$; but each is equally an equivalent, and therefore each is equally a fine Extension. Similarly, each of the combinations of the R Shunt's in the three positions with nine Extreme Bells, is an Extension. And so on with the increased number

of Combinations on the higher numbers.

The following formulae give -

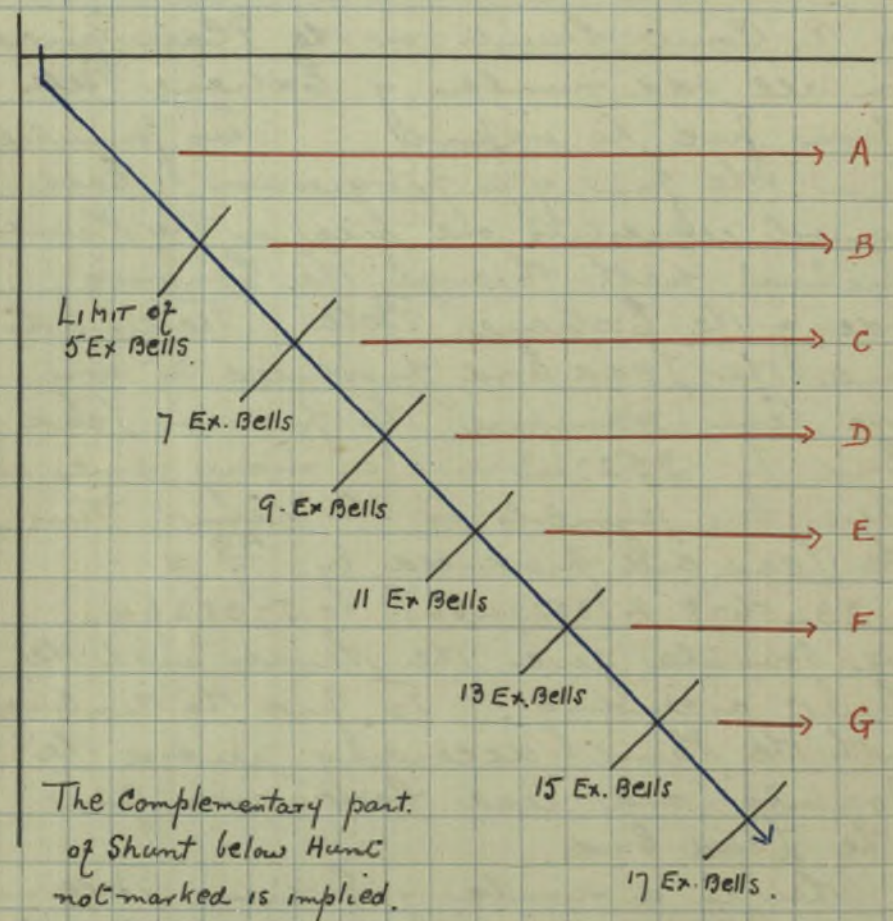
1. All the possible combinations of R. Court Shunts on the Plain Principle on all odd numbers of Extreme Bells from five to infinity. This formulae is in the form of a progression. Each symbol represents one step in the Hunt's cyclical path through the Courting Order of the Extreme Bells. Therefore to find the Lead End produced by any one term, transpose the previous Lead End by 352748..... as many times as there are symbols in the term. Thus the Lead end produced by $\frac{AB}{7} =$

$$2345678 * (3527486)^2 = 5738264.$$

The formula gives the Shunts with the Hunt ascending. To find the combinations with the Hunt descending, reverse the formula, and read backwards from the Lead End.

When to a number of Extreme Bells in strict progression, a series of these terms also in strict progression, is applied a fine Extension is produced.

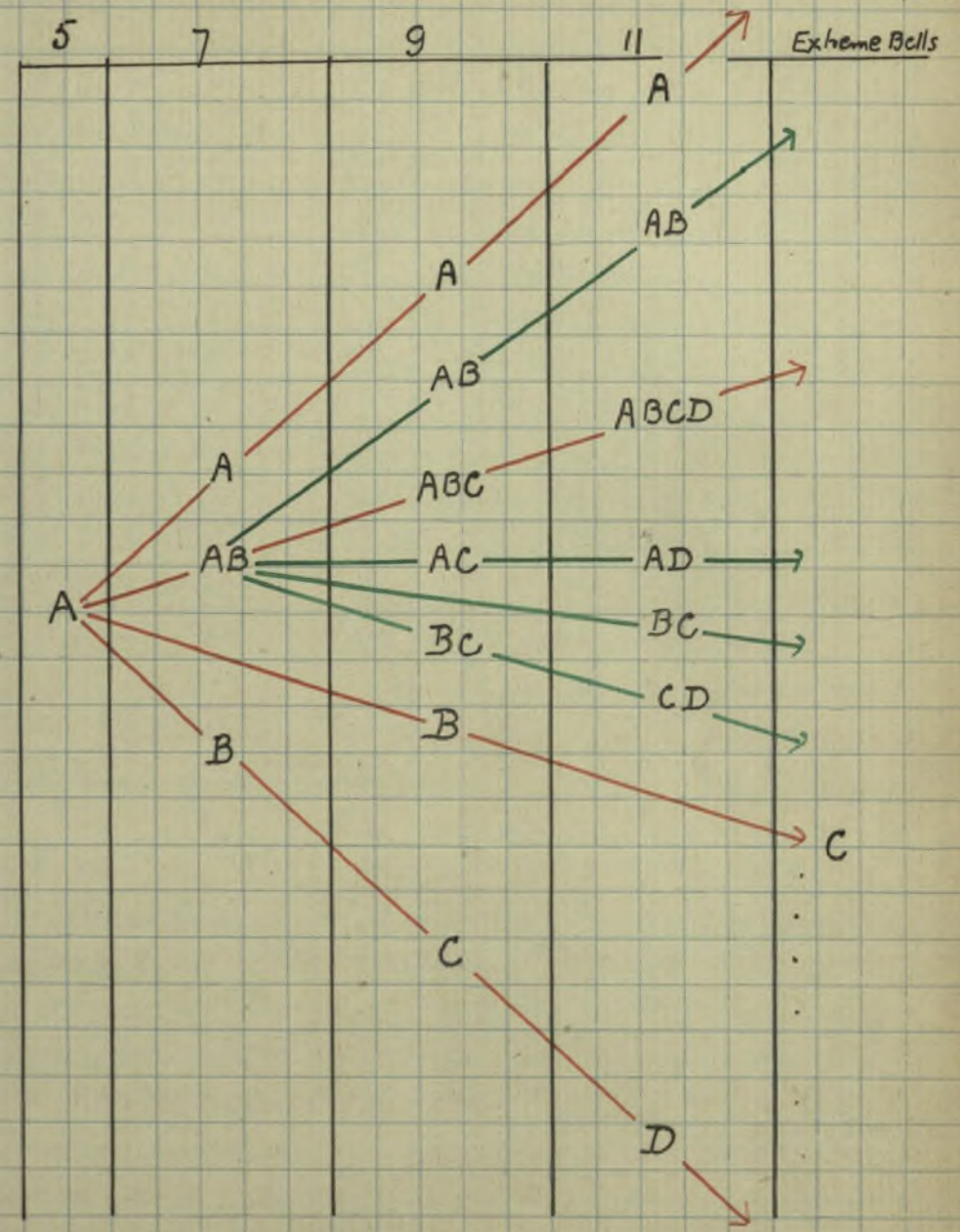
Formula 2. (page 302) gives the more important of these Extensions.



LIMIT OF EXTREME BELLS.

| | | | |
|----|-------|----|--------|
| | | | BCDE |
| | | | BC E |
| 5 | A | | B D E |
| | AB | | B E |
| 7 | B | | CDE |
| | ABC | | C E |
| | AC | | DE |
| | BC | 13 | E |
| 9 | C | | ABCDEF |
| | ABCD | | ABCD F |
| | AB D | | ABC EF |
| | ACD | | ABC F |
| | A D | | AB DEF |
| | BCD | | AB D F |
| | B D | | AB EF |
| | CD | | AB F |
| 11 | D | | A CDEF |
| | ABCDE | | A CD F |
| | ABC E | | A C EF |
| | AB DE | | A C F |
| | AB E | | A DEF |
| | ACDE | | A D F |
| | AC E | | A EF |
| | A DE | | A E |
| | A E | | BCDEF |

Ad Inf.



$$\frac{A}{5}$$

A.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 6 | 5 | 4 | 2 | 3 | 1 |
| 5 | 6 | 4 | 3 | 2 | 1 |
| 5 | 6 | 3 | 4 | 2 | 1 |
| 5 | 3 | 6 | 2 | 4 | 1 |
| 1 | 3 | 5 | 2 | 6 | 4 |

A1

A2.

Two Examples will suffice to illustrate the Extension of R Count Shunt.

A shows an R.C. Shunt with five Extreme Bells Shunt ascending.

The position of this Shunt can be described as follows.

1. It is the nearest position to the Shunt's whole full Before;
2. It is the nearest position to the Shunt's whole full Behind;
3. It is the position midway between the Shunt's whole fulls at Before and Behind.

4. It is every possible position in which an R.C. Shunt can be made.

Neither 1, 2, 3 nor 4, by itself, fully represents the position of the Shunt with five Extreme Bells, but each is equally entitled to be considered the equivalent on the higher numbers.

The position of the Shunt with the Shunt descending corresponds. This gives us the following Extensions.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 3 | 1 |
| 4 | 6 | 5 | 2 | 3 | 1 |
| 6 | 4 | 5 | 3 | 2 | 1 |
| 6 | 1 | 4 | 5 | 2 | 3 |
| 6 | 5 | 4 | 3 | 2 | 1 |
| 1 | 5 | 6 | 3 | 4 | 2 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 7 |
| 4 | 2 | 6 | 3 | 8 | 1 | 7 | 5 |
| 4 | 6 | 2 | 8 | 3 | 7 | 1 | 5 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |
| 8 | 6 | 7 | 4 | 5 | 2 | 1 | 3 |
| 8 | 7 | 6 | 5 | 4 | 2 | 3 | 1 |
| 7 | 8 | 5 | 6 | 1 | 4 | 3 | 2 |
| 8 | 7 | 5 | 1 | 6 | 3 | 4 | 2 |
| 7 | 8 | 5 | 3 | 6 | 2 | 4 | 1 |
| 7 | 1 | 8 | 5 | 6 | 3 | 4 | 2 |
| 7 | 5 | 8 | 3 | 6 | 2 | 4 | 1 |
| 1 | 5 | 7 | 3 | 8 | 2 | 6 | 4 |

Extension I

$\frac{A}{5}$ $\frac{A}{7}$ $\frac{A}{9}$ $\frac{A}{11}$ $\frac{A}{13}$ $\frac{A}{15}$ →
 ad. inf.

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 8 | 1 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 1 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 3 | 7 | 1 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 1 | 2 | 3 |
| 9 | 0 | 7 | 8 | 5 | 6 | 1 | 4 | 3 | 2 |
| 9 | 7 | 0 | 5 | 8 | 1 | 6 | 3 | 4 | 2 |
| 7 | 9 | 5 | 0 | 8 | 3 | 6 | 2 | 4 | 1 |
| 9 | 7 | 5 | 0 | 3 | 8 | 2 | 6 | 4 | 1 |
| 7 | 9 | 5 | 3 | 0 | 2 | 8 | 4 | 6 | 1 |
| 7 | 9 | 5 | 0 | 3 | 8 | 2 | 6 | 4 | 1 |
| 1 | 7 | 5 | 9 | 3 | 0 | 2 | 8 | 4 | 6 |
| 1 | 5 | 7 | 3 | 9 | 2 | 0 | 4 | 8 | 6 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 3 | 8 | 1 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 1 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 1 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 9 | 1 | 7 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 3 | 7 | 1 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| T | E | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 2 | 3 | 1 |
| E | T | 9 | 0 | 7 | 8 | 5 | 6 | 1 | 4 | 3 | 2 |
| E | 9 | T | 7 | 0 | 5 | 8 | 1 | 6 | 3 | 4 | 2 |
| 9 | E | 7 | T | 5 | 0 | 1 | 8 | 3 | 6 | 2 | 4 |
| 9 | 7 | E | 5 | T | 0 | 3 | 8 | 2 | 6 | 4 | 1 |
| 7 | 9 | 5 | E | T | 3 | 0 | 2 | 8 | 4 | 6 | 1 |
| 9 | 7 | 5 | E | 3 | T | 2 | 0 | 4 | 8 | 6 | 1 |
| 7 | 9 | 5 | 3 | E | 2 | T | 4 | 0 | 6 | 8 | 1 |
| 7 | 9 | 5 | E | 3 | T | 2 | 0 | 4 | 8 | 6 | 1 |
| 1 | 7 | 5 | 9 | 3 | E | 2 | T | 4 | 0 | 6 | 8 |
| 1 | 5 | 7 | 3 | 9 | 2 | E | 4 | T | 6 | 0 | 8 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 3 | 1 |
| 4 | 6 | 5 | 1 | 2 | 3 |
| 6 | 4 | 1 | 5 | 3 | 2 |
| 6 | 1 | 4 | 5 | 2 | 3 |
| 6 | 5 | 4 | 3 | 2 | 1 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 6 | 2 | 8 | 1 | 3 | 5 | 7 |
| 6 | 4 | 8 | 2 | 3 | 1 | 7 | 5 |
| 4 | 6 | 2 | 8 | 3 | 7 | 1 | 5 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |
| 8 | 6 | 7 | 4 | 5 | 2 | 1 | 3 |
| 6 | 8 | 4 | 7 | 5 | 1 | 2 | 3 |
| 8 | 6 | 7 | 4 | 1 | 5 | 3 | 2 |
| 8 | 7 | 6 | 1 | 4 | 5 | 2 | 3 |
| 7 | 8 | 1 | 6 | 5 | 4 | 3 | 2 |
| 7 | 1 | 8 | 5 | 6 | 3 | 4 | 2 |
| 7 | 5 | 8 | 3 | 6 | 2 | 4 | 1 |
| 1 | 5 | 7 | 3 | 8 | 2 | 6 | 4 |

Extension II.

| | | | | | |
|---|---|---|----|----|----|
| A | B | C | D | E | F |
| 5 | 7 | 9 | 11 | 13 | 15 |

ad. inf.

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 1 | 9 | 3 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 1 | 3 | 5 | 7 |
| 8 | 6 | 0 | 4 | 9 | 2 | 3 | 1 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 3 | 7 | 1 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 1 | 3 |
| 8 | 0 | 6 | 9 | 4 | 7 | 5 | 2 | 3 | 1 |
| 0 | 8 | 9 | 6 | 7 | 4 | 1 | 5 | 3 | 2 |
| 0 | 9 | 8 | 7 | 6 | 1 | 4 | 5 | 2 | 3 |
| 9 | 0 | 7 | 8 | 1 | 6 | 5 | 4 | 3 | 2 |
| 9 | 7 | 0 | 8 | 5 | 6 | 3 | 4 | 2 | 1 |
| 7 | 9 | 1 | 0 | 5 | 8 | 3 | 6 | 2 | 4 |
| 7 | 1 | 9 | 5 | 0 | 3 | 8 | 2 | 6 | 4 |
| 7 | 5 | 9 | 3 | 0 | 2 | 8 | 4 | 6 | 1 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 1 | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 1 | 9 | 3 | 7 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 1 | 3 | 5 | 7 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 3 | 1 | 7 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 3 | 7 | 1 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 1 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 5 | 1 | 2 | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 1 | 5 | 3 | 2 |
| T | E | 0 | 9 | 8 | 7 | 6 | 1 | 4 | 5 | 2 | 3 |
| E | T | 9 | 0 | 7 | 8 | 1 | 6 | 5 | 4 | 3 | 2 |
| E | 9 | T | 7 | 0 | 8 | 5 | 6 | 3 | 4 | 2 | 1 |
| 9 | E | 7 | T | 1 | 0 | 5 | 8 | 3 | 6 | 2 | 4 |
| 9 | 7 | E | 1 | T | 5 | 0 | 3 | 8 | 2 | 6 | 4 |
| 7 | 9 | 1 | E | 5 | T | 3 | 0 | 2 | 8 | 4 | 6 |
| 7 | 1 | 9 | 5 | E | 3 | T | 2 | 0 | 4 | 8 | 6 |
| 7 | 5 | 9 | 3 | E | 2 | T | 4 | 0 | 6 | 8 | 1 |
| 1 | 5 | 7 | 3 | 9 | 2 | E | 4 | T | 6 | 0 | 8 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 4 | 6 | 5 | 1 | 2 | 3 |
| 6 | 4 | 1 | 5 | 3 | 2 |
| 6 | 4 | 5 | 2 | 3 | 1 |
| 6 | 5 | 4 | 3 | 2 | 1 |
| 1 | 5 | 6 | 3 | 4 | 2 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | 1 |
| 6 | 4 | 8 | 2 | 7 | 3 | 1 | 5 |
| 4 | 6 | 2 | 8 | 7 | 1 | 3 | 5 |
| 6 | 4 | 8 | 2 | 1 | 7 | 5 | 3 |
| 4 | 6 | 8 | 1 | 2 | 7 | 3 | 5 |
| 6 | 4 | 1 | 8 | 7 | 2 | 5 | 3 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 1 | 6 | 8 | 4 | 7 | 2 | 5 | 3 |
| 1 | 8 | 6 | 7 | 4 | 5 | 2 | 3 |

Extension III

| | | | |
|----------|-----------|------------|-------------|
| <u>A</u> | <u>AB</u> | <u>ABC</u> | <u>ABCD</u> |
| 5 | 7 | 9 | 11 |

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| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 0 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 7 | 1 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 5 | 1 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 9 | 1 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 7 | 5 | 1 |
| 4 | 6 | 2 | 8 | 0 | 1 | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 9 | 3 | 7 | 5 | 1 |
| 4 | 6 | 8 | 1 | 2 | 0 | 3 | 9 | 5 | 7 |
| 6 | 4 | 1 | 8 | 0 | 2 | 9 | 3 | 7 | 5 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 5 | 7 | 1 |
| 1 | 6 | 8 | 4 | 0 | 2 | 9 | 3 | 7 | 5 |
| 1 | 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 5 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 | E | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | 1 | E |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | 1 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | 7 | E | 9 | 1 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 | 1 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | E | 1 | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 9 | 7 | 1 |
| 4 | 6 | 2 | 8 | 3 | 0 | T | 5 | E | 7 | 9 | 1 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | E | 5 | 9 | 7 | 1 |
| 4 | 6 | 2 | 8 | 0 | 1 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 9 | T | 3 | E | 5 | 9 | 7 |
| 4 | 6 | 8 | 1 | 2 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 1 | 8 | 0 | 2 | T | 3 | E | 5 | 9 | 7 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 | 1 |
| 1 | 6 | 8 | 4 | 0 | 2 | T | 3 | E | 5 | 9 | 7 |
| 1 | 8 | 6 | 0 | 4 | T | 2 | E | 3 | 9 | 5 | 7 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 3 | 5 | 6 |
| 4 | 2 | 3 | 1 | 6 | 5 |
| 2 | 4 | 3 | 6 | 1 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 1 | 3 |
| 2 | 6 | 5 | 1 | 2 | 3 |
| 6 | 4 | 1 | 5 | 3 | 2 |
| 6 | 1 | 4 | 5 | 2 | 3 |
| 1 | 6 | 5 | 4 | 3 | 2 |
| 1 | 5 | 6 | 3 | 4 | 2 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 3 | 5 | 0 | 7 | 9 |
| 6 | 4 | 8 | 2 | 3 | 1 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 1 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 3 | 7 | 1 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 1 | 3 |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 1 | 2 | 3 |
| 9 | 0 | 7 | 8 | 5 | 6 | 1 | 4 | 3 | 2 |
| 0 | 9 | 8 | 7 | 5 | 1 | 6 | 3 | 4 | 2 |
| 9 | 0 | 7 | 8 | 1 | 5 | 3 | 6 | 2 | 4 |
| 9 | 7 | 0 | 1 | 8 | 5 | 6 | 3 | 4 | 2 |
| 7 | 9 | 1 | 0 | 5 | 8 | 3 | 6 | 2 | 4 |
| 7 | 1 | 9 | 5 | 0 | 3 | 8 | 2 | 6 | 4 |
| 1 | 7 | 5 | 9 | 3 | 0 | 2 | 8 | 4 | 6 |
| 1 | 5 | 7 | 3 | 9 | 2 | 0 | 4 | 8 | 6 |

Extension IV

| | | | | | | | | |
|---|---|----|----|----|----|----|----|----------|
| A | B | C | D | E | F | G | H | Ad. inf. |
| 5 | 9 | 13 | 17 | 21 | 25 | 29 | 33 | |

| | | | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 11 | 14 | 13 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 12 | 9 | 14 | 11 | 13 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 12 | 7 | 14 | 9 | 13 | 11 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | 12 | 5 | 14 | 7 | 13 | 9 | 11 |
| 6 | 4 | 8 | 2 | 0 | 1 | 12 | 3 | 14 | 5 | 13 | 7 | 11 | 9 |
| 6 | 8 | 4 | 0 | 2 | 12 | 1 | 3 | 5 | 14 | 7 | 13 | 9 | 11 |
| 8 | 6 | 0 | 4 | 12 | 2 | 3 | 1 | 14 | 5 | 13 | 7 | 11 | 9 |
| 6 | 8 | 4 | 0 | 2 | 12 | 3 | 14 | 1 | 13 | 5 | 11 | 7 | 9 |
| 8 | 6 | 0 | 4 | 12 | 2 | 14 | 3 | 13 | 1 | 11 | 5 | 9 | 7 |
| 8 | 0 | 6 | 12 | 4 | 14 | 2 | 13 | 3 | 11 | 1 | 9 | 5 | 7 |
| 0 | 8 | 12 | 6 | 14 | 4 | 13 | 2 | 11 | 3 | 9 | 1 | 7 | 5 |
| 0 | 12 | 8 | 14 | 6 | 13 | 4 | 11 | 2 | 9 | 3 | 7 | 1 | 5 |
| 12 | 0 | 14 | 8 | 13 | 6 | 11 | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 12 | 14 | 0 | 13 | 8 | 11 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| 14 | 12 | 13 | 0 | 11 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 1 | 3 |
| 14 | 13 | 12 | 11 | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 1 | 2 | 3 |
| 13 | 14 | 11 | 12 | 9 | 0 | 7 | 8 | 5 | 6 | 4 | 3 | 2 | 1 |
| 13 | 11 | 14 | 9 | 12 | 7 | 0 | 5 | 8 | 6 | 3 | 4 | 2 | 1 |
| 11 | 13 | 9 | 14 | 7 | 12 | 5 | 0 | 8 | 3 | 6 | 2 | 4 | 1 |
| 13 | 11 | 14 | 9 | 12 | 7 | 5 | 0 | 3 | 8 | 2 | 6 | 4 | 1 |
| 11 | 13 | 9 | 14 | 7 | 12 | 5 | 3 | 0 | 2 | 8 | 4 | 6 | 1 |
| 11 | 9 | 13 | 7 | 14 | 12 | 5 | 0 | 3 | 8 | 2 | 6 | 4 | 1 |
| 9 | 11 | 7 | 13 | 14 | 5 | 12 | 3 | 0 | 2 | 8 | 4 | 6 | 1 |
| 9 | 7 | 11 | 13 | 5 | 14 | 3 | 12 | 2 | 0 | 4 | 8 | 6 | 1 |

If these four Extensions are tested they will be found to be true progressions in every feature. There are four of them for a similar reason that there are four Extensions of Forward Minor*

* See pp. 278-283.

These Shuntis are:-

| | | | | | | | | |
|----|---|---|---|---|---|---|---|----|
| | 2 | 3 | 4 | 5 | 6 | 7 | 8 | |
| | 2 | 4 | 3 | 6 | 5 | 8 | 7 | A1 |
| | 2 | 4 | 3 | 5 | 6 | 7 | 8 | |
| A2 | 4 | 2 | 3 | 6 | 5 | 8 | 7 | B1 |
| | 2 | 4 | 3 | 6 | 5 | 7 | 8 | |
| B2 | 4 | 2 | 6 | 3 | 5 | 8 | 7 | |
| | 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| | 4 | 2 | 6 | 3 | 8 | 5 | 7 | |

1. Those made in the two positions next the Huntis Whole full Before;

2. Those made in the two positions next the Huntis Whole full Behind;

3. Those made in the two positions midway between the Huntis Whole full Before and Behind;

4. Those made in every possible position;

5. Those made in the position next the Huntis Whole full Before, and the Huntis Whole full Behind.

| | | | | | | | | |
|-----|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | |
| A2 | 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| | 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |
| B2 | 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 |
| | 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 |
| | 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| | 4 | 6 | 2 | 8 | 3 | 7 | 5 | 1 |
| BB2 | 6 | 4 | 8 | 2 | 7 | 3 | 1 | 5 |
| | 4 | 6 | 2 | 8 | 7 | 1 | 3 | 5 |
| AA2 | 6 | 4 | 8 | 2 | 1 | 7 | 5 | 3 |
| | 4 | 6 | 8 | 1 | 2 | 7 | 3 | 5 |
| | 6 | 4 | 1 | 8 | 7 | 2 | 5 | 3 |
| | 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| | 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |
| | 1 | 8 | 6 | 7 | 4 | 5 | 2 | 3 |

| | | | | | | | | | | |
|-----|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | |
| A1 | 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| | 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 |
| B1 | 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 |
| | 2 | 4 | 3 | 6 | 5 | 8 | 1 | 0 | 7 | 9 |
| | 4 | 2 | 6 | 3 | 8 | 5 | 0 | 1 | 9 | 7 |
| | 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 1 | 7 |
| | 6 | 4 | 8 | 2 | 0 | 3 | 9 | 5 | 7 | 1 |
| | 6 | 8 | 4 | 0 | 2 | 9 | 3 | 7 | 5 | 1 |
| | 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 1 | 5 |
| | 8 | 0 | 6 | 9 | 4 | 7 | 2 | 1 | 3 | 5 |
| | 0 | 8 | 9 | 6 | 7 | 4 | 1 | 2 | 5 | 3 |
| | 8 | 0 | 6 | 9 | 7 | 1 | 4 | 5 | 2 | 3 |
| | 0 | 8 | 9 | 6 | 1 | 7 | 5 | 4 | 3 | 2 |
| BB1 | 8 | 0 | 9 | 1 | 6 | 7 | 4 | 5 | 2 | 3 |
| | 0 | 8 | 1 | 9 | 7 | 6 | 5 | 4 | 3 | 2 |
| AA1 | 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| | 1 | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |

Extension I.

| | | | | | | | | |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|----------|
| <u>AB</u> | <u>AB</u> | <u>AB</u> | <u>AB</u> | <u>AB</u> | <u>AB</u> | <u>AB</u> | <u>AB</u> | |
| 7 | 9 | 11 | 13 | 15 | 17 | 21 | 23 | Ad. Inf. |

| | | | | | | | | | | | | |
|-----|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| A1 | 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| | 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T |
| B1 | 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | T | E |
| | 2 | 4 | 3 | 6 | 5 | 8 | 1 | 0 | 7 | T | 9 | E |
| | 4 | 2 | 6 | 3 | 8 | 5 | 0 | 1 | T | 7 | E | 9 |
| | 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | 1 | E | 7 | 9 |
| | 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 1 | 9 | 7 |
| | 6 | 8 | 4 | 0 | 2 | T | 3 | E | 5 | 9 | 1 | 7 |
| | 8 | 6 | 0 | 4 | T | 2 | E | 3 | 9 | 5 | 7 | 1 |
| | 8 | 0 | 6 | T | 4 | E | 2 | 9 | 3 | 7 | 5 | 1 |
| | 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 3 | 1 | 5 |
| | 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 1 | 3 | 5 |
| | T | 0 | E | 8 | 9 | 6 | 7 | 4 | 1 | 2 | 5 | 3 |
| | T | E | 0 | 9 | 8 | 7 | 6 | 1 | 4 | 5 | 2 | 3 |
| BA2 | E | T | 9 | 0 | 7 | 8 | 1 | 6 | 5 | 4 | 3 | 2 |
| | T | E | 0 | 9 | 7 | 1 | 8 | 5 | 6 | 3 | 4 | 2 |
| AB2 | E | T | 9 | 0 | 1 | 7 | 5 | 8 | 3 | 6 | 2 | 4 |
| | T | E | 9 | 1 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |
| | E | T | 1 | 9 | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 |
| AA1 | E | T | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 | |
| | E | 9 | T | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 | |
| | 1 | 9 | E | 7 | T | 5 | 0 | 3 | 8 | 2 | 6 | 4 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | 1 |
| 6 | 4 | 8 | 2 | 7 | 3 | 1 | 5 |
| 4 | 6 | 2 | 8 | 7 | 1 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 5 | 3 | 1 |
| 4 | 6 | 8 | 1 | 2 | 7 | 3 | 5 |
| 6 | 4 | 8 | 7 | 2 | 5 | 3 | 1 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |
| 1 | 8 | 6 | 7 | 4 | 5 | 2 | 3 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 3 | 5 | 0 | 7 | 9 |
| 6 | 4 | 8 | 2 | 3 | 1 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | 5 | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | 5 | 1 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 1 | 7 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 5 | 7 | 1 |
| 6 | 8 | 4 | 0 | 2 | 9 | 3 | 7 | 5 | 1 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 1 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 7 | 1 | 3 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 1 | 7 | 5 | 3 |
| 6 | 8 | 4 | 0 | 9 | 1 | 2 | 7 | 3 | 5 |
| 8 | 6 | 0 | 4 | 1 | 9 | 7 | 2 | 5 | 3 |
| 8 | 0 | 6 | 1 | 4 | 9 | 2 | 7 | 3 | 5 |
| 0 | 8 | 1 | 6 | 9 | 4 | 7 | 2 | 5 | 3 |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| 1 | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |

Extension II.

| | | | | | | |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| <u>AB</u> | <u>BC</u> | <u>CD</u> | <u>DE</u> | <u>EF</u> | <u>FG</u> | <u>GH</u> |
| 7 | 9 | 11 | 13 | 15 | 17 | 19 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 1 | 3 | 5 | E | 7 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | 3 | 1 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 1 | 5 | 7 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 1 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 5 | 9 | 1 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 9 | 5 | 7 | 1 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 3 | 7 | 5 | 1 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 3 | 1 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 7 | 1 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 1 | 7 | 5 | 3 |
| 8 | 0 | 6 | T | 4 | E | 9 | 1 | 2 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 1 | 9 | 7 | 2 | 5 | 3 |
| 0 | T | 8 | E | 6 | 1 | 4 | 9 | 2 | 7 | 3 | 5 |
| T | 0 | E | 8 | 1 | 6 | 9 | 4 | 7 | 2 | 5 | 3 |
| T | E | 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| E | T | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| E | T | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 | 1 |
| E | 9 | T | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 | 1 |
| 1 | 9 | E | 7 | T | 5 | 0 | 3 | 8 | 2 | 6 | 4 |

| | | | | | | | | |
|-----|---|---|---|---|---|---|---|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | A1 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | |
| A2 | 4 | 2 | 3 | 1 | 6 | 5 | 8 | B1 |
| | 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |
| B2 | 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 |
| | 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 |
| | 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| | 4 | 6 | 2 | 8 | 3 | 7 | 5 | 1 |
| BB2 | 6 | 4 | 8 | 2 | 7 | 3 | 1 | 5 |
| | 4 | 6 | 2 | 8 | 7 | 1 | 3 | 5 |
| AA1 | 6 | 4 | 8 | 2 | 1 | 7 | 5 | 3 |
| | 4 | 6 | 8 | 1 | 2 | 7 | 3 | 5 |
| | 6 | 4 | 1 | 8 | 7 | 2 | 5 | 3 |
| | 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| | 6 | 8 | 4 | 7 | 2 | 5 | 3 | |
| | 1 | 8 | 6 | 7 | 4 | 5 | 2 | 3 |

Extension III

| | | | | | |
|----------------|-----------------|-----------------|-----------------|-----------------|----------|
| $\frac{AB}{7}$ | $\frac{BC}{11}$ | $\frac{CD}{15}$ | $\frac{DE}{19}$ | $\frac{EF}{23}$ | ad. Inf. |
|----------------|-----------------|-----------------|-----------------|-----------------|----------|

Extension IV see page. 306.

| | | | | |
|----------------|-----------------|-------------------|--------------------|---------------------|
| $\frac{AB}{7}$ | $\frac{ABC}{9}$ | $\frac{ABCD}{11}$ | $\frac{ABCDE}{13}$ | $\frac{ABCDEF}{15}$ |
|----------------|-----------------|-------------------|--------------------|---------------------|

| | | | | | | | | | | | | |
|-----|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | |
| B1 | 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| | 4 | 6 | 2 | 8 | 1 | 3 | 0 | 7 | T | 9 | E | |
| B2 | 6 | 4 | 8 | 2 | 3 | 1 | 0 | 5 | T | 7 | E | 9 |
| | 4 | 6 | 2 | 8 | 3 | 0 | 1 | 5 | 7 | T | 9 | E |
| C2 | 6 | 4 | 8 | 2 | 0 | 3 | 5 | 1 | T | 7 | E | 9 |
| | 4 | 6 | 2 | 8 | 3 | 0 | 5 | 1 | E | 7 | 9 | |
| | 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 1 | 9 | 7 |
| | 6 | 8 | 4 | 0 | 2 | T | 3 | E | 5 | 9 | 1 | 7 |
| | 8 | 6 | 0 | 4 | T | 2 | E | 3 | 9 | 5 | 7 | 1 |
| | 8 | 0 | 6 | T | 4 | E | 2 | 9 | 3 | 7 | 5 | 1 |
| | 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 3 | 1 | 5 |
| | 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 1 | 3 | 5 |
| CC2 | T | 0 | E | 8 | 9 | 6 | 7 | 4 | 1 | 2 | 5 | 3 |
| | 0 | T | 8 | E | 6 | 9 | 7 | 1 | 4 | 5 | 2 | 3 |
| BB2 | T | 0 | E | 8 | 9 | 6 | 1 | 7 | 5 | 4 | 3 | 2 |
| | 0 | T | 8 | E | 9 | 1 | 6 | 7 | 4 | 5 | 2 | 3 |
| | T | 0 | E | 8 | 1 | 9 | 7 | 6 | 5 | 4 | 3 | 2 |
| | T | E | 0 | 1 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 |
| | E | T | 1 | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 |
| | E | 1 | T | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |
| | E | 9 | T | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 | |
| | 1 | 9 | E | 7 | T | 5 | 0 | 3 | 8 | 2 | 6 | 4 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | 1 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 4 | 6 | 2 | 8 | 7 | 1 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 5 | 3 | 1 |
| 4 | 6 | 8 | 2 | 7 | 3 | 5 | 1 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |
| 4 | 8 | 6 | 7 | 4 | 5 | 2 | 3 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 8 | 1 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | 5 | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | 5 | 1 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 1 | 7 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 5 | 7 | 1 |
| 6 | 8 | 4 | 0 | 2 | 9 | 3 | 7 | 5 | 1 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 1 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 7 | 1 | 3 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 5 | 3 | 1 |
| 8 | 0 | 6 | 9 | 4 | 1 | 2 | 7 | 3 | 5 |
| 0 | 8 | 9 | 6 | 1 | 4 | 7 | 2 | 5 | 3 |
| 8 | 0 | 9 | 1 | 6 | 7 | 4 | 5 | 2 | 3 |
| 0 | 8 | 1 | 9 | 7 | 6 | 5 | 4 | 3 | 2 |
| 0 | 1 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 |
| 1 | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 |
| 4 | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 3 | 8 | 1 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 1 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 1 | 5 | 7 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 1 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 5 | 9 | 1 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 9 | 5 | 7 | 1 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 3 | 7 | 5 | 1 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 3 | 1 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 7 | 1 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 5 | 3 | 1 |
| 0 | T | 8 | E | 6 | 9 | 4 | 1 | 2 | 7 | 3 | 5 |
| T | 0 | E | 8 | 9 | 6 | 1 | 4 | 7 | 2 | 5 | 3 |
| T | E | 0 | 9 | 8 | 1 | 6 | 7 | 4 | 5 | 2 | 3 |
| E | T | 9 | 0 | 1 | 8 | 7 | 6 | 5 | 4 | 3 | 2 |
| T | E | 9 | 1 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |
| E | T | 1 | 9 | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 |
| E | T | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 | 1 |
| E | 9 | T | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 | 1 |
| 1 | 9 | E | 7 | T | 5 | 0 | 3 | 8 | 2 | 6 | 4 |

Extension √

| | | | | | | | |
|----------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|---------|
| $\frac{AB}{7}$ | $\frac{AC}{9}$ | $\frac{AD}{11}$ | $\frac{AE}{13}$ | $\frac{AF}{15}$ | $\frac{AG}{17}$ | $\frac{AH}{19}$ | Ad. mt. |
|----------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|---------|

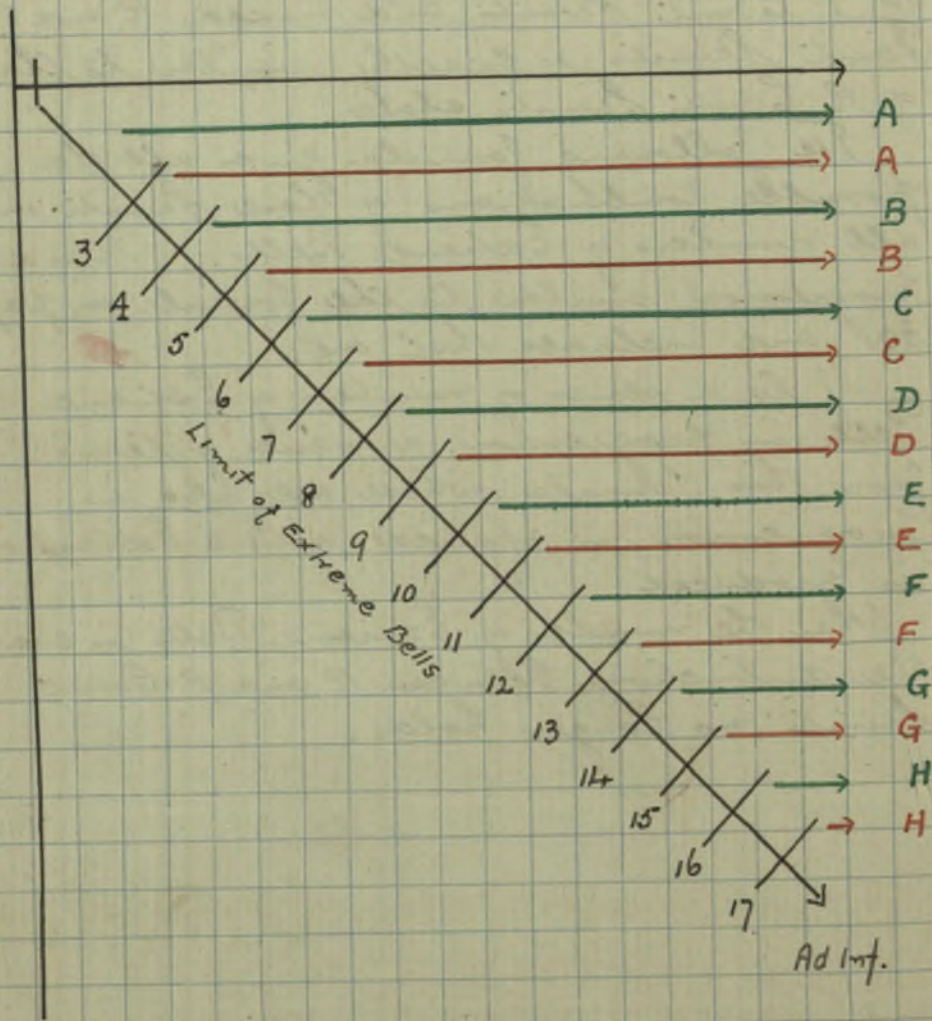
All Court Shunts are essentially the same things; the difference between R and P Court Shunts being a matter chiefly of classification. Therefore the Extension of P Court Shunts and mixed R and P Court Shunts, is exactly similar to that of R Court Shunts alone.

The following formula gives all the possible combinations of these Shunts on all numbers of Extreme Bells. It is a progression similar to the formula on page 301 and includes that one.

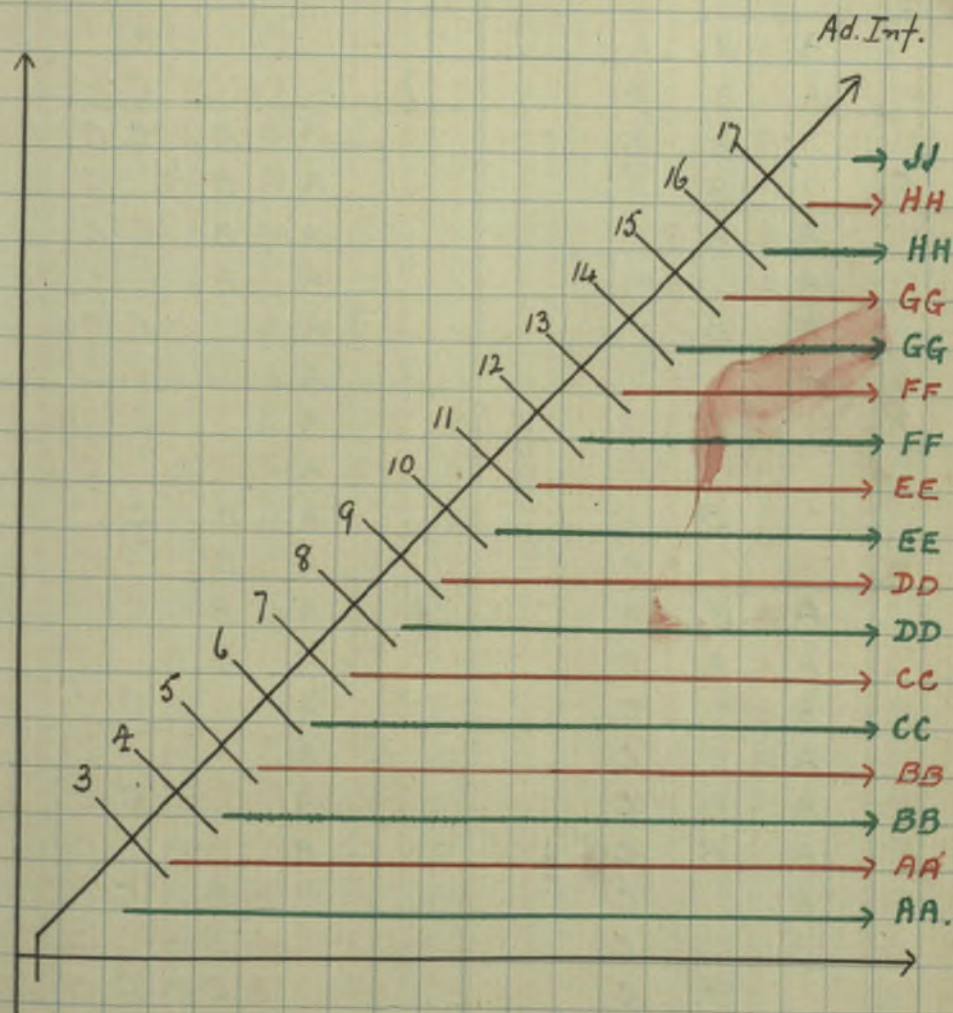
If to a series of numbers of Extreme Bells in progression, a series of terms from this formula, which are also in progression, is applied, a true Extension is produced.

When the number of Extreme Bells is even the distinction between R and P Court Shunts no longer holds.

Mixed R and P COURT SHUNTS
 Hunt Ascending



Hunt decending



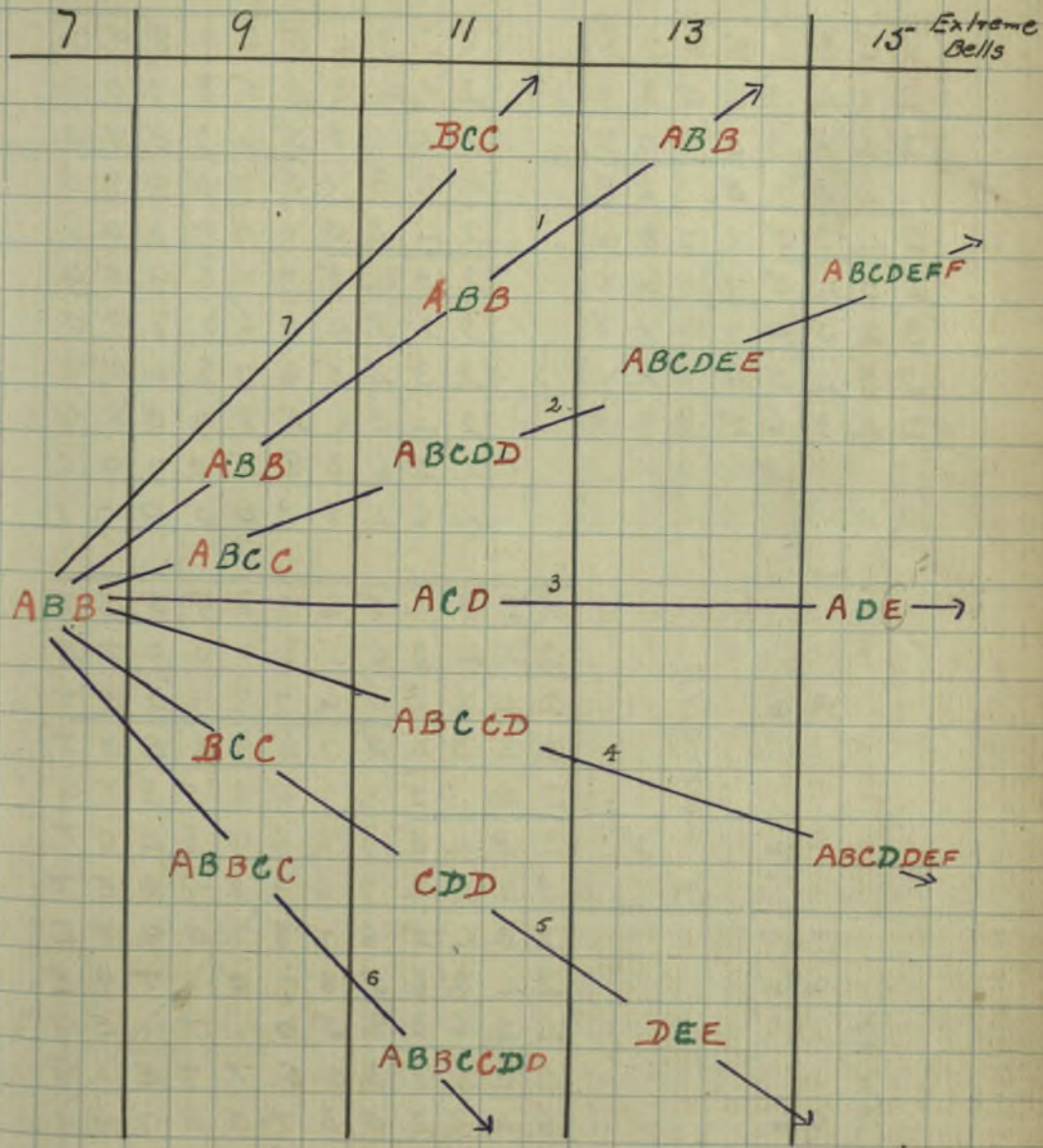
LIMIT OF
EXTREME
BELLS.

| | | | |
|---|-------------|-------------|---|
| 3 | A | A | C |
| | A A | B B C | |
| 4 | A | B C | |
| | A A B | B C | |
| 5 | A B | C | |
| | A A B B C C | A A B B C C | |
| 6 | A A B B C C | A A B B C C | |
| | A A B C C | A A B C C | |
| 7 | A A B C C | A A B C C | |
| | A A B C C | A A B C C | |
| 8 | A A B C C | A A B C C | |
| | A A B C C | A A B C C | |

| | | | |
|----|---------------|-------------|---|
| 3 | A B C | A A | D |
| | A C C | A B B C C D | |
| 4 | A C | A B B C D | |
| | B B C C | A B B C D | |
| 5 | B B C C | A B B C D | |
| | B C C | A B C C D | |
| 6 | B C C | A B C D | |
| | B C | A B C D | |
| 7 | C C | A B C D | |
| | C | A B C D | |
| 8 | A A B B C C D | A B C C D | |
| | A A B B C D | A B C D | |
| 9 | A A B B C D | A B C D | |
| | A A B C C D | A B C D | |
| 10 | A A B C D | A B C D | |
| | A A B C D | A B C D | |
| 11 | A A B C D | A B C D | |
| | A A B C D | A B C D | |
| 12 | A A B C D | A B C D | |
| | A A B C D | A B C D | |
| 13 | A A B C D | A B C D | |
| | A A B C D | A B C D | |
| 14 | A A B C D | A B C D | |
| | A A B C D | A B C D | |
| 15 | A A B C D | A B C D | |
| | A A B C D | A B C D | |

Ad. Int.

Example of Extension from Formula. p. 315



| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 8 |
| 2 | 4 | 3 | 5 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 1 |

A2
B2
B2

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | 0 |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | 0 | 8 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | 0 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 | 9 | 0 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 0 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 7 | 1 |

A1
B1
B1

7 ABB
9 ABB
11 ABB
13 ABB
15 ABB
Ad Int.

Extension I.

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | E | 0 | T |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | E | 8 | T | 0 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | E | 0 | T |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 | 9 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | T | 9 | E |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | E | 9 | 1 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | 7 | E | 1 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 | 1 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 5 | 9 | 7 | 1 |

A1
B1
B1

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 8 |
| 2 | 4 | 3 | 5 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 1 |

A2
B2
B2

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | 0 |
| 2 | 4 | 3 | 5 | 1 | 6 | 7 | 8 | 9 | 0 |
| 2 | 3 | 4 | 5 | 6 | 1 | 7 | 9 | 8 | 0 |
| 2 | 4 | 3 | 6 | 5 | 7 | 1 | 9 | 0 | 8 |
| 2 | 3 | 4 | 5 | 6 | 7 | 9 | 1 | 8 | 0 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 1 | 0 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | 1 |

A1
B1
B1
A2
B2
C2
C2

7 ABB
9 ABCC
11 ABCCD
13 ABCDE
Ad Int.

Extension II

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | E | 0 | T |
| 2 | 4 | 3 | 5 | 1 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 1 | 7 | 9 | 8 | E | 0 | T |
| 2 | 4 | 3 | 6 | 5 | 7 | 1 | 8 | 9 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 9 | E | 0 | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 9 | 1 | E | T | 0 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | E | 1 | 0 | T |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | E | 0 | 1 | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | 1 |

A2
B2
C2
D2
D2

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 8 |
| 2 | 4 | 3 | 5 | 1 | 7 | 8 | 6 |
| 1 | 3 | 4 | 5 | 7 | 6 | 1 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 1 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 9 | 8 | 0 | E | T |
| 4 | 2 | 6 | 3 | 5 | 1 | 7 | 9 | 8 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 7 | 1 | 9 | 8 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 9 | 1 | 8 | 0 | E | T |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 1 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | 1 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 0 | E | T | 1 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | 1 |

Extension IV.

ABB 7

ABCCD 11

ABCDEEF 15

ABCDEEFGH 19

Ad. inf.

Extension VI.

ABB 7

ABBCC 9

ABBCCDD 11

Ad. inf.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 8 |
| 2 | 4 | 3 | 5 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 1 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | E | 0 | T |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | E | 8 | T | 0 |
| 2 | 3 | 4 | 5 | 7 | 1 | 9 | E | 6 | T | 8 | 0 |
| 3 | 2 | 5 | 4 | 7 | 9 | 1 | E | T | 6 | 0 | 8 |
| 3 | 5 | 2 | 7 | 4 | 9 | E | 1 | T | 0 | 6 | 8 |
| 5 | 3 | 7 | 2 | 9 | 4 | E | T | 1 | 0 | 8 | 6 |
| 5 | 7 | 3 | 9 | 2 | E | 4 | T | 0 | 1 | 6 | 8 |
| 7 | 5 | 9 | 3 | E | 2 | T | 4 | 0 | 6 | 1 | 8 |
| 5 | 7 | 3 | 9 | 2 | E | 4 | T | 6 | 0 | 8 | 1 |
| 5 | 3 | 7 | 2 | 9 | 4 | E | 6 | T | 8 | 0 | 1 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | 0 |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | 0 | 8 |
| 2 | 3 | 4 | 5 | 7 | 1 | 9 | 0 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 9 | 1 | 0 | 8 | 6 |
| 3 | 5 | 2 | 7 | 4 | 9 | 0 | 1 | 6 | 8 |
| 5 | 3 | 7 | 2 | 9 | 4 | 0 | 6 | 1 | 8 |
| 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 | 1 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 0 | 1 |

As Single Count Shunts are identical with Count Shunts, (except that the second portion of each member is made above the Hount when that bell is descending, instead of below the Hount when that bell is ascending,) the formulae given on pages 301 and 314 will produce the total number of combinations possible on all numbers of bells, and will also give every full Extension. Only those terms in the formulae which are symmetrical about a point midway between the Hounts whose pulls before and behind, will give symmetrical combinations of Single Count Shunts. The ordinarily accepted rules for producing Single variations of Method are constitutionally not quite sound.

Reverse Count Shunts extend similarly to Single Count Shunts.

Slow Work Shunts divide the total number of Bells into.

- (a) Slow Work Bells;
 - (b) Other Bells.
- (a) are Shunts of a secondary cycle;
- (b) are Extreme Bells of the same cycle.

The omission of one Member of this secondary cycle becomes one Member of the Constitutional Shunt of the Method.

The Constitutional Shunt divides the total number of bells into

- (c) Shunts
- (d) Extreme Bells.

The second division is a different one from the first.

By the nature of cyclical movement, each cycle included in the above can expand in regular progression as the number of bells involved in it. Since the ratio of expansion of the cycles is different, the expansion of the Method will necessarily be unequal.

The following formula gives every Slow Work Shunt on all numbers to infinity.

In the formula the top figure in each term represents the number of Slow Work Bells, and the bottom figure the number of other Bells. Thus $\frac{4}{5}$ represents four Slow Work Bells and five other Bells in a method on nine Bells.

The Extension of the
SLOW WORK CONSTRUCTIONAL SHUNTS

| | | | | | | | | | |
|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|-----------------|-----------------|
| | $\frac{1}{3}$ | $\frac{1}{4}$ | $\frac{1}{5}$ | $\frac{1}{6}$ | $\frac{1}{7}$ | $\frac{1}{8}$ | $\frac{1}{9}$ | $\frac{1}{10}$ | $\frac{1}{11}$ |
| $\frac{2}{2}$ | $\frac{2}{3}$ | $\frac{2}{4}$ | $\frac{2}{5}$ | $\frac{2}{6}$ | $\frac{2}{7}$ | $\frac{2}{8}$ | $\frac{2}{9}$ | $\frac{2}{10}$ | $\frac{2}{11}$ |
| $\frac{3}{2}$ | $\frac{3}{3}$ | $\frac{3}{4}$ | $\frac{3}{5}$ | $\frac{3}{6}$ | $\frac{3}{7}$ | $\frac{3}{8}$ | $\frac{3}{9}$ | $\frac{3}{10}$ | $\frac{3}{11}$ |
| $\frac{4}{2}$ | $\frac{4}{3}$ | $\frac{4}{4}$ | $\frac{4}{5}$ | $\frac{4}{6}$ | $\frac{4}{7}$ | $\frac{4}{8}$ | $\frac{4}{9}$ | $\frac{4}{10}$ | $\frac{4}{11}$ |
| $\frac{5}{2}$ | $\frac{5}{3}$ | $\frac{5}{4}$ | $\frac{5}{5}$ | $\frac{5}{6}$ | $\frac{5}{7}$ | $\frac{5}{8}$ | $\frac{5}{9}$ | $\frac{5}{10}$ | $\frac{5}{11}$ |
| $\frac{6}{2}$ | $\frac{6}{3}$ | $\frac{6}{4}$ | $\frac{6}{5}$ | $\frac{6}{6}$ | $\frac{6}{7}$ | $\frac{6}{8}$ | $\frac{6}{9}$ | $\frac{6}{10}$ | $\frac{6}{11}$ |
| $\frac{7}{2}$ | $\frac{7}{3}$ | $\frac{7}{4}$ | $\frac{7}{5}$ | $\frac{7}{6}$ | $\frac{7}{7}$ | $\frac{7}{8}$ | $\frac{7}{9}$ | $\frac{7}{10}$ | $\frac{7}{11}$ |
| $\frac{8}{2}$ | $\frac{8}{3}$ | $\frac{8}{4}$ | $\frac{8}{5}$ | $\frac{8}{6}$ | $\frac{8}{7}$ | $\frac{8}{8}$ | $\frac{8}{9}$ | $\frac{8}{10}$ | $\frac{8}{11}$ |
| $\frac{9}{2}$ | $\frac{9}{3}$ | $\frac{9}{4}$ | $\frac{9}{5}$ | $\frac{9}{6}$ | $\frac{9}{7}$ | $\frac{9}{8}$ | $\frac{9}{9}$ | $\frac{9}{10}$ | $\frac{9}{11}$ |
| $\frac{10}{2}$ | $\frac{10}{3}$ | $\frac{10}{4}$ | $\frac{10}{5}$ | $\frac{10}{6}$ | $\frac{10}{7}$ | $\frac{10}{8}$ | $\frac{10}{9}$ | $\frac{10}{10}$ | $\frac{10}{11}$ |

Ad. int.

As a Slow Work Shunt puts the Shunt backwards as many positions in Counting Order as there are Slow Work Bells, to find the Lead End produced by any term in the preceding formula, transpose the previous Lead End by 4263850.... as many times as there are Slow Work Bells.

Thus from Rounds $\frac{3}{5}$ produces:-
 1 2 3 4 5 6 7 8 * (4263857)³ = 18674523

Slow Work Shunts in their original state, are never used in practical methods. Additional Shunts must be made to prevent the bells lying still for more than five consecutive blows in any one position. These Additional Shunts cannot be applied equally to all numbers of Slow Work Bells. Therefore many of the Extensions given on page 321. are of no use in practical methods.

The following will serve as illustrations of the Extension of Slow Work Shunts.

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 2 | 1 | 4 | 3 |
| 2 | 4 | 1 | 3 |
| 2 | 4 | 3 | 1 |
| 2 | 3 | 4 | 1 |
| 2 | 3 | 1 | 4 |
| 2 | 1 | 3 | 4 |
| 1 | 4 | 2 | 3 |

| | | | | |
|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 |
| 2 | 1 | 4 | 3 | 5 |
| 2 | 4 | 1 | 5 | 3 |
| 2 | 4 | 5 | 1 | 3 |
| 2 | 5 | 4 | 3 | 1 |
| 2 | 5 | 3 | 4 | 1 |
| 2 | 3 | 5 | 1 | 4 |
| 2 | 3 | 1 | 5 | 4 |
| 2 | 1 | 3 | 4 | 5 |
| 1 | 4 | 2 | 5 | 3 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 2 | 4 | 6 | 1 | 5 | 3 |
| 2 | 6 | 4 | 5 | 1 | 3 |
| 2 | 6 | 5 | 4 | 3 | 1 |
| 2 | 5 | 6 | 3 | 4 | 1 |
| 2 | 5 | 3 | 6 | 1 | 4 |
| 2 | 3 | 5 | 1 | 6 | 4 |
| 2 | 3 | 1 | 5 | 4 | 6 |
| 2 | 1 | 3 | 4 | 5 | 6 |
| 1 | 4 | 2 | 6 | 3 | 5 |

| | | | | | | |
|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 2 | 1 | 4 | 3 | 6 | 5 | 7 |
| 2 | 4 | 1 | 6 | 3 | 7 | 5 |
| 2 | 4 | 6 | 1 | 7 | 3 | 5 |
| 2 | 6 | 4 | 7 | 1 | 5 | 3 |
| 2 | 6 | 7 | 4 | 5 | 1 | 3 |
| 2 | 7 | 6 | 5 | 4 | 3 | 1 |
| 2 | 7 | 5 | 6 | 3 | 4 | 1 |
| 2 | 5 | 7 | 3 | 6 | 1 | 4 |
| 2 | 5 | 3 | 7 | 1 | 6 | 4 |
| 2 | 3 | 5 | 1 | 7 | 4 | 6 |
| 2 | 3 | 1 | 5 | 4 | 7 | 6 |
| 2 | 1 | 3 | 4 | 5 | 6 | 7 |
| 1 | 4 | 2 | 6 | 3 | 7 | 5 |

Example I

$\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{5}$ $\frac{1}{6}$ $\frac{1}{7}$ $\frac{1}{8}$ $\frac{1}{9}$ $\frac{1}{10}$ $\frac{1}{11}$ $\frac{1}{12}$

Ad. Inf.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 2 | 4 | 6 | 1 | 8 | 3 | 7 | 5 |
| 2 | 6 | 4 | 8 | 1 | 7 | 3 | 5 |
| 2 | 6 | 8 | 4 | 7 | 1 | 5 | 3 |
| 2 | 8 | 6 | 7 | 4 | 5 | 1 | 3 |
| 2 | 8 | 7 | 6 | 5 | 4 | 3 | 1 |
| 2 | 7 | 8 | 5 | 6 | 3 | 4 | 1 |
| 2 | 7 | 5 | 8 | 3 | 6 | 1 | 4 |
| 2 | 5 | 7 | 3 | 8 | 1 | 6 | 4 |
| 2 | 5 | 3 | 7 | 1 | 8 | 4 | 6 |
| 2 | 3 | 5 | 1 | 7 | 4 | 8 | 6 |
| 2 | 3 | 1 | 5 | 4 | 7 | 6 | 8 |
| 2 | 1 | 3 | 4 | 5 | 6 | 7 | 8 |
| 1 | 4 | 2 | 6 | 3 | 8 | 5 | 7 |

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 9 | 7 |
| 2 | 4 | 6 | 1 | 8 | 3 | 9 | 5 | 7 |
| 2 | 6 | 4 | 8 | 1 | 9 | 3 | 7 | 5 |
| 2 | 6 | 8 | 4 | 9 | 1 | 7 | 3 | 5 |
| 2 | 8 | 6 | 9 | 4 | 7 | 1 | 5 | 3 |
| 2 | 8 | 9 | 6 | 7 | 4 | 5 | 1 | 3 |
| 2 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 1 |
| 2 | 9 | 7 | 8 | 5 | 6 | 3 | 4 | 1 |
| 2 | 7 | 9 | 5 | 8 | 3 | 6 | 1 | 4 |
| 2 | 7 | 5 | 9 | 3 | 8 | 1 | 6 | 4 |
| 2 | 5 | 7 | 3 | 9 | 1 | 8 | 4 | 6 |
| 2 | 5 | 3 | 7 | 1 | 9 | 4 | 8 | 6 |
| 2 | 3 | 5 | 1 | 7 | 4 | 9 | 6 | 8 |
| 2 | 3 | 1 | 5 | 4 | 7 | 6 | 9 | 8 |
| 2 | 1 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1 | 4 | 2 | 6 | 3 | 8 | 5 | 9 | 7 |

| | | | | |
|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 |
| 2 | 1 | 4 | 3 | 5 |
| 2 | 4 | 1 | 5 | 3 |
| 4 | 2 | 5 | 1 | 3 |
| 4 | 2 | 5 | 3 | 1 |
| 4 | 5 | 2 | 3 | 1 |
| 4 | 5 | 2 | 1 | 3 |
| 5 | 4 | 2 | 3 | 1 |
| 5 | 4 | 3 | 2 | 1 |
| 5 | 3 | 4 | 2 | 1 |
| 3 | 5 | 2 | 4 | 1 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 4 | 2 | 6 | 1 | 5 | 3 |
| 4 | 2 | 6 | 5 | 1 | 3 |
| 4 | 2 | 6 | 5 | 3 | 1 |
| 4 | 6 | 2 | 3 | 5 | 1 |
| 4 | 6 | 2 | 3 | 1 | 5 |
| 4 | 6 | 2 | 1 | 3 | 5 |
| 6 | 4 | 2 | 5 | 3 | 1 |
| 6 | 4 | 5 | 2 | 3 | 1 |
| 6 | 5 | 4 | 3 | 2 | 1 |
| 5 | 6 | 3 | 4 | 2 | 1 |

| | | | | | | |
|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 2 | 1 | 4 | 3 | 6 | 5 | 7 |
| 2 | 4 | 1 | 6 | 3 | 7 | 5 |
| 4 | 2 | 6 | 1 | 7 | 3 | 5 |
| 4 | 2 | 6 | 7 | 1 | 5 | 3 |
| 4 | 2 | 6 | 7 | 5 | 1 | 3 |
| 4 | 2 | 6 | 5 | 7 | 3 | 1 |
| 4 | 6 | 2 | 5 | 3 | 7 | 1 |
| 4 | 6 | 2 | 3 | 5 | 7 | 1 |
| 4 | 6 | 2 | 3 | 1 | 5 | 7 |
| 4 | 6 | 2 | 1 | 3 | 7 | 5 |
| 6 | 4 | 2 | 7 | 3 | 5 | 1 |
| 6 | 4 | 7 | 2 | 5 | 3 | 1 |
| 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 7 | 6 | 5 | 4 | 3 | 2 | 1 |

Example II

| | | | | | | | | | | |
|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|----------------|----------------|----------|
| $\frac{3}{2}$ | $\frac{3}{3}$ | $\frac{3}{4}$ | $\frac{3}{5}$ | $\frac{3}{6}$ | $\frac{3}{7}$ | $\frac{3}{8}$ | $\frac{3}{9}$ | $\frac{3}{10}$ | $\frac{3}{11}$ | Ad. int. |
|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|----------------|----------------|----------|

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 2 | 6 | 8 | 1 | 7 | 3 | 5 |
| 4 | 2 | 6 | 8 | 7 | 1 | 5 | 3 |
| 4 | 2 | 6 | 7 | 8 | 5 | 1 | 3 |
| 4 | 2 | 6 | 7 | 5 | 8 | 3 | 1 |
| 4 | 6 | 2 | 5 | 7 | 3 | 8 | 1 |
| 4 | 6 | 2 | 5 | 3 | 7 | 1 | 8 |
| 4 | 6 | 2 | 3 | 5 | 1 | 7 | 8 |
| 4 | 6 | 2 | 3 | 1 | 5 | 8 | 7 |
| 4 | 6 | 2 | 1 | 3 | 8 | 5 | 7 |
| 6 | 4 | 2 | 8 | 3 | 7 | 5 | 1 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |
| 8 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 9 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 9 | 5 | 7 |
| 4 | 2 | 6 | 8 | 1 | 9 | 3 | 7 | 5 |
| 4 | 2 | 6 | 8 | 9 | 1 | 7 | 3 | 5 |
| 4 | 2 | 6 | 9 | 8 | 7 | 1 | 5 | 3 |
| 4 | 2 | 6 | 9 | 7 | 8 | 5 | 1 | 3 |
| 4 | 2 | 6 | 7 | 9 | 5 | 8 | 3 | 1 |
| 4 | 6 | 2 | 7 | 5 | 9 | 3 | 8 | 1 |
| 4 | 6 | 2 | 5 | 7 | 3 | 9 | 1 | 8 |
| 4 | 6 | 2 | 5 | 3 | 7 | 1 | 9 | 8 |
| 4 | 6 | 2 | 3 | 5 | 7 | 8 | 9 | 1 |
| 4 | 6 | 2 | 3 | 1 | 5 | 8 | 7 | 9 |
| 4 | 6 | 2 | 1 | 3 | 8 | 5 | 9 | 7 |
| 6 | 4 | 2 | 8 | 3 | 9 | 5 | 7 | 1 |
| 6 | 4 | 8 | 2 | 9 | 3 | 7 | 5 | 1 |
| 6 | 8 | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 8 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 2 | 1 | 4 | 3 |
| 2 | 4 | 1 | 3 |
| 2 | 4 | 3 | 1 |
| 2 | 3 | 4 | |
| 2 | 3 | | 4 |
| 2 | 1 | 3 | 4 |
| 1 | 4 | 2 | 3 |

| | | | | |
|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 |
| 2 | 1 | 4 | 3 | 5 |
| 2 | 4 | 1 | 5 | 3 |
| 2 | 4 | 5 | 1 | 3 |
| 2 | 4 | 5 | 3 | 1 |
| 4 | 2 | 3 | 5 | |
| 4 | 2 | 3 | | 5 |
| 4 | 2 | 1 | 3 | 5 |
| 4 | 1 | 2 | 5 | 3 |
| 4 | 5 | 2 | 3 | |
| 1 | 5 | 4 | 3 | 2 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 4 | 2 | 6 | 1 | 5 | 3 |
| 4 | 2 | 6 | 5 | 1 | 3 |
| 4 | 2 | 6 | 5 | 3 | 1 |
| 4 | 6 | 2 | 3 | 5 | 1 |
| 4 | 6 | 2 | 3 | 1 | 5 |
| 4 | 6 | 2 | 1 | 3 | 5 |
| 6 | 4 | 2 | 5 | 3 | |
| 6 | 4 | 2 | 5 | 3 | |
| 6 | 1 | 4 | 5 | 2 | 3 |
| 6 | 5 | 4 | 3 | 2 | |
| 1 | 5 | 6 | 3 | 4 | 2 |

| | | | | | | |
|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 2 | 1 | 4 | 3 | 6 | 5 | 7 |
| 2 | 4 | 1 | 6 | 3 | 7 | 5 |
| 4 | 2 | 6 | 1 | 7 | 3 | 5 |
| 4 | 6 | 2 | 7 | 1 | 5 | 3 |
| 4 | 6 | 2 | 7 | 5 | 1 | 3 |
| 4 | 6 | 2 | 7 | 5 | 3 | 1 |
| 6 | 4 | 7 | 2 | 3 | 5 | 1 |
| 6 | 4 | 7 | 2 | 3 | 1 | 5 |
| 6 | 4 | 7 | 2 | 1 | 3 | 5 |
| 6 | 7 | 4 | 1 | 2 | 5 | 3 |
| 7 | 6 | 4 | 5 | 2 | 3 | |
| 7 | 6 | 5 | 4 | 3 | 2 | |
| 7 | 5 | 6 | 3 | 4 | 2 | |
| 1 | 5 | 7 | 3 | 6 | 2 | 4 |

Example III

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----------|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | |
| 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | Ad. int. |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 6 | 2 | 8 | 1 | 7 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 1 | 5 | 3 |
| 6 | 4 | 8 | 2 | 7 | 5 | 1 | 3 |
| 6 | 4 | 8 | 2 | 7 | 5 | 3 | 1 |
| 6 | 8 | 4 | 7 | 2 | 3 | 5 | 1 |
| 6 | 8 | 4 | 7 | 2 | 3 | 1 | 5 |
| 6 | 8 | 4 | 7 | 2 | 1 | 3 | 5 |
| 8 | 6 | 7 | 4 | 1 | 2 | 5 | 3 |
| 8 | 7 | 6 | 4 | 5 | 2 | 3 | |
| 7 | 8 | 6 | 5 | 4 | 3 | 2 | |
| 7 | 8 | 5 | 6 | 3 | 4 | 2 | |
| 7 | 5 | 8 | 3 | 6 | 2 | 4 | |
| 1 | 5 | 7 | 3 | 8 | 2 | 6 | 4 |

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 9 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 9 | 5 | 7 |
| 4 | 6 | 2 | 8 | 1 | 9 | 3 | 7 | 5 |
| 6 | 4 | 8 | 2 | 9 | 1 | 7 | 3 | 5 |
| 6 | 8 | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 6 | 8 | 4 | 9 | 2 | 7 | 5 | 1 | 3 |
| 6 | 8 | 4 | 9 | 2 | 7 | 5 | 3 | 1 |
| 8 | 6 | 9 | 4 | 7 | 2 | 3 | 5 | 1 |
| 8 | 6 | 9 | 4 | 7 | 2 | 3 | 1 | 5 |
| 8 | 6 | 9 | 4 | 7 | 2 | 1 | 3 | 5 |
| 8 | 9 | 6 | 7 | 4 | 1 | 2 | 5 | 3 |
| 9 | 8 | 7 | 6 | 4 | 5 | 2 | 3 | |
| 9 | 7 | 8 | 6 | 5 | 4 | 3 | 2 | |
| 7 | 9 | 8 | 5 | 6 | 3 | 4 | 2 | |
| 7 | 9 | 5 | 8 | 3 | 6 | 2 | 4 | |
| 7 | 5 | 9 | 3 | 8 | 2 | 6 | 4 | |
| 1 | 5 | 7 | 3 | 9 | 2 | 8 | 4 | 6 |

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 2 | 1 | 4 | 3 |
| 2 | 4 | 1 | 3 |
| 2 | 4 | 3 | 1 |
| 2 | 3 | 4 | 1 |
| 2 | 3 | 1 | 4 |
| 2 | 3 | 3 | 4 |
| 2 | 4 | 3 | 1 |
| 1 | 4 | 2 | 3 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 2 | 4 | 6 | 1 | 5 | 3 |
| 2 | 4 | 6 | 5 | 1 | 3 |
| 2 | 4 | 5 | 6 | 3 | 1 |
| 4 | 2 | 5 | 3 | 6 | 1 |
| 4 | 2 | 3 | 5 | 1 | 6 |
| 4 | 2 | 3 | 1 | 5 | 6 |
| 4 | 2 | 1 | 3 | 6 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 1 | 6 | 4 | 5 | 2 | 3 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 2 | 6 | 8 | 1 | 7 | 3 | 5 |
| 4 | 2 | 6 | 8 | 7 | 1 | 5 | 3 |
| 4 | 2 | 6 | 7 | 8 | 5 | 1 | 3 |
| 4 | 2 | 6 | 7 | 5 | 8 | 3 | 1 |
| 4 | 6 | 2 | 5 | 7 | 3 | 8 | 1 |
| 4 | 6 | 2 | 5 | 3 | 7 | 1 | 8 |
| 4 | 6 | 2 | 3 | 5 | 1 | 7 | 8 |
| 4 | 6 | 2 | 3 | 1 | 5 | 8 | 7 |
| 4 | 6 | 2 | 1 | 3 | 8 | 5 | 7 |
| 6 | 4 | 1 | 2 | 8 | 3 | 7 | 5 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | 1 |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |
| 1 | 8 | 6 | 7 | 4 | 5 | 2 | 3 |

Example IV.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 3 | 4 | 5 | 6 | 7 | 8 |

Ad. int.

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 4 | 6 | 2 | 8 | 0 | 1 | 9 | 3 | 7 | 5 |
| 4 | 6 | 2 | 8 | 0 | 9 | 1 | 7 | 3 | 5 |
| 4 | 6 | 2 | 8 | 9 | 0 | 7 | 1 | 5 | 3 |
| 4 | 6 | 2 | 8 | 9 | 7 | 0 | 5 | 1 | 3 |
| 4 | 6 | 2 | 8 | 7 | 9 | 5 | 0 | 3 | 1 |
| 6 | 4 | 8 | 2 | 7 | 5 | 9 | 3 | 0 | 1 |
| 6 | 4 | 8 | 2 | 5 | 7 | 3 | 9 | 1 | 0 |
| 6 | 4 | 8 | 2 | 5 | 3 | 7 | 1 | 9 | 0 |
| 6 | 4 | 8 | 2 | 3 | 5 | 1 | 7 | 0 | 9 |
| 6 | 4 | 8 | 2 | 3 | 5 | 0 | 7 | 9 | 1 |
| 6 | 4 | 8 | 2 | 1 | 3 | 0 | 5 | 9 | 7 |
| 6 | 8 | 4 | 1 | 2 | 0 | 3 | 9 | 5 | 7 |
| 8 | 6 | 4 | 0 | 2 | 9 | 3 | 7 | 5 | 1 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| 1 | 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 4 | 8 | 2 | 0 | T | 1 | E | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | T | E | 1 | 9 | 3 | 7 | 5 |
| 6 | 4 | 8 | 2 | 0 | E | T | 9 | 1 | 7 | 3 | 5 |
| 6 | 4 | 8 | 2 | 0 | E | 9 | T | 7 | 1 | 5 | 3 |
| 6 | 4 | 8 | 2 | 0 | 9 | E | 7 | T | 5 | 1 | 3 |
| 6 | 4 | 8 | 2 | 0 | 9 | 7 | E | 5 | T | 3 | 1 |
| 6 | 8 | 4 | 0 | 2 | 7 | 9 | 5 | E | 3 | T | 1 |
| 6 | 8 | 4 | 0 | 2 | 7 | 5 | 9 | 3 | E | 1 | T |
| 6 | 8 | 4 | 0 | 2 | 5 | 7 | 3 | 9 | 1 | E | T |
| 6 | 8 | 4 | 0 | 2 | 5 | 3 | 7 | 1 | 9 | T | E |
| 6 | 8 | 4 | 0 | 2 | 3 | 5 | 1 | 7 | T | 9 | E |
| 6 | 8 | 4 | 0 | 2 | 3 | 1 | 5 | T | 7 | E | 9 |
| 6 | 8 | 4 | 0 | 2 | 1 | 3 | T | 5 | E | 7 | 9 |
| 8 | 6 | 0 | 4 | 1 | 2 | T | 3 | E | 5 | 9 | 7 |
| 8 | 0 | 6 | 1 | 4 | T | 2 | E | 3 | 9 | 5 | 7 |
| 0 | 8 | 1 | 6 | T | 4 | E | 2 | 9 | 3 | 7 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 1 | 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 |
| 1 | T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 |

Note.

These two diagrams are similar in form and relative position of parts.

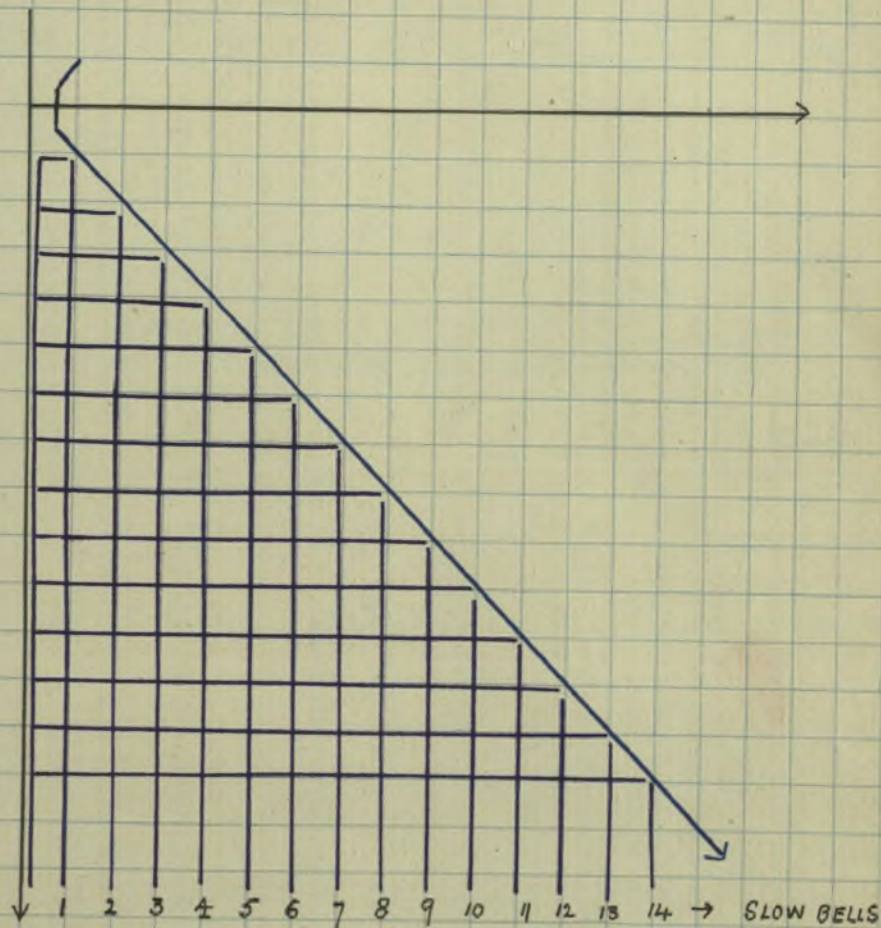
Should they not be "out of phase"?

J.E.

The first (red lines) should be "raised" one whole row, I think.

A.F.B.

The SLOW WORK CONSTRUCTIONAL SHUNTS.
on all numbers of Bells from four
to infinity.



Ad int.

Mixed Court Shunts and Slow Work

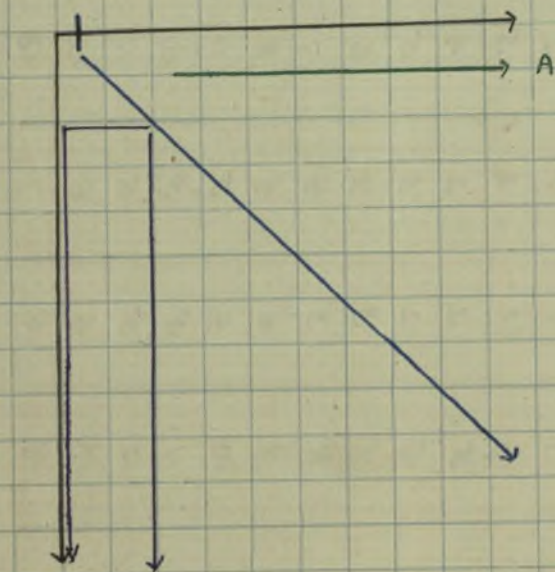
Shunts. In any Lead containing a Slow Work Shunt, the number of positions available for making Court Shunts depends solely on the number of Slow Work Bells and is irrespective of the total number of Bells.

| No of SLOW BELLS | No of Positions of P. Ct. Shunts | No of Positions of P. Ct. Shunts | Total No Positions of Court Shunts | on all numbers of Bells. |
|------------------|----------------------------------|----------------------------------|------------------------------------|--|
| 1 | 0 | 0 | 0 | The Court Shunts are with Hunt either ascending or descending. Double the Nos. for both. |
| 2 | 0 | 1 | 1 | |
| 3 | 1 | 1 | 2 | |
| 4 | 1 | 2 | 3 | |
| 5 | 2 | 2 | 4 | |
| 6 | 2 | 3 | 5 | |
| 7 | 3 | 3 | 6 | |
| 8 | 3 | 4 | 7 | |
| 9 | 4 | 4 | 8 | |
| 10 | 4 | 5 | 9 | |
| 11 | 5 | 5 | 10 | |
| 12 | 5 | 6 | 11 | |
| 13 | 6 | 6 | 12 | |
| 14 | 6 | 7 | 13 | |

Ad inf.

The total Number of mixed.
SLOW WORK and COURT SHUNTS
on all numbers of Bells.

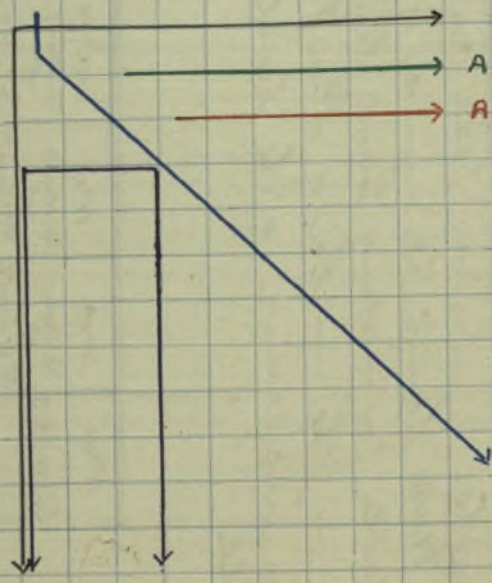
1. 2 Bell. S.W. Shunt.



Combinations

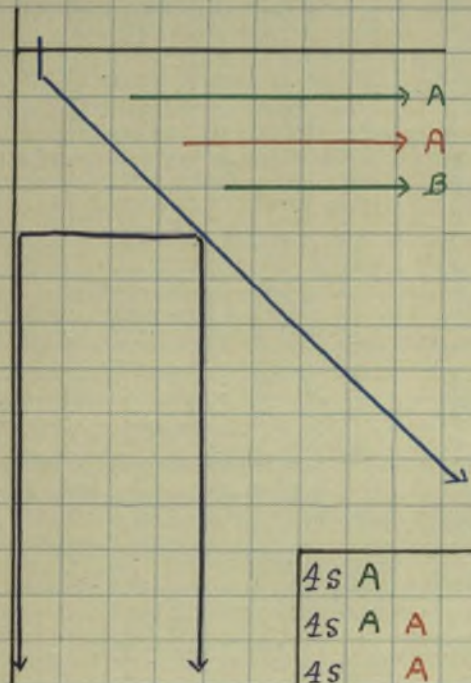
| |
|-------|
| 2sw A |
|-------|

2. 3 Bell. S.W. SHUNT.



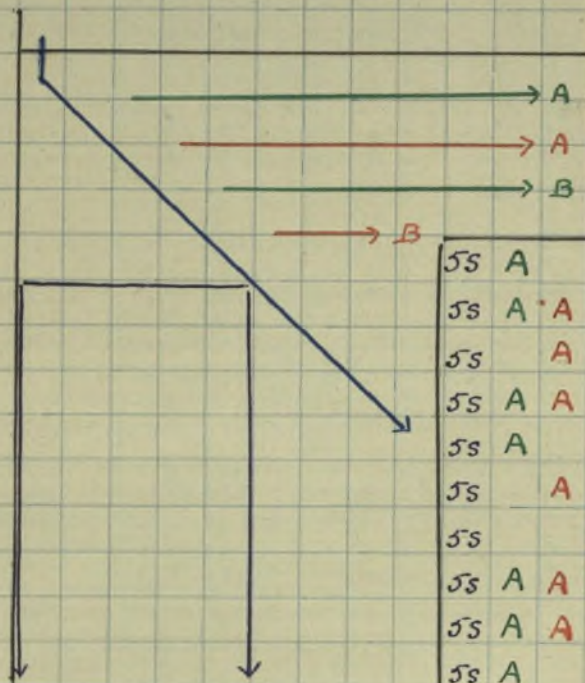
| |
|---------|
| 3sw A |
| 3sw A A |
| 3sw. A |

4. 3 Bell. S.W. Shunt.



| |
|----------|
| 4s A |
| 4s A A |
| 4s A |
| 4s A A B |
| 4s A B |
| 4s A B |
| 4s B |

5. 4 Bell. S.W. Shunt.



| |
|------------|
| 5s A |
| 5s A A |
| 5s A |
| 5s A A B |
| 5s A B |
| 5s A B |
| 5s B |
| 5s A A B B |
| 5s A A B |
| 5s A B B |
| 5s A B |
| 5s A B B |
| 5s A B |
| 5s B B |
| 5s B |

The formula given on page 315 will produce the total combinations of Court Shunts possible with all numbers of Slow Work Shunts to infinity.

Methods produced by mixed Court and Slow Work Shunts extend in regular progression as follows.

A. The number of Slow Work Bells and the number of Court Shunts remain constant on all numbers;

B. The number of Slow Work Bells and the number of Court Shunts expand in regular progression and in equal arithmetical ratio;

C. The number of Slow Work Bells expands in regular progression, but the Court Shunts remain constant in number and position;

D. The number of Slow Work Bells expands in regular progression; the Court Shunts remain constant in number but are allied in position in regular progression.

| | | | | | | |
|----------|----------|----------|----------|---|---|---|
| 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | <u>3</u> | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 |
| <u>4</u> | <u>2</u> | <u>3</u> | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 8 | 5 | 7 |
| 2 | 4 | 3 | 6 | 8 | 7 | 5 |
| 2 | 4 | 3 | 6 | 7 | 8 | 5 |
| 4 | 2 | 6 | 3 | 7 | 5 | 8 |
| 4 | 2 | 6 | 3 | 5 | 7 | 8 |
| <u>4</u> | <u>2</u> | <u>6</u> | <u>3</u> | 5 | 8 | 7 |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 |

| | | | | | | | | |
|----------|----------|----------|----------|---|---|---|---|---|
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | <u>3</u> | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| <u>4</u> | <u>2</u> | <u>3</u> | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 8 | 5 | 0 | 7 | 9 |
| 2 | 4 | 3 | 6 | 8 | 0 | 5 | 9 | 7 |
| 2 | 4 | 3 | 6 | 8 | 0 | 9 | 5 | 7 |
| 2 | 4 | 3 | 6 | 0 | 8 | 9 | 7 | 5 |
| 2 | 4 | 3 | 6 | 0 | 9 | 8 | 7 | 5 |
| 2 | 4 | 3 | 6 | 9 | 0 | 7 | 8 | 5 |
| 4 | 2 | 6 | 3 | 9 | 7 | 0 | 5 | 8 |
| 4 | 2 | 6 | 3 | 7 | 9 | 5 | 0 | 8 |
| 4 | 2 | 6 | 3 | 7 | 5 | 9 | 0 | 8 |
| 4 | 2 | 6 | 3 | 5 | 7 | 9 | 8 | 0 |
| 4 | 2 | 6 | 3 | 5 | 7 | 8 | 9 | 0 |
| <u>4</u> | <u>2</u> | <u>6</u> | <u>3</u> | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 8 | 3 | 0 | 5 | 9 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 7 |
| 6 | 4 | 8 | 2 | 0 | 3 | 9 | 5 | 7 |

| | | | | | | | | | | |
|----------|----------|----------|----------|---|---|---|---|---|---|---|
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | <u>3</u> | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| <u>4</u> | <u>2</u> | <u>3</u> | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 8 | 5 | 0 | 7 | T | 9 | E |
| 2 | 4 | 3 | 6 | 8 | 0 | 5 | T | 7 | E | 9 |
| 2 | 4 | 3 | 6 | 8 | 0 | T | 5 | E | 7 | 9 |
| 2 | 4 | 3 | 6 | 0 | 8 | T | E | 5 | 9 | 7 |
| 2 | 4 | 3 | 6 | 0 | T | 8 | E | 9 | 5 | 7 |
| 2 | 4 | 3 | 6 | T | 0 | E | 8 | 9 | 7 | 5 |
| 2 | 4 | 3 | 6 | T | E | 0 | 9 | 8 | 7 | 5 |
| 2 | 4 | 3 | 6 | E | T | 9 | 0 | 7 | 8 | 5 |
| 4 | 2 | 6 | 3 | E | 9 | T | 7 | 0 | 5 | 8 |
| 4 | 2 | 6 | 3 | 9 | E | 7 | T | 5 | 0 | 8 |
| 4 | 2 | 6 | 3 | 9 | 7 | E | 5 | T | 0 | 8 |
| 4 | 2 | 6 | 3 | 7 | 9 | 5 | E | T | 8 | 0 |
| 4 | 2 | 6 | 3 | 7 | 5 | 9 | E | 8 | T | 0 |
| 4 | 2 | 6 | 3 | 5 | 7 | 9 | 8 | E | 0 | T |
| 4 | 2 | 6 | 3 | 5 | 7 | 8 | 9 | 0 | E | T |
| <u>4</u> | <u>2</u> | <u>6</u> | <u>3</u> | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 3 | 8 | 3 | 0 | 5 | T | 7 | E |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 |

Example of Extension A.

A4SAA A4SAA A4SAA A4SAA
 7 9 11 13
 Adint.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 7 |
| 2 | 4 | 3 | 6 | 8 | 1 | 7 | 5 |
| 2 | 4 | 3 | 6 | 8 | 7 | 1 | 5 |
| 2 | 4 | 3 | 6 | 7 | 8 | 5 | 1 |
| 4 | 2 | 6 | 3 | 7 | 5 | 8 | 1 |
| 4 | 2 | 6 | 3 | 5 | 7 | 1 | 8 |
| 4 | 2 | 6 | 3 | 5 | 1 | 7 | 8 |
| 4 | 2 | 6 | 3 | 1 | 5 | 8 | 7 |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 7 | 5 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 1 | 6 | 4 | 8 | 2 | 7 | 3 | 5 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 0 | 7 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 0 | 1 | 9 | 7 |
| 2 | 4 | 3 | 6 | 5 | 8 | 0 | 9 | 1 | 7 |
| 2 | 4 | 3 | 6 | 5 | 8 | 9 | 0 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 9 | 7 | 0 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 9 | 1 | 0 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 9 | 0 |
| 4 | 2 | 6 | 3 | 8 | 5 | 1 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 8 | 1 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 1 | 8 | 0 | 5 | 9 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 1 | 6 | 4 | 8 | 2 | 0 | 3 | 9 | 5 | 7 |

Example of
EXTENSION B.

A 4s. AA. AB 6s. AA. BB. 7 9

ABC 8s. AA. BB. CC. 11 Ad. int.

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | T | 9 | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | T | 1 | E | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | T | E | 1 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | E | T | 9 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | E | 9 | T | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | E | 1 | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 | E | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 1 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 0 | 7 | T | 9 | E | |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | T | 7 | E | 9 | |
| 2 | 4 | 3 | 6 | 8 | 5 | 0 | 7 | T | 9 | E | |
| 4 | 2 | 6 | 3 | 8 | 0 | 5 | T | 7 | E | 9 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | |
| 1 | 6 | 4 | 8 | 2 | 0 | 3 | T | 7 | E | 9 | |
| 1 | 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 |

A1
A2
B1
B2
C1
C2
CC2
BB2
AA2
CC1
BB1
AA1

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 7 |
| 2 | 4 | 3 | 6 | 8 | 1 | 7 | 5 |
| 2 | 4 | 3 | 6 | 8 | 7 | 1 | 5 |
| 2 | 4 | 3 | 6 | 8 | 7 | 5 | 1 |
| 4 | 2 | 6 | 3 | 7 | 5 | 8 | |
| 4 | 2 | 6 | 3 | 5 | 7 | 1 | 8 |
| 4 | 2 | 6 | 3 | 5 | 1 | 7 | 8 |
| 4 | 2 | 6 | 3 | 5 | 8 | 7 | |
| 2 | 4 | 6 | 1 | 3 | 8 | 5 | 7 |
| 4 | 2 | 1 | 6 | 8 | 3 | 7 | 5 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | |
| 1 | 6 | 4 | 8 | 2 | 7 | 3 | 5 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 8 | 1 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | 9 | 5 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 9 | 1 | 7 | 5 |
| 4 | 6 | 2 | 8 | 3 | 0 | 9 | 7 | 1 | 5 |
| 4 | 6 | 2 | 8 | 3 | 0 | 7 | 9 | 5 | 1 |
| 6 | 4 | 8 | 2 | 0 | 3 | 7 | 5 | 9 | 1 |
| 6 | 4 | 8 | 2 | 0 | 3 | 5 | 7 | 1 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | 5 | 1 | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | 1 | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | 1 | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | 1 | 2 | 9 | 3 | 7 | 5 |
| 6 | 8 | 0 | 1 | 4 | 9 | 2 | 7 | 3 | 5 |
| 8 | 6 | 1 | 0 | 9 | 4 | 7 | 2 | 5 | 3 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 5 | |
| 8 | 0 | 6 | 9 | 4 | 9 | 2 | 5 | 3 | |
| 1 | 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 |

Example of Extension C.

- A4s AA
7
- A6s AA
9
- A8s AA
11
- A10s AA
13

Ad. mt.

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 3 | 8 | 1 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 1 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 1 | 9 | 5 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 9 | 1 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 9 | 7 | 1 | 5 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 7 | 9 | 5 | 1 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 7 | 5 | 9 | 1 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 7 | 1 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 1 | 7 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 9 | 7 | |
| 8 | 0 | 6 | T | 4 | E | 2 | 1 | 3 | 9 | 5 | 7 |
| 0 | 8 | T | 6 | E | 4 | 1 | 2 | 9 | 3 | 7 | 5 |
| 0 | T | 8 | E | 6 | 1 | 4 | 9 | 2 | 7 | 3 | 5 |
| T | 0 | E | 8 | 1 | 6 | 9 | 4 | 7 | 2 | 5 | 3 |
| 0 | T | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| T | 0 | E | 8 | 7 | 6 | 5 | 4 | 3 | 2 | | |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 1 | T | E | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 |
| 1 | E | T | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 7 |
| 2 | 4 | 3 | 6 | 8 | 1 | 7 | 5 |
| 2 | 4 | 3 | 6 | 8 | 7 | 1 | 5 |
| 2 | 4 | 3 | 6 | 7 | 8 | 5 | 1 |
| 4 | 2 | 6 | 3 | 7 | 5 | 8 | 1 |
| 4 | 2 | 6 | 3 | 5 | 7 | 1 | 8 |
| 4 | 2 | 6 | 3 | 5 | 7 | 8 | 1 |
| 4 | 2 | 6 | 3 | 1 | 5 | 8 | 7 |
| 2 | 4 | 6 | 1 | 3 | 8 | 5 | 7 |
| 4 | 2 | 1 | 6 | 8 | 3 | 7 | 5 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 1 | 4 | 6 | 2 | 8 | 3 | 7 | 5 |
| 1 | 6 | 4 | 8 | 2 | 7 | 3 | 5 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 3 | 5 | 0 | 7 | 9 |
| 6 | 4 | 8 | 2 | 3 | 1 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 1 | 9 | 5 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 9 | 1 | 7 | 5 |
| 4 | 6 | 2 | 8 | 3 | 0 | 9 | 7 | 1 | 5 |
| 4 | 6 | 2 | 8 | 3 | 0 | 7 | 9 | 5 | 1 |
| 6 | 4 | 8 | 2 | 0 | 3 | 7 | 5 | 9 | 1 |
| 6 | 4 | 8 | 2 | 0 | 3 | 5 | 7 | 1 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | 5 | 7 | 1 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | 1 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 0 | 1 | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 9 | 3 | 7 | 5 | 1 |
| 6 | 8 | 4 | 1 | 2 | 0 | 3 | 9 | 5 | 7 |
| 8 | 6 | 1 | 4 | 0 | 2 | 9 | 3 | 7 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| X | 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 1 | 3 | 5 | E | 7 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | 3 | 1 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 1 | 9 | 5 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 9 | 1 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 9 | 7 | 1 | 5 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 7 | 9 | 5 | 1 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 7 | 5 | 9 | 1 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 7 | 1 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 1 | 7 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | E | 3 | 5 | 9 | 7 | 1 |
| 6 | 8 | 4 | 0 | 2 | T | E | 3 | 9 | 5 | 7 | 1 |
| 8 | 6 | 0 | 4 | T | 2 | E | 9 | 3 | 7 | 5 | 1 |
| 8 | 0 | 6 | T | 4 | 1 | 2 | E | 3 | 9 | 5 | 7 |
| 0 | 8 | T | 6 | 1 | 4 | E | 2 | 9 | 3 | 7 | 5 |
| 0 | T | 8 | 6 | E | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| T | 0 | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| T | E | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| 1 | E | T | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |

Example of Extension D

| | | | | |
|-------|-------|-------|--------|--------|
| A4SAA | B6SBB | C8SCC | D10SDD | Adint. |
| 7 | 9 | 11 | 13 | |

Mixed Extreme Shunts, Count Shunts,
and Slow Work Shunts.

To every Course produced by Count Shunts,
Extreme Shunts can be added as follows -

1. A With the Hunts at the Lead;
2. B With the Hunts behind;
3. A/B With the Hunts at the Lead; and
with the Hunts behind.

To every Course produced by Single Count
Shunts, by Slow Work Shunts, or by mixed
Count and Slow Work Shunts, A can be
added, but not B .

To every Course produced by Reverse Count
Shunts, Reverse Slow Work Shunts, or
by mixed Count and Reverse Slow Work
Shunts, B can be added but not A .

With the addition of these, the formulae
given for Count and Slow Work Shunts,
will produce every possible Constitutional
Shunt and combination of Constitutional
Shunts, on the Plain Principle, on all numbers
to infinity. Some of these combinations will
produce one Lead only, others a block
less than a full Course but in all cases
the Hunts Cyclical path is complete.*
In any combination of Shunts, the number
of Extreme Bells in each Shunt must

* See p. 187.

be the same.

Combinations of Extreme Shunts, Count Shunts, and Slow Hook Shunts, extend exactly similarly to the Extensions already described. Examples;—

(a) DOUBLE OXFORD BOB

(a)

| | | | | |
|--|---|--|---|---|
| $\frac{A \langle B \rangle AA \langle A \rangle}{5}$ | $\frac{A \langle B \rangle AA \langle A \rangle}{7}$ | $\frac{A \langle B \rangle AA \langle A \rangle}{9}$ | $\frac{A \langle B \rangle AA \langle A \rangle}{11}$ | → |
| $\frac{A \langle B \rangle AA \langle A \rangle}{5}$ | $\frac{B \langle B \rangle BB \langle A \rangle}{7}$ | $\frac{C \langle B \rangle CC \langle A \rangle}{9}$ | $\frac{D \langle B \rangle DD \langle A \rangle}{11}$ | → |
| $\frac{A \langle B \rangle AA \langle A \rangle}{5}$ | $\frac{A \langle B \rangle \langle B \rangle AA \langle BB \rangle \langle A \rangle}{7}$ | $\frac{A \langle B \rangle C \langle B \rangle AA \langle BB \rangle \langle CC \rangle \langle A \rangle}{9}$ | | → |
| $\frac{A \langle B \rangle AA \langle A \rangle}{5}$ | $\frac{B \langle B \rangle BB \langle A \rangle}{9}$ | $\frac{C \langle B \rangle CC \langle A \rangle}{13}$ | $\frac{D \langle B \rangle DD \langle A \rangle}{15}$ | → |

| | | | | |
|---|--|--|---|---|
| $\frac{A \langle 4s \rangle AA \langle A \rangle}{7}$ | $\frac{A \langle 4s \rangle AA \langle A \rangle}{9}$ | $\frac{A \langle 4s \rangle AA \langle A \rangle}{11}$ | $\frac{A \langle 4s \rangle AA \langle A \rangle}{13}$ | → |
| $\frac{A \langle 4s \rangle AA \langle A \rangle}{7}$ | $\frac{A \langle B \rangle \langle 6s \rangle AA \langle BB \rangle \langle A \rangle}{9}$ | $\frac{A \langle B \rangle C \langle 8s \rangle AA \langle BB \rangle \langle CC \rangle \langle A \rangle}{11}$ | | → |
| $\frac{A \langle 4s \rangle AA \langle A \rangle}{7}$ | $\frac{A \langle 6s \rangle AA \langle A \rangle}{9}$ | $\frac{A \langle 8s \rangle AA \langle A \rangle}{11}$ | $\frac{A \langle 10s \rangle AA \langle A \rangle}{13}$ | → |
| $\frac{A \langle 4s \rangle AA \langle A \rangle}{7}$ | $\frac{B \langle 6s \rangle BB \langle A \rangle}{9}$ | $\frac{C \langle 8s \rangle CC \langle A \rangle}{11}$ | $\frac{D \langle 10s \rangle DD \langle A \rangle}{13}$ | → |

As the Extreme, Count, and Slow Work
Constitutional Shunts apply to the Treble
Bob Principle exactly in the same way that
they do to the Plain Principle, the explanations
just given will so far apply to the
Extension of Treble Bob Methods. The
Constitutional Shunts peculiar to the
Treble Bob Principle are all variations
of these Constitutional Shunts, and extend
similarly. I will presently give some
examples.

The Extension of Additional Shunts.

Every Additional Shunt consists of either,
(a) a Hunting Course on five or more
bells;
(b) a Dodging Movement on five or more
bells;
(c) a Combination of Hunting Courses,
or of Hunting Courses and Dodging
Movements.

Every Hunting Course can expand in regular
progression as the difference in the
number of bells involved.
Every Dodging Movement can expand in

regular progression.

The expansion of the Principle, and of the Constitutional Shunt, gives more bells to make Additional Shunts and more room to make them in.

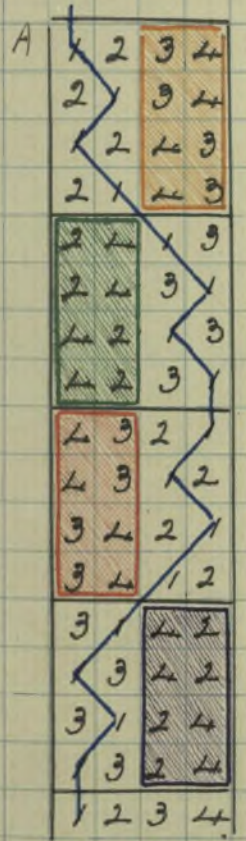
Therefore, prima facie, it is probable that an Additional Shunt can expand as follows. -

1. It may increase in size by adding to the number of bells taking part in it;
2. It may remain constant in size, number, and position;
3. It may remain constant in size and number, but be altered in position in a regular progression;
4. It may remain constant in size, but increase in number in regular progression.

But since the expansion of the Principle and of the Constitutional Shunt is necessarily in a different ratio to the expansion of any Additional Shunt, the capacity of the latter for expansion is very much restricted.

There is one general law for the extension of Additional Shunts, which adapts itself

is the different conditions produced by the Principle and the Constitutional Shunt.



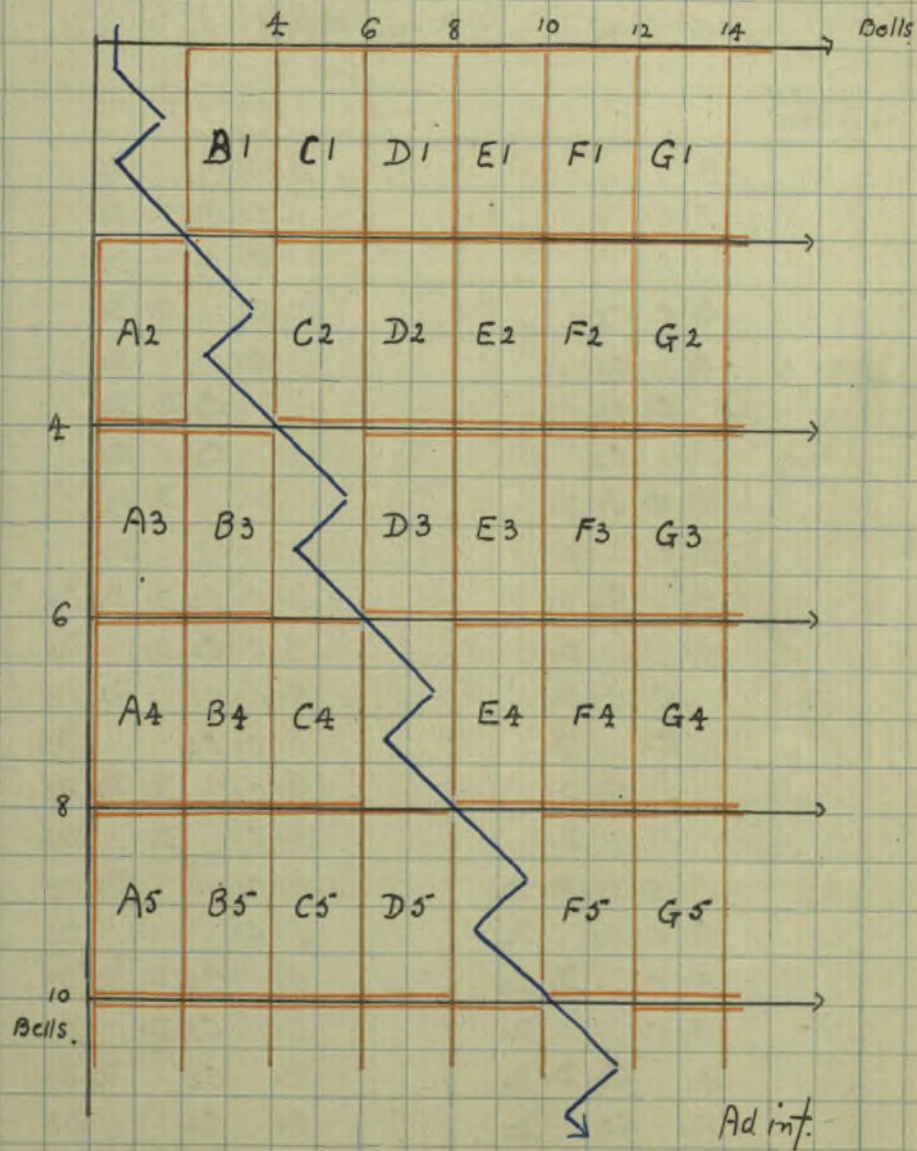
A is a Lead produced by the Treble Bob Principle in each Division of which a 2-Bell Hunting Course Additional Shunt is made, the object and effect of which is to get rid of the repetition of Rows caused by the Principle.

The Principle extends in a regular progression. In what way can the Additional Shunt extend?

The Extension of the Principle increases the size of the Division horizontally, but leaves it constant vertically. Therefore the Additional Shunt cannot expand in size.

The Extension of the Principle not only increases the size of the Divisions horizontally, but also increases the number of Divisions, and therefore increases in regular progression the number of positions in which 2-Bell. Add: Shunt can be made.

TWO-BELL HUNTING COURSE ADD: SHUNTS (KENT ADD: SHUNTS)
 applied to a Method on the TREBLE BOB PRINCIPLE.



COMBINATIONS of KENT ADD: SHUNTS applied to
the TREBLE BOB PRINCIPLE

HUNT ASCENDING ABOVE HUNT.

Limit of
No of Bells.

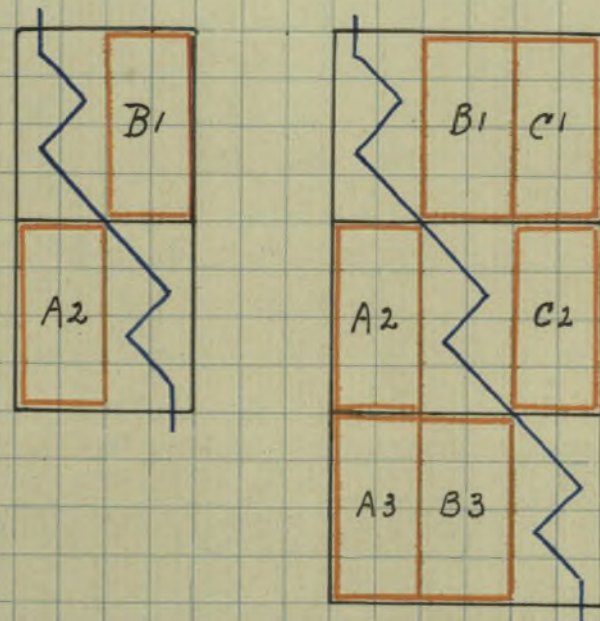
| | | |
|----|----------------|-------------------|
| 4 | B1 | B1 C1 D2 |
| | B1 C1 | C1 C2 D1 D2 |
| | C2 | C1 C2 D2 |
| | B1 C1 C2 | C1 D1 D2 |
| | B1 C2 | C1 D2 |
| | C1 C2 | C2 D1 D2 |
| 6. | C2 | C2 D2 |
| | B1 C1 C2 D1 | D1 D2 |
| | B1 C1 D1 | D2 |
| | B1 C2 D1 | B1 C1 C2 D1 D2 D3 |
| | B1 D1 | B1 C1 C2 D1 D3 |
| | C1 C2 D1 | B1 C1 C2 D2 D3 |
| | C1 D1 | B1 C1 C2 D3 |
| | C2 D1 | B1 C1 D1 D2 D3 |
| | D1 | B1 C1 D1 D3 |
| | B1 C1 C2 D1 D2 | B1 C1 D2 D3 |
| | B1 C1 C2 D2 | B1 C1 D3 |
| | B1 C1 D1 D2 | B1 C2 D1 D2 D3 |
| | B1 C1 D2 | B1 C2 D1 D3 |
| | B1 C2 D1 D2 | B1 C2 D2 D3 |
| | B1 C2 D2 | B1 C2 D3 |
| | B1 D1 D2 | Ad Int. |

HUNT ASCENDING BELOW HUNT.

| | | |
|----|----------------|-------------------|
| 4 | A2 | A2 B4 |
| | A2 A3 | A3 B3 A4 B4 |
| | A3 | A3 B3 B4 |
| | A2 A3 B3 | A3 A4 B4 |
| | A2 B3 | A3 B4 |
| | A3 B3 | B3 A4 B4 |
| 6. | B3 | B3 B4 |
| | A2 A3 B3 A4 | A4 B4 |
| | A2 A3 A4 | B4 |
| | A2 B3 A4 | A2 A3 B3 A4 B4 C4 |
| | A2 A4 | A2 A3 B3 A4 B4 C4 |
| | A3 B3 A4 | A2 A3 B3 B4 C4 |
| | A3 A4 | A2 A3 B3 C4 |
| | B3 A4 | A2 A3 A4 B4 C4 |
| | A4 | A2 A3 A4 C4 |
| | A2 A3 B3 A4 B4 | A2 A3 B4 C4 |
| | A2 A3 B3 B4 | A2 A3 C4 |
| | A2 A3 A4 B4 | A2 B3 A4 B4 C4 |
| | A2 A3 B4 | A2 B3 A4 C4 |
| | A2 B3 A4 B4 | A2 B3 B4 C4 |
| | A2 B3 B4 | A2 B3 C4 |
| | A2 A4 B4 | / Ad Int. |

Each term in the table for the Hunt is above the Hunt can be used with every one of the terms in the table for the Hunt below the Hunt, giving on the higher numbers an immense number of combinations.

To obtain the combinations with the Hunt descending reverse the diagram and use the same tables.



Neither $\frac{B1}{6}$ nor $\frac{C1}{6}$ nor $\frac{C2}{6}$ nor $\frac{B1C1}{6}$ nor $\frac{C1C2}{6}$ nor $\frac{B1C1C2}{6}$ is exactly the same as $\frac{B1}{4}$; but each is equally an equivalent. We get therefore the following extensions; -

$$\frac{B_1}{4} \quad \frac{B_1}{6} \quad \frac{B_1}{8} \quad \frac{B_1}{10} \quad \frac{B_1}{12} \quad \frac{B_1}{14} \quad \frac{B_1}{16} \quad \frac{B_1}{18} \quad \frac{B_1}{20} \longrightarrow \text{Ad Int.}$$

$$\frac{B_1}{4} \quad \frac{C_1}{6} \quad \frac{D_1}{8} \quad \frac{E_1}{10} \quad \frac{F_1}{12} \quad \frac{G_1}{14} \quad \frac{H_1}{16} \quad \frac{J_1}{18} \quad \frac{K_1}{20} \longrightarrow$$

$$\frac{B_1}{4} \quad \frac{C_2}{6} \quad \frac{D_3}{8} \quad \frac{E_4}{10} \quad \frac{F_5}{12} \quad \frac{G_6}{14} \quad \frac{H_7}{16} \quad \frac{J_8}{18} \quad \frac{K_9}{20} \longrightarrow$$

$$\frac{B_1}{4} \quad \frac{C_2}{8} \quad \frac{D_3}{12} \quad \frac{E_4}{16} \quad \frac{F_5}{20} \quad \frac{G_6}{24} \quad \frac{H_7}{28} \quad \frac{J_8}{32} \quad \frac{K_9}{36} \longrightarrow$$

$$\frac{B_1}{4} \quad \frac{B_1 C_1}{6} \quad \frac{B_1 C_1 D_1}{8} \quad \frac{B_1 C_1 D_1 E_1}{10} \longrightarrow$$

$$\frac{B_1}{4} \quad \frac{C_1 C_2}{6} \quad \frac{D_1 D_2 D_3}{8} \quad \frac{E_1 E_2 E_3 E_4}{10} \longrightarrow$$

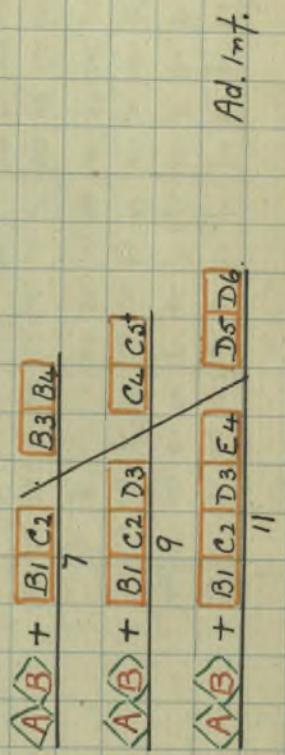
$$\frac{B_1}{4} \quad \frac{B_1 C_1 C_2}{6} \quad \frac{B_1 C_1 D_1 C_2 D_2 D_3}{8} \longrightarrow \text{Ad Int.}$$

The following are two examples of Extensions from Table on page 341. The Constititional Shunts are the two Esclimens A and B .

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 4 | 6 | 5 | 8 | 7 |
| 1 | 2 | 4 | 3 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 3 | 8 | 7 | 5 |
| 2 | 4 | 6 | 8 | 3 | 5 | 7 | |
| 4 | 2 | 6 | 8 | 3 | 7 | 5 | |
| 4 | 6 | 2 | 8 | 1 | 7 | 3 | 5 |
| 6 | 4 | 2 | 8 | 7 | 1 | 5 | 3 |
| 4 | 6 | 8 | 2 | 1 | 7 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 1 | 5 | 3 |
| 6 | 8 | 4 | 7 | 2 | 5 | 1 | 3 |
| 8 | 6 | 4 | 7 | 5 | 2 | 3 | 1 |
| 6 | 8 | 7 | 4 | 2 | 5 | 1 | 3 |
| 8 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 3 | 4 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 3 | 8 | 0 | 5 | 9 | 7 |
| 2 | 4 | 6 | 8 | 3 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 1 | 3 | 9 | 7 | 5 |
| 4 | 6 | 2 | 8 | 1 | 0 | 9 | 3 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 1 | 9 | 3 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 4 | 2 | 9 | 7 | 1 | 5 | 3 |
| 6 | 8 | 4 | 0 | 9 | 2 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 1 | 3 |
| 0 | 8 | 9 | 6 | 4 | 7 | 5 | 2 | 3 | 1 |
| 8 | 0 | 6 | 9 | 7 | 4 | 2 | 5 | 1 | 3 |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 3 | 4 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 1 | 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 3 | 8 | 0 | 5 | T | 7 | E | 9 |
| 2 | 4 | 6 | 8 | 3 | 5 | 0 | 7 | T | 9 | E | |
| 4 | 2 | 6 | 8 | 3 | 0 | 5 | T | 7 | E | 9 | |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | 3 | T | E | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 0 | T | 3 | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 1 | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 1 | 3 | 9 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | T | E | 1 | 9 | 3 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 1 | 9 | 3 | 7 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 1 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 2 | 9 | 7 | 1 | 5 | 3 |
| 8 | 0 | 6 | T | 4 | E | 9 | 2 | 1 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 1 | 3 |
| T | 0 | E | 8 | 9 | 6 | 4 | 7 | 5 | 2 | 3 | 1 |
| 0 | T | 8 | E | 6 | 9 | 7 | 4 | 2 | 5 | 1 | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |

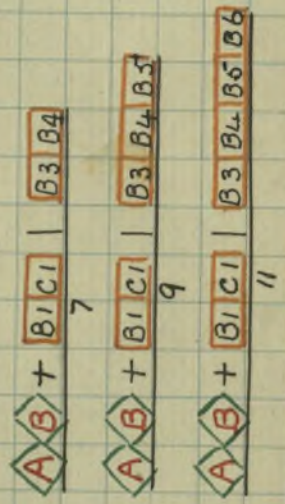


| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 3 | 4 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 7 | 5 | |
| 2 | 4 | 6 | 8 | 3 | 5 | 7 | |
| 4 | 2 | 6 | 8 | 3 | 7 | 5 | |
| 4 | 6 | 2 | 8 | 7 | 3 | 5 | |
| 6 | 4 | 2 | 8 | 7 | 5 | 3 | |
| 4 | 6 | 8 | 2 | 7 | 3 | 5 | |
| 6 | 4 | 8 | 2 | 7 | 5 | 3 | |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | |
| 8 | 6 | 4 | 7 | 5 | 2 | 3 | |
| 6 | 8 | 7 | 4 | 2 | 5 | 3 | |
| 8 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | 1 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 3 | 4 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 0 | 5 | 9 | 7 | |
| 2 | 4 | 6 | 8 | 3 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 4 | 6 | 2 | 8 | 0 | 3 | 9 | 5 | 7 | |
| 6 | 4 | 2 | 8 | 0 | 9 | 3 | 7 | 5 | |
| 4 | 6 | 8 | 2 | 0 | 3 | 9 | 5 | 7 | |
| 6 | 4 | 8 | 2 | 0 | 9 | 3 | 7 | 5 | |
| 6 | 8 | 4 | 0 | 2 | 9 | 7 | 3 | 5 | |
| 8 | 6 | 4 | 0 | 9 | 2 | 7 | 5 | 3 | |
| 6 | 8 | 0 | 4 | 2 | 9 | 7 | 3 | 5 | |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 5 | 3 | |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | |
| 0 | 8 | 6 | 9 | 7 | 4 | 5 | 2 | 3 | |
| 8 | 0 | 9 | 6 | 4 | 7 | 2 | 5 | 3 | |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 3 | 4 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | |
| 4 | 2 | 6 | 3 | 8 | 0 | 5 | T | 7 | E | 9 | |
| 2 | 4 | 6 | 8 | 3 | 5 | 0 | 7 | T | 9 | E | |
| 4 | 2 | 6 | 8 | 3 | 0 | 5 | T | 7 | E | 9 | |
| 4 | 6 | 2 | 8 | 0 | 3 | T | 5 | E | 7 | 9 | |
| 6 | 4 | 2 | 8 | 0 | T | 3 | E | 5 | 9 | 7 | |
| 4 | 6 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 | |
| 6 | 4 | 8 | 2 | 0 | T | 3 | E | 5 | 9 | 7 | |
| 6 | 8 | 4 | 0 | 2 | T | E | 3 | 9 | 5 | 7 | |
| 8 | 6 | 4 | 0 | T | 2 | E | 9 | 3 | 7 | 5 | |
| 6 | 8 | 0 | 4 | 2 | T | E | 3 | 9 | 5 | 7 | |
| 8 | 6 | 0 | 4 | T | 2 | E | 9 | 3 | 7 | 5 | |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 7 | 3 | 5 | |
| 0 | 8 | 6 | T | E | 4 | 9 | 2 | 7 | 5 | 3 | |
| 8 | 0 | T | 6 | 4 | E | 2 | 9 | 7 | 3 | 5 | |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 5 | 3 | |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| T | 0 | 8 | E | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 0 | T | E | 8 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 | 1 |

Ad Int.



In many cases the extension of the Constructional Shunt's expand the available room for making the Additional Shunt horizontally as well as vertically; and when such expansion is sufficiently great, the Additional Shunt can be extended by adding to the bells taking part in it.

On page 347 is an example of such expansion. It will be noticed that it requires the addition of four bells in the Constructional Shunt's to give sufficient room to add five bells to the Additional Shunt.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 5 | 7 | 6 | 8 |
| 2 | 3 | 4 | 7 | 5 | 8 | 6 | |
| 2 | 1 | 4 | 3 | 7 | 8 | 5 | 6 |
| 2 | 4 | 1 | 3 | 8 | 7 | 6 | 5 |
| 4 | 2 | 3 | 1 | 8 | 6 | 7 | 5 |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |
| 2 | 3 | 4 | 6 | 5 | 1 | 8 | 7 |
| 3 | 2 | 6 | 4 | 5 | 1 | 7 | 8 |
| 3 | 6 | 2 | 4 | 5 | 1 | 8 | 7 |
| 6 | 3 | 4 | 2 | 5 | 8 | 1 | 7 |
| 6 | 4 | 3 | 2 | 8 | 5 | 7 | 1 |
| 4 | 6 | 2 | 3 | 5 | 8 | 1 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 1 |

A1
A2
B1

B2

B

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 7 | 9 | 8 | E | 0 | T |
| 2 | 3 | 4 | 5 | 6 | 9 | 7 | E | 8 | T | 0 | |
| 2 | 1 | 4 | 3 | 6 | 5 | 9 | E | 7 | T | 8 | 0 |
| 2 | 4 | 1 | 3 | 5 | 6 | E | 9 | T | 7 | 0 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | E | T | 9 | 0 | 7 | 8 |
| 2 | 4 | 1 | 3 | 5 | 6 | T | E | 0 | 9 | 8 | 7 |
| 4 | 2 | 3 | 1 | 6 | 5 | T | 0 | E | 8 | 9 | 7 |
| 2 | 4 | 3 | 6 | 1 | 5 | 0 | T | 8 | E | 7 | 9 |
| 4 | 2 | 6 | 3 | 5 | 1 | 0 | 8 | T | 7 | E | 9 |
| 2 | 4 | 3 | 6 | 1 | 5 | 8 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 8 | 7 | 1 | 0 | 9 | T | E |
| 3 | 2 | 5 | 4 | 8 | 6 | 1 | 7 | 9 | 0 | E | T |
| 3 | 5 | 2 | 8 | 4 | 6 | 7 | 1 | 0 | 9 | T | E |
| 5 | 3 | 8 | 2 | 6 | 4 | 7 | 0 | 1 | 9 | E | T |
| 5 | 8 | 3 | 6 | 2 | 4 | 0 | 7 | 9 | 1 | T | E |
| 8 | 5 | 6 | 3 | 4 | 2 | 7 | 0 | 1 | 9 | E | T |
| 8 | 6 | 5 | 4 | 3 | 2 | 0 | 7 | 9 | 1 | T | E |
| 6 | 8 | 4 | 5 | 2 | 3 | 7 | 0 | 9 | T | 1 | E |

A1
A2
B1

B2

C1

D2

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|
| 6 | 4 | 8 | 2 | 5 | 3 | 0 | 7 | T | 9 | E |
| 4 | 6 | 2 | 8 | 3 | 5 | 7 | 0 | 9 | T | E |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |

B

| | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 | 15 | 16 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 9 | 11 | 0 | 13 | 12 | 15 | 14 | 16 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 11 | 9 | 13 | 0 | 15 | 12 | 16 | 14 | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 11 | 13 | 9 | 15 | 0 | 16 | 12 | 14 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 13 | 11 | 15 | 9 | 16 | 0 | 14 | 12 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 13 | 15 | 11 | 16 | 9 | 14 | 0 | 12 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 15 | 13 | 16 | 11 | 14 | 9 | 12 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 15 | 16 | 13 | 14 | 11 | 12 | 9 | 0 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 16 | 15 | 14 | 13 | 12 | 11 | 0 | 9 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 16 | 14 | 15 | 12 | 13 | 0 | 11 | 9 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 14 | 16 | 12 | 15 | 0 | 13 | 9 | 11 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 14 | 12 | 16 | 0 | 15 | 9 | 13 | 11 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 12 | 14 | 0 | 16 | 9 | 15 | 11 | 13 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 12 | 0 | 14 | 9 | 16 | 11 | 15 | 13 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 0 | 12 | 9 | 14 | 11 | 16 | 13 | 15 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 0 | 9 | 12 | 11 | 14 | 13 | 16 | 15 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 | 11 | 12 | 13 | 14 | 15 | 16 |

A2

B2

C2

A1

B1

C1

D1

The Additional Shunt, illustrated on page 347, can remain constant in size on all numbers of bells. The Extension of the number of Shunts, and their position will then be similar to that of the KENT Shunt illustrated on page 340, adapted to the increased room supplied by the Conditional Shunt. In many such cases the expansion will not be great enough to remove the falseness of the Treble Bob Principle. As for example.

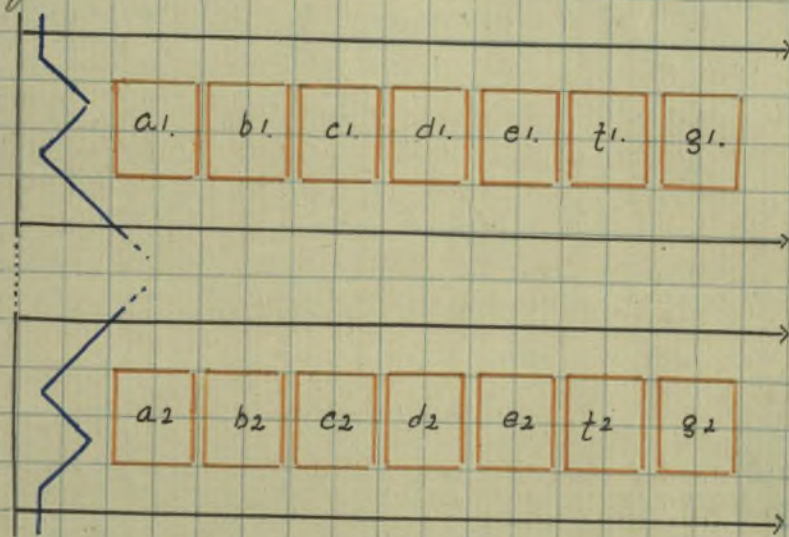
| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 5 | 7 | 6 | 8 | |
| 1 | 2 | 3 | 4 | 7 | 5 | 8 | 6 |
| 2 | 4 | 3 | 7 | 8 | 5 | 6 | |
| 2 | 4 | 1 | 3 | 8 | 7 | 6 | 5 |
| 4 | 2 | 3 | 1 | 8 | 6 | 7 | 5 |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 7 | 9 | 8 | 0 | |
| 1 | 2 | 3 | 4 | 5 | 6 | 9 | 7 | 0 | 8 |
| 2 | 4 | 3 | 6 | 5 | 9 | 0 | 7 | 8 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 0 | 9 | 8 | 7 |
| 4 | 2 | 3 | 1 | 6 | 5 | 0 | 8 | 9 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 8 | 0 | 7 | 9 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 |

The backward hunting of the four kind bells

Cannot be Continued in the Changes marked x.; for that would mean beginning a fresh Additional Shunt, and there is not room enough to complete it.

Additional Shunts Consisting of Hunting Courses, in which the members are separated, extend according to the same law as those in which the members come all together.



The above are the positions in which the Additional Shunts of Oxford Treble Bob can be made. The following shows their Extension.

The Extension of the OXFORD ADDITIONAL SHUNT. applied to Treble Bob.

| | | | | |
|--------------|--------------|---------------|----------------|-----------------|
| | ↑ | ↑ | ↑ | ↑ |
| a | ab | abc | abcd | abcde |
| 5 | 7 | 9 | 11 | 13 |
| ↓ | ↓ | ↓ | ↓ | ↓ |
| a | b | bc | bcd | bcde |
| 7 | 7 | 9 | 11 | 13 |
| ↓ | ↓ | ↓ | ↓ | ↓ |
| a | b | c | cd | cde |
| 9 | 9 | 9 | 11 | 13 |
| ↓ | ↓ | ↓ | ↓ | ↓ |
| a | b | c | d | de |
| 11 | 11 | 11 | 11 | 13 |
| ↓ | ↓ | ↓ | ↓ | ↓ |
| a | b | c | d | e |
| 13 | 13 | 13 | 13 | 13 |
| ↓ | ↓ | ↓ | ↓ | ↓ |

The next example shows how the expansion of the Constitutional Shunt will allow the number of Additional Shunts to be increased. Notice that to allow the Additional Shunts to be doubled, the Extreme Bells must be increased by four.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 3 | 4 | 6 | 5 | 7 | 8 |
| 2 | 1 | 4 | 3 | 5 | 6 | 8 | 7 |
| 2 | 4 | 1 | 3 | 6 | 5 | 7 | 8 |
| 4 | 2 | 3 | 1 | 5 | 6 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 |
| 2 | 4 | 3 | 6 | 5 | 1 | 8 | 7 |
| 4 | 2 | 6 | 3 | 5 | 8 | 1 | 7 |
| 4 | 2 | 3 | 4 | 8 | 5 | 7 | 1 |
| 2 | 4 | 3 | 4 | 5 | 8 | 1 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | 1 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 1 | 2 | 3 | 4 | 6 | 5 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 5 | 6 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 6 | 5 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 5 | 6 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 0 | 9 | E | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 8 | 1 | 9 | 0 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 | E | T |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 | T | E |
| 2 | 4 | 6 | 3 | 5 | 8 | 7 | 0 | 1 | 9 | E | T |
| 4 | 2 | 3 | 6 | 8 | 5 | 0 | 7 | 9 | 1 | T | E |
| 2 | 4 | 6 | 3 | 5 | 8 | 7 | 0 | 9 | T | 1 | E |

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 6 | 8 | 5 | 0 | 7 | T | 9 | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |

| | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 | 15 | 16 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | | | | | | | | |
| 1 | 2 | 3 | 4 | 6 | 5 | 7 | 8 | | | | | | | | |
| 2 | 1 | 4 | 3 | 5 | 6 | 8 | 7 | | | | | | | | |
| 2 | 4 | 1 | 3 | 6 | 5 | 7 | 8 | | | | | | | | |
| 4 | 2 | 3 | 1 | 5 | 6 | 8 | 7 | | | | | | | | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | | | | | | | | |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 11 | | | | |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | 11 | 12 | | | | |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | 12 | 11 | | | | |
| | | 3 | 6 | 1 | 5 | 7 | 8 | 0 | 9 | 11 | 12 | | | | |
| | | 6 | 3 | 5 | 1 | 8 | 7 | 9 | 0 | 12 | 11 | | | | |
| | | 3 | 6 | 5 | 8 | 1 | 7 | 0 | 9 | 11 | 12 | | | | |
| | | | 8 | 5 | 7 | 1 | 7 | 9 | 0 | 12 | 11 | | | | |
| | | | 5 | 8 | 1 | 7 | 7 | 9 | 0 | 11 | 12 | | | | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 | 0 | 9 | 12 | 11 | 14 | 13 | 16 | 15 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 | 11 | 12 | 13 | 14 | 15 | 16 |

A Dodging Movement on x bells consists of y steps of Forward Hunting, followed by y steps of Backward Hunting, or of y steps of Backward Hunting, followed by y steps of Forward Hunting. This will expand by adding to x in regular progression; or to y in regular progression; or to both x and y .

It follows, that an Additional Hunt which consists of a Dodging Movement can, *prima facie*, extend as follows -

1. By adding to the number of bells involved;
2. By increasing the number of steps of Forward and Backward Hunting;
3. By adding to the number of bells, and also increasing the number of steps of Backward and Forward Hunting;
4. The Hunt may remain constant in size, number, and position;
5. The Hunt may remain constant in size and number, but the position be altered in regular progression;
6. The Hunt may remain constant in size, but increase in number in regular progression.

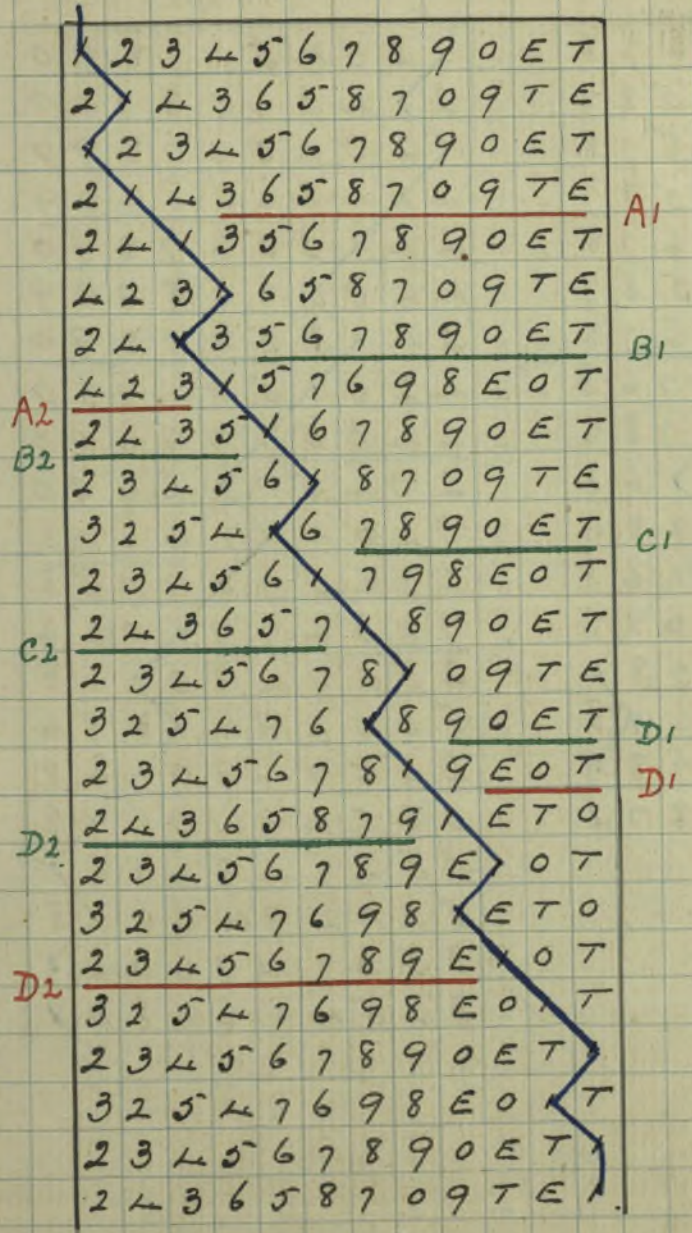
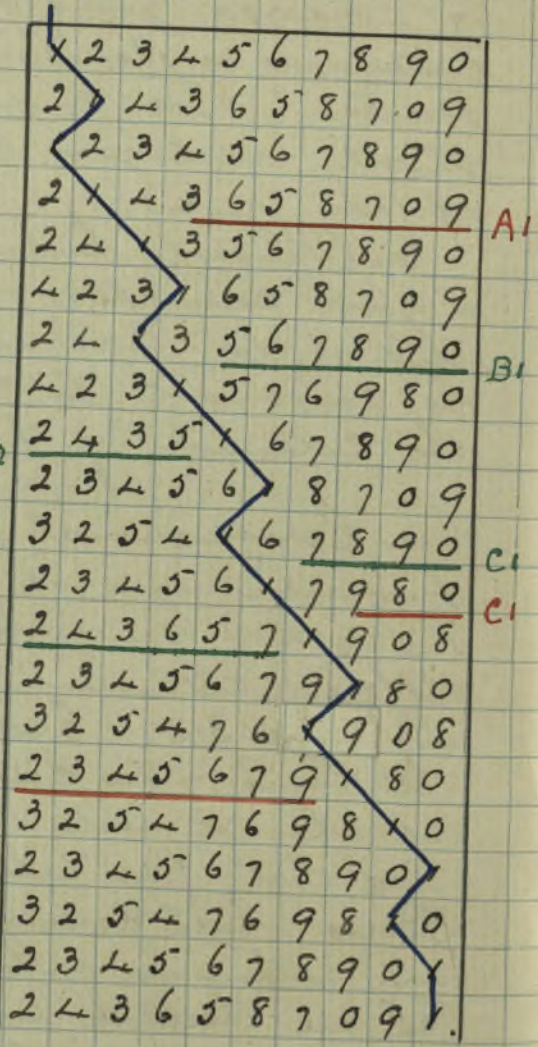
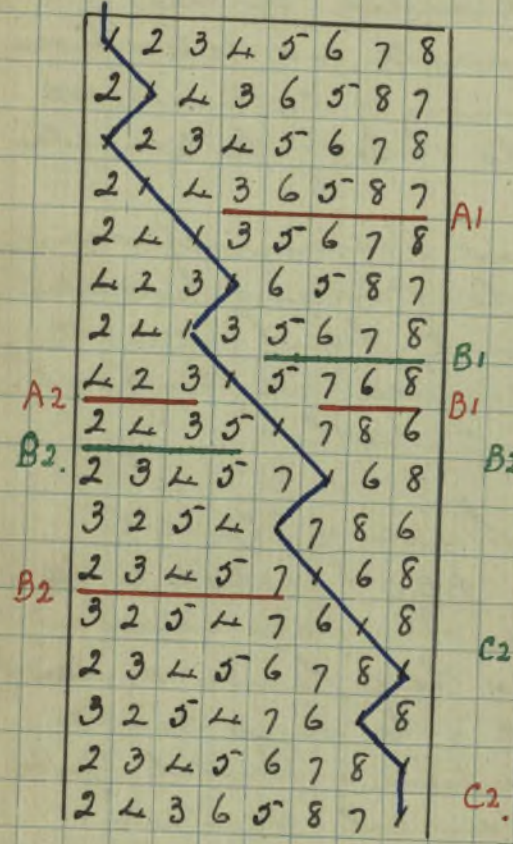
In any particular method this power

of expansion is conditioned by the amount of increased room provided by the Extension of the Principle and the Constructional Shunts. The Conditions of Extension are strictly analogous to those of the examples already given.

As Bristol Surprise Major includes a good example of the Dodging Movement used as an Additional Shunt, it will be convenient to consider at this point the extension of that Method.

The Constructional Shunts of Bristol Surprise Major are ABB applied to the Treble Bob Principle. There are seven different extensions of these Shunts as shown on page 316. Each of the seven can be the basis of an extension of Bristol Major but when we write them out we shall find that four will contain repetition of Rows which cannot be remedied by any extension of the Additional Shunts. They are therefore worthless for practical purposes, but interesting as examples of Extension.

The Constructional Shunts of BRISTOL SURPRISE



ABCDEF
13

ABCD
11

ABCC
9

ABB
7

Extension A.

Ad. int.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 8 |
| 2 | 4 | 3 | 5 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 1 |

A1

B1

B1

A2

B2

B2

C2

C2

A2
B2

B2

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | 0 |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | 0 | 8 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | 0 |
| 3 | 2 | 5 | 4 | 1 | 7 | 9 | 6 | 0 | 8 |
| 2 | 3 | 4 | 5 | 7 | 1 | 9 | 0 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 9 | 1 | 0 | 8 | 6 |
| 2 | 5 | 2 | 7 | 4 | 9 | 0 | 1 | 6 | 8 |
| 5 | 3 | 7 | 2 | 9 | 4 | 1 | 0 | 8 | 6 |
| 3 | 5 | 2 | 7 | 4 | 9 | 0 | 1 | 6 | 8 |
| 5 | 3 | 7 | 2 | 9 | 4 | 0 | 6 | 1 | 8 |
| 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 | 1 |
| 5 | 3 | 7 | 2 | 9 | 4 | 0 | 6 | 1 | 8 |
| 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 | 1 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 0 | 1 |

A1

B1

B1

C1

C1

C1

C1

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | E | 0 | T |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | E | 8 | T | 0 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | E | 0 | T |
| 3 | 2 | 5 | 4 | 1 | 7 | 9 | 6 | E | 8 | T | 0 |
| 2 | 3 | 4 | 5 | 7 | 1 | 9 | E | 6 | T | 8 | 0 |
| 3 | 2 | 5 | 4 | 7 | 9 | 1 | E | T | 6 | 0 | 8 |
| 3 | 5 | 2 | 7 | 4 | 9 | E | 1 | 6 | T | 8 | 0 |
| 5 | 3 | 7 | 2 | 9 | 4 | E | T | 6 | 0 | 8 | 1 |
| 3 | 5 | 2 | 7 | 4 | 9 | E | 1 | T | 0 | 6 | 8 |
| 5 | 3 | 7 | 2 | 9 | 4 | E | T | 1 | 0 | 8 | 6 |
| 5 | 7 | 3 | 9 | 2 | E | 4 | T | 0 | 1 | 6 | 8 |
| 7 | 5 | 9 | 3 | E | 2 | T | 4 | 1 | 0 | 8 | 6 |
| 5 | 7 | 3 | 9 | 2 | E | 4 | T | 0 | 1 | 6 | 8 |
| 7 | 5 | 9 | 3 | E | 2 | T | 4 | 0 | 6 | 1 | 8 |
| 5 | 7 | 3 | 9 | 2 | E | 4 | T | 6 | 0 | 8 | 1 |
| 7 | 5 | 9 | 3 | E | 2 | T | 4 | 0 | 6 | 1 | 8 |
| 5 | 7 | 3 | 9 | 2 | E | 4 | T | 6 | 0 | 8 | 1 |
| 5 | 3 | 7 | 2 | 9 | 4 | E | 6 | T | 8 | 0 | 1 |

A1

B1

B1

C1

C1

C1

C1

D1

D1

A2

B2

B2

C2

C2

D2

D2

A B B A B B C C A B B C C D D A B B C C D D E E

13

11

9

7

Extension B.

Ad. int.

| | | | | | | | | |
|----|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 3 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | |
| A2 | 4 | 2 | 3 | 1 | 5 | 7 | 6 | 8 |
| B2 | 2 | 4 | 3 | 5 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 | |
| 3 | 2 | 5 | 4 | 1 | 7 | 8 | 6 | |
| B2 | 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 | |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 1 | |

| | | | | | | | | | | | | |
|----|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 3 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T | |
| A2 | 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T | |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T | |
| C1 | 4 | 2 | 6 | 3 | 5 | 1 | 7 | 9 | 8 | E | O | T |
| C1 | 2 | 4 | 3 | 6 | 5 | 7 | 1 | 9 | E | 8 | T | O |
| 2 | 3 | 4 | 5 | 6 | 7 | 9 | 1 | 8 | E | O | T | |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 9 | E | 8 | T | O | |
| 2 | 3 | 4 | 5 | 6 | 7 | 9 | 1 | 8 | E | O | T | |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 1 | E | T | O | |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | E | 1 | O | T | |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 1 | E | T | O | |
| D2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | E | 1 | O | T |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | E | O | 1 | T | |

| | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | E | O | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |

| | | | | | | | | | | | | | | | |
|----|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 | 15 | 16 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 11 | 14 | 13 | 16 | 15 |
| 3 | 2 | 3 | 4 | 5 | 6 | | | | | | | | | | |
| 2 | 1 | 4 | 3 | 6 | 5 | | | | | | | | | | |
| 2 | 4 | 1 | 3 | 5 | 6 | | | | | | | | | | |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | | | | | | | | |
| A2 | 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | | | | | | | |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | | | | | | | | |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | | | | | | | | |
| B2 | 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 | | | | | |
| 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 | | | | | | | | |
| 6 | 3 | 8 | 5 | 7 | 1 | 0 | 9 | | | | | | | | |
| 3 | 6 | 5 | 8 | 1 | 7 | 9 | 0 | 11 | 12 | 13 | 14 | 15 | 16 | | |
| D1 | 6 | 3 | 8 | 5 | 7 | 1 | 9 | 11 | 0 | 13 | 12 | 15 | 14 | 16 | |
| C1 | 3 | 6 | 5 | 8 | 7 | 9 | 1 | 11 | 13 | 0 | 15 | 12 | 16 | 14 | |

Adj. Int.

Extension C.

15

11

7

A B C D D D E F

A B C C D

A B B

Ad. int.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 8 |
| 2 | 4 | 3 | 5 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 1 | 7 | 8 | 6 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |

A1

B1

A2

B2

B2

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | 0 |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | 0 | 8 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | 0 |
| 3 | 2 | 5 | 4 | 1 | 7 | 9 | 6 | 0 | 8 |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | 0 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 | 9 | 0 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 0 | 9 |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 | 9 | 0 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 0 | 9 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | 9 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 7 | 1 |

A1

B1

A2

B2

B2

B2

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 5 | 7 | 6 | 9 | 8 | E | 0 | T |
| 2 | 4 | 3 | 5 | 1 | 7 | 9 | 6 | 8 | E | 0 | T |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | E | 0 | T |
| 3 | 2 | 5 | 4 | 1 | 7 | 9 | 6 | E | 8 | 0 | T |
| 2 | 3 | 4 | 5 | 7 | 1 | 6 | 9 | 8 | E | 0 | T |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 | 9 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 0 | 9 | T | E |
| 3 | 2 | 5 | 4 | 7 | 6 | 1 | 8 | 9 | 0 | E | T |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 1 | 0 | 9 | T | E |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | T | 9 | E |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | E | 9 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 1 | T | 9 | E |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | T | E | 9 | |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | 7 | E | 1 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 | |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | T | 7 | E | 1 | 9 |
| 6 | 4 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 | |
| 6 | 8 | 4 | 0 | 2 | T | 3 | E | 5 | 9 | 7 | 1 |

A1

B1

B1

A2

B2

B2

A B B / 15

A B B / 13

A B B / 11

A B B / 9

A B B / 7

Extension D

The other three Extensions of the Constructional Shunts are:-

| | | | | | |
|---|------------|------------|------------|------------|--------------|
| E | <u>ABB</u> | <u>BCC</u> | <u>CDD</u> | <u>DEE</u> | <u>EFF</u> → |
| | 7 | 11 | 15 | 19 | 23 |
| F | <u>ABB</u> | <u>ACD</u> | <u>ADF</u> | <u>AEH</u> | <u>AFK</u> → |
| | 7 | 11 | 15 | 19 | 23 |
| G | <u>ABB</u> | <u>BCC</u> | <u>CDD</u> | <u>DEE</u> | <u>EFF</u> → |
| | 7 | 9 | 11 | 13 | 15 |

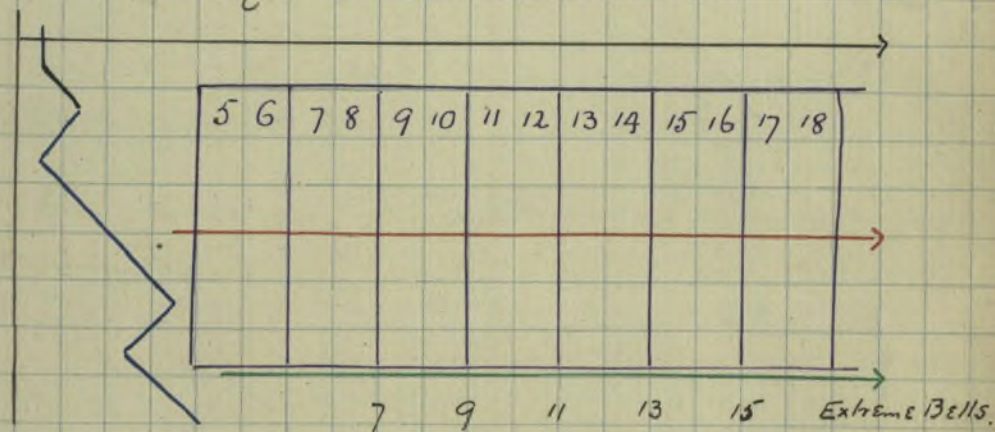
Each Lead of Bristol Surprise Major contains four similar, but independent, additional shunts.

The Additional Shunt consists of a Dodging Movement on four bells; three steps of Forward Hunting followed by three steps of Backward Hunting which is substituted for the three dodges produced by the Principle and the Constructional Shunt -

| | | |
|---------|------------|---------|
| 6 5 8 7 | instead of | 6 5 8 7 |
| 6 8 5 7 | | 5 6 7 8 |
| 8 6 7 5 | | 6 5 8 7 |
| 6 8 5 7 | | 5 6 7 8 |
| 6 5 8 7 | | 6 5 8 7 |
| 5 6 7 8 | | 5 6 7 8 |

As we have seen, (page 352) this Additional Shunt by itself can be extended in several ways. Actually its capacity for expansion is restricted by the room allowed by the extension of the Principle and the Constructional Shunt.

Extensions of Constructional Shunts A+B.



The expansion of the Constructional Shunt and the Principle increases the room available for the Additional Shunt, horizontally in regular progression. Vertically, the space remains constant.

Therefore the number of steps of Forward and Backward hunting will remain constant on all numbers.

That leaves three ways in which the

Additional Shunt can expand.

1. It may remain constant in size and position on all numbers;
2. It may remain constant in size but its position may be altered in regular progression;
3. It may increase in size in regular progression.

That gives us the following Extensions. -

(a)

| | | | | | | |
|-----------------|-----------------|------------------|------------------|------------------|------------------|---|
| $\frac{5-8}{7}$ | $\frac{5-8}{9}$ | $\frac{5-8}{11}$ | $\frac{5-8}{13}$ | $\frac{5-8}{15}$ | $\frac{5-8}{17}$ | → |
|-----------------|-----------------|------------------|------------------|------------------|------------------|---|

(b)

| | | | | | | |
|-----------------|------------------|-------------------|--------------------|--------------------|--------------------|---|
| $\frac{5-8}{7}$ | $\frac{7-10}{9}$ | $\frac{9-12}{11}$ | $\frac{11-14}{13}$ | $\frac{13-16}{15}$ | $\frac{15-18}{17}$ | → |
|-----------------|------------------|-------------------|--------------------|--------------------|--------------------|---|

(c)

| | | | | | | |
|-----------------|-------------------|-------------------|--------------------|--------------------|--------------------|---|
| $\frac{5-8}{7}$ | $\frac{7-10}{11}$ | $\frac{9-12}{15}$ | $\frac{11-14}{19}$ | $\frac{13-16}{23}$ | $\frac{15-18}{27}$ | → |
|-----------------|-------------------|-------------------|--------------------|--------------------|--------------------|---|

(d)

| | | | | | | |
|-----------------|------------------|-------------------|-------------------|-------------------|-------------------|---|
| $\frac{5-8}{7}$ | $\frac{5-10}{9}$ | $\frac{5-12}{11}$ | $\frac{5-14}{13}$ | $\frac{5-16}{15}$ | $\frac{5-18}{17}$ | → |
|-----------------|------------------|-------------------|-------------------|-------------------|-------------------|---|

EXTENSIONS OF CONSTRUCTIONAL SHUNTS A and B
EXTENSION OF ADDITIONAL SHUNT (a)

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|--|--|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | | |
| 1 | 2 | 3 | 4 | 6 | 8 | 5 | 7 | | |
| 2 | 1 | 4 | 3 | 8 | 6 | 7 | 5 | | |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 | | |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | | |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 6 | 8 | 5 | 7 | 9 | 0 |
| 2 | 1 | 4 | 3 | 8 | 6 | 7 | 5 | 0 | 9 |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 1 | 2 | 3 | 4 | 6 | 8 | 5 | 7 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 8 | 6 | 7 | 5 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 | 9 | 0 | E | T |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |

| | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 11 | 14 | 13 |
| 1 | 2 | 3 | 4 | 6 | 8 | 5 | 7 | 9 | 0 | 11 | 12 | 13 | 14 |
| 2 | 1 | 4 | 3 | 8 | 6 | 7 | 5 | 0 | 9 | 12 | 11 | 14 | 13 |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 | 9 | 0 | 11 | 12 | 13 | 14 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 11 | 14 | 13 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 |

EXTENSION OF ADDITIONAL SHUNT (b)

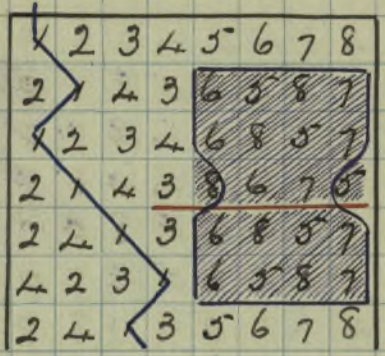
| | | | | | | | | | |
|---|---|---|---|---|---|---|---|--|--|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | | |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | | |
| 1 | 2 | 3 | 4 | 6 | 8 | 5 | 7 | | |
| 2 | 1 | 4 | 3 | 8 | 6 | 7 | 5 | | |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 | | |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | | |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 5 | 6 | 8 | 0 | 7 | 9 |
| 2 | 1 | 4 | 3 | 6 | 5 | 0 | 8 | 9 | 0 |
| 2 | 4 | 1 | 3 | 5 | 6 | 8 | 0 | 7 | 9 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |

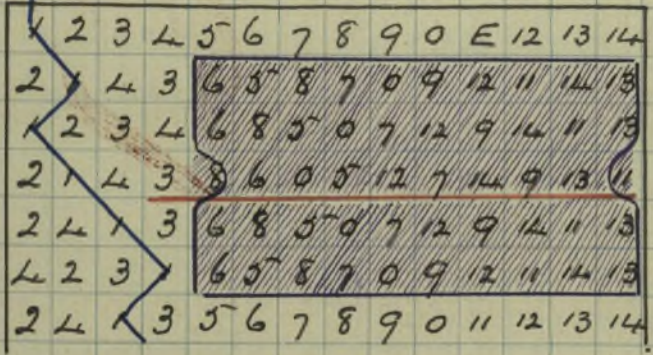
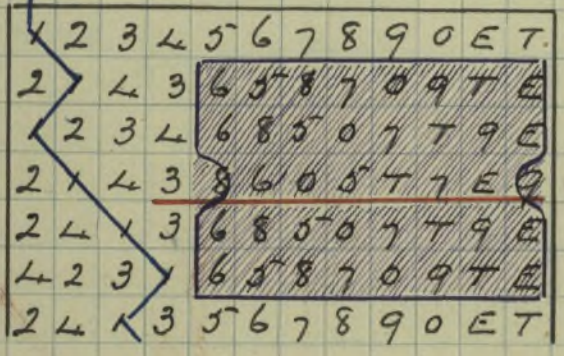
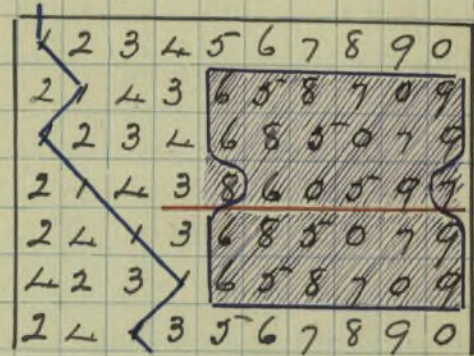
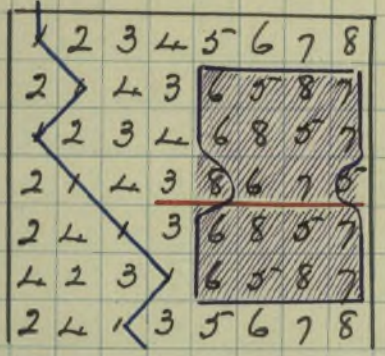
| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 0 | T | 9 | E |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 0 | E | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 0 | T | 9 | E |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |

| | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 11 | 14 | 13 |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 12 | 14 | 11 | 13 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 13 | 14 | 11 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | 12 | 14 | 11 | 13 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 | 12 | 11 | 14 | 13 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | 11 | 12 | 13 | 14 |

EXTENSION OF ADDITIONAL SHUNT (c)



EXTENSION OF ADDITIONAL SHUNT (d)



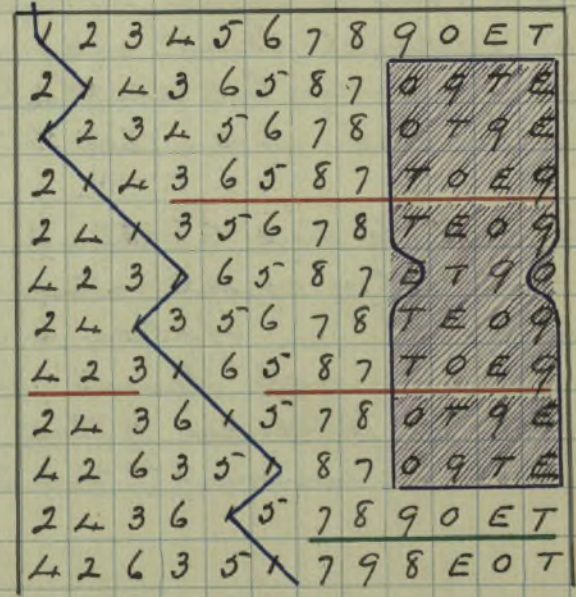
The Extension of the Constitutional Shunt No C page 356. gives increased room for the Additional Shunt, not only horizontally but also vertically. Therefore all the Extensions of the Additional Shunt given on p.p. 360-362. will apply; and in addition the following

1. The Additional Shunt may expand vertically, but remain constant horizontally;
2. The Additional Shunt may expand both vertically and horizontally;
3. The Additional Shunt may remain constant, in size both vertically and horizontally, but increase in number;
4. The Additional Shunt may remain constant vertically, but expand horizontally and also increase in number;

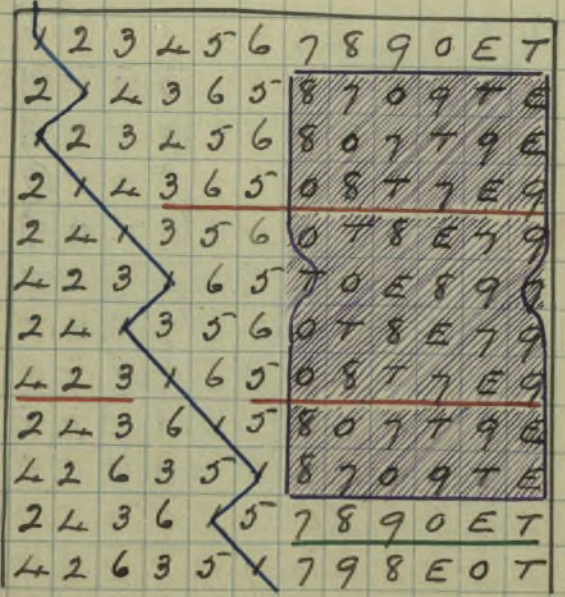
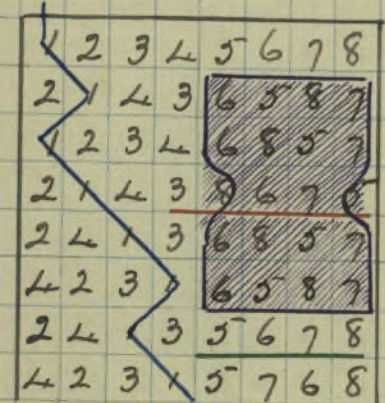
These will all be true Extensions, but they are not all of equal value. Those given on p.p. 360-362. applied to Extension C of the Constitutional Shunt will not remove all the falseness of that Extension. Neither will Extensions 1. and 2.

EXTENSION OF CONSTRUCTIONAL SHUNTS C

The Additional Shunt remains constant horizontally but Expands vertically



The Additional Shunt expands both horizontally and vertically



The Additional Shunt remains constant in size but expands in number.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 3 | 4 | 6 | 8 | 5 | 7 | |
| 2 | 4 | 3 | 8 | 6 | 7 | 5 | |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | |
| 4 | 2 | 3 | 5 | 7 | 6 | 8 | |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 3 | 4 | 6 | 8 | 5 | 7 | 0 | T | 9 | E | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | E | 9 | | |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 0 | T | 9 | E |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 3 | 5 | 6 | 8 | 0 | 7 | 9 | E | T | |
| 4 | 2 | 3 | 6 | 5 | 0 | 8 | 9 | E | T | | |
| 2 | 4 | 3 | 0 | 1 | 5 | 8 | 0 | 7 | 9 | E | T |
| 4 | 2 | 6 | 3 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 5 | 7 | 9 | 8 | E | 0 | T | |

The Additional Shunt remains constant vertically but expands horizontally; and in number.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 3 | 4 | 6 | 8 | 5 | 7 | |
| 2 | 4 | 3 | 8 | 6 | 7 | 5 | |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 7 |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | |
| 4 | 2 | 3 | 5 | 7 | 6 | 8 | |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 3 | 4 | 6 | 8 | 5 | 0 | 7 | T | 9 | E | |
| 2 | 4 | 3 | 8 | 6 | 0 | 5 | T | 7 | E | | |
| 2 | 4 | 1 | 3 | 6 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 3 | 5 | 6 | 8 | 0 | 7 | T | 9 | E | |
| 4 | 2 | 3 | 6 | 5 | 0 | 8 | T | 7 | E | | |
| 2 | 4 | 3 | 6 | 1 | 5 | 8 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 3 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 | E | T |
| 4 | 2 | 6 | 3 | 5 | 7 | 9 | 8 | E | 0 | T | |

The other three Additional Shunts Extend in exactly similar fashion to the examples given (p.p.).

Extensions of Constructional Shunts D and G -

The Additional Shunts in these expand as Extensions A and B (p.p. 360-362), except that in D, the Shunts below the Treble must remain constant on all numbers; and in G the Shunt above the Treble must remain constant on all numbers.

Extension of Constructional Shunt E -

The Additional Shunts in this expand as in Extensions A and B.

Extension of Constructional Shunt F -

The Additional Shunts cannot be applied to this.

The Extensions of Bristol Surprise Major are excellent examples of how an Add: Shunt which consists of a Dodging Movement can expand. They illustrate also the fact that an expanded Add: Shunt will not always perform the same duty in removing repetition of

Rows that its original does.

These Extensions also show the correct way in which the different Extensions of any Method should be worked out.

First, take the Principle and apply the Laws of Extension to it. See if there is more than one valid Extension.

Second, to each Extension of the Principle apply every possible valid Extension of the Constitutional Shuntis.

Thirdly, to each Extension of the Constitutional Shuntis apply every possible valid Extension of the Additional Shuntis, if there be any.

The result will be the total number of valid Extensions of the Method. There then arises the further question of the different values of these Extensions. I will deal with that presently.

In their natural form Slow Work Shunts are of no use in practical methods. Additional Shunts must be made to prevent the bells lying for more than two consecutive blows in any one position. Various Additional Shunts and combinations of Additional Shunts will do this; but no Shunt or combination of Shunts (with Extensions) will apply to every Slow Work Shunt. The two most & nearly universal are as follows;—

1. When there is an even number of Slow Work Bells they should dodge continually. This applies to every Principle.

2. On the Treble Bob Principle, when there is an odd number of Slow Work Bells, the Slow Work Bell next the other Bells should consecutively make places in the interior of the sections, the rest of the Slow Work Bells dodging continually.*

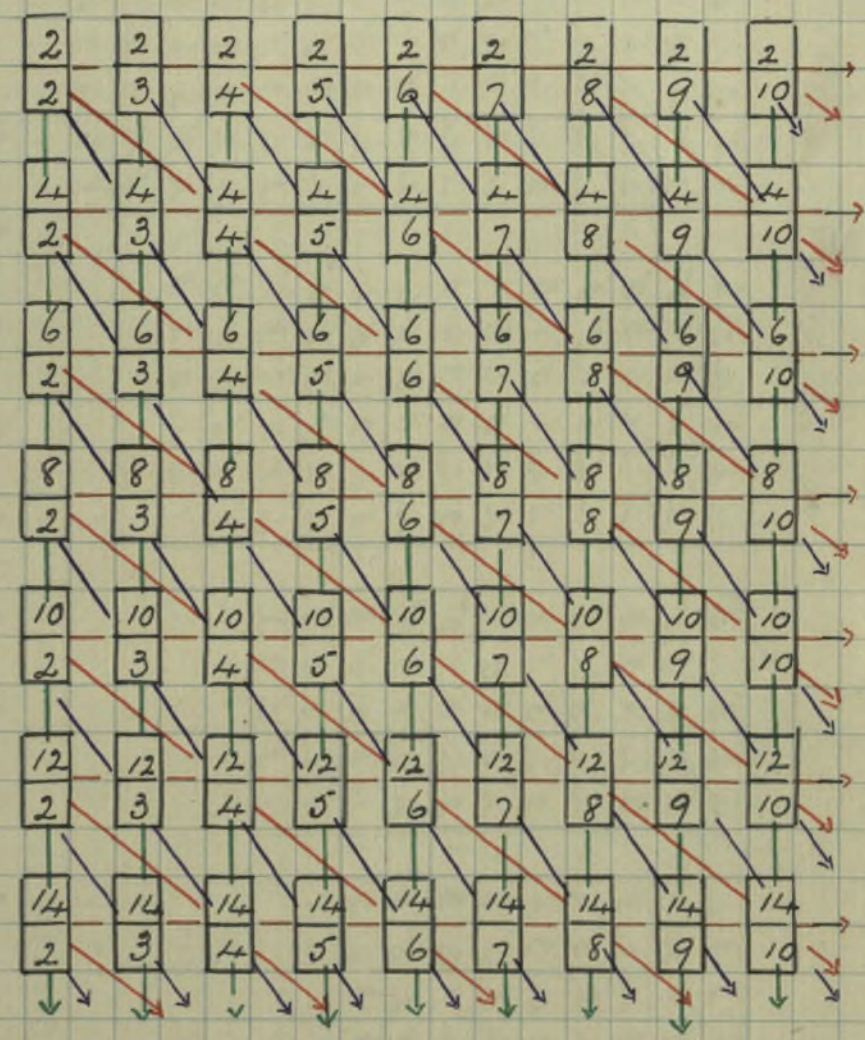
The following are the Extensions of these Shunts;—

* See pp. 210. 211.

In the Table the top figure in each symbol represents the number of Slow Work Bells
 The bottom figure represents the number of "Other" Bells including the Hunt of the Method.

In addition to the Extensions marked, if any two Symbols be connected by a straight line and that line prolonged to infinity the series of Symbols it passes through will represent a valid Extension.

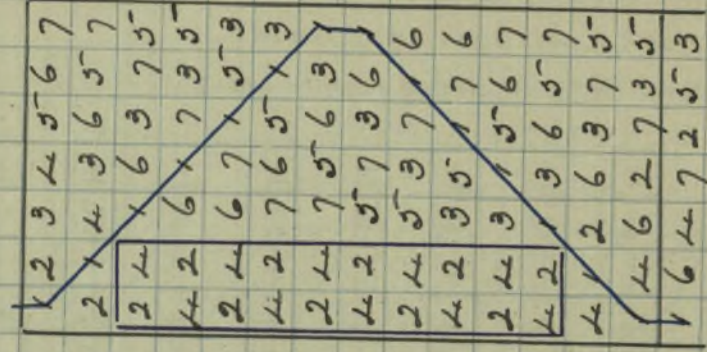
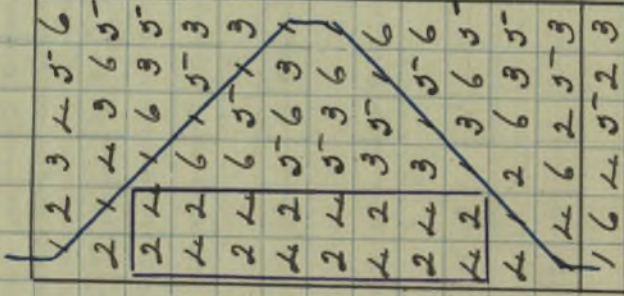
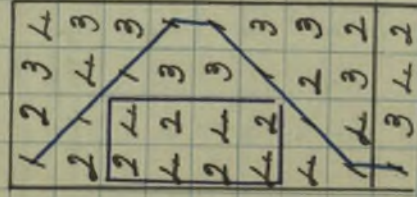
On All PRINCIPLES
 SLOW WORK CONSTRUCTIONAL SHUNT.
 Slow Work Bells to dodge continuously.



ad int.

Examples of EXTENSIONS from Formula page 369.

COLLEGE MINOR.

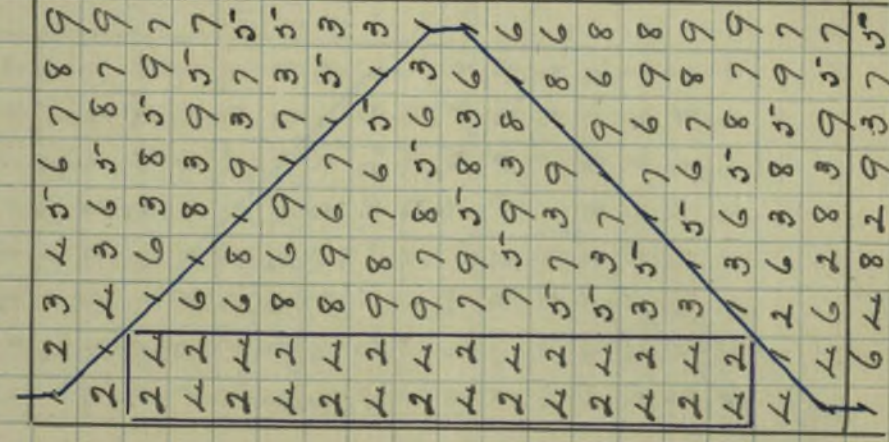
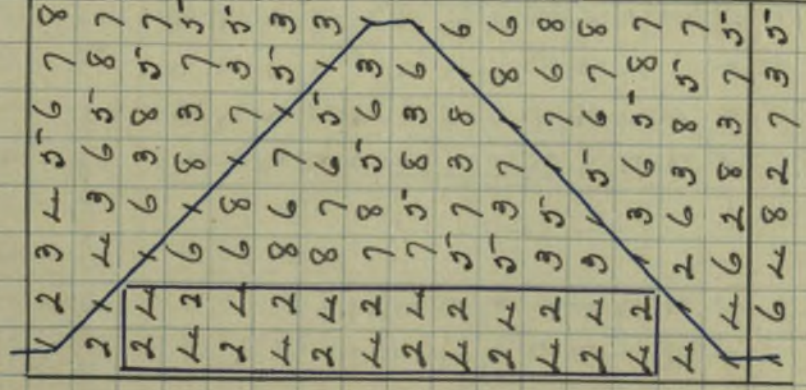


Example 1.

$$\frac{2}{2} \quad \frac{2}{3} \quad \frac{2}{4} \quad \frac{2}{5}$$

$$\frac{2}{6} \quad \frac{2}{7} \quad \frac{2}{8} \quad \frac{2}{9}$$

$$\frac{2}{10} \quad \rightarrow \text{ad inf.}$$



| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 2 | 4 | 3 | |
| 2 | 2 | 3 | |
| 2 | 2 | 3 | |
| 2 | 1 | 3 | |
| 4 | 1 | 3 | |
| 1 | 3 | 2 | |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 4 | 3 | 6 | 5 | |
| 2 | 4 | 6 | 3 | 5 | |
| 2 | 2 | 6 | 1 | 5 | 3 |
| 2 | 2 | 6 | 5 | 1 | 3 |
| 6 | 2 | 5 | 2 | 3 | |
| 6 | 2 | 5 | 2 | 3 | |
| 6 | 2 | 5 | 2 | 3 | |
| 6 | 5 | 4 | 1 | 2 | 3 |
| 5 | 6 | 4 | 3 | 2 | |
| 5 | 6 | 3 | 4 | 2 | |
| 5 | 3 | 6 | 2 | 4 | |
| 1 | 3 | 5 | 2 | 6 | 4 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 6 | 2 | 8 | 1 | 7 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 1 | 5 | 3 |
| 6 | 8 | 4 | 7 | 2 | 5 | 1 | 3 |
| 8 | 6 | 4 | 7 | 2 | 5 | 1 | 3 |
| 8 | 6 | 7 | 4 | 5 | 2 | | 3 |
| 8 | 7 | 6 | 5 | 4 | 1 | 2 | 3 |
| 7 | 8 | 5 | 6 | 1 | 4 | 3 | 2 |
| 7 | 5 | 8 | 1 | 6 | 3 | 4 | 2 |
| 5 | 7 | 1 | 8 | 3 | 6 | 2 | 4 |
| 5 | 7 | 7 | 3 | 8 | 2 | 6 | 4 |
| 5 | 3 | 7 | 2 | 8 | 4 | 6 | |
| 1 | 3 | 5 | 2 | 7 | 4 | 8 | 6 |

Example of Extension 2.

$$\frac{2}{2} \frac{4}{2} \frac{6}{2} \frac{8}{2} \frac{10}{2} \rightarrow \text{ad inf.}$$

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 2 | 6 | 2 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 1 | 9 | 3 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 0 | 1 | 3 |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 1 | 2 | 3 |
| 9 | 0 | 7 | 8 | 5 | 6 | 1 | 4 | 3 | 2 |
| 9 | 9 | 0 | 5 | 8 | 1 | 6 | 3 | 4 | 2 |
| 7 | 9 | 5 | 0 | 1 | 8 | 3 | 6 | 2 | 4 |
| 7 | 5 | 9 | 1 | 0 | 3 | 8 | 2 | 6 | 4 |
| 5 | 7 | 1 | 9 | 3 | 9 | 0 | 2 | 8 | 4 |
| 5 | 7 | 1 | 9 | 3 | 9 | 2 | 0 | 4 | 8 |
| 5 | 3 | 7 | 2 | 9 | 4 | 0 | 6 | 8 | |
| 1 | 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | T | E | E | |
| 2 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 9 | 7 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | E | 9 | 3 | 7 | 5 | |
| 8 | 6 | 0 | 4 | T | E | 2 | 9 | 1 | 7 | 5 | 3 |
| 8 | 0 | 6 | T | E | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 1 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 2 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 2 | 3 |
| T | E | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 1 | 2 | 3 |
| E | T | 9 | 0 | 7 | 8 | 5 | 6 | 1 | 4 | 3 | 2 |
| E | 9 | T | 7 | 0 | 5 | 8 | 1 | 6 | 3 | 4 | 2 |
| 9 | E | 7 | T | 5 | 0 | 1 | 8 | 3 | 6 | 2 | 4 |
| 9 | 7 | E | 5 | T | 1 | 0 | 3 | 8 | 2 | 6 | 4 |
| 7 | 9 | 5 | E | T | 3 | 0 | 2 | 8 | 4 | 6 | |
| 7 | 5 | 9 | 1 | E | 3 | T | 2 | 0 | 4 | 8 | 6 |

| | | | |
|---|---|---|---|
| 1 | 2 | 3 | 4 |
| 2 | 1 | 4 | 3 |
| 2 | 4 | 1 | 3 |
| 4 | 2 | 3 | 1 |
| 2 | 4 | 3 | 1 |
| 4 | 2 | 1 | 3 |
| 4 | 1 | 2 | 3 |
| 1 | 4 | 3 | 2 |
| 1 | 3 | 4 | 2 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 6 | 2 | 8 | 1 | 7 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 1 | 5 | 3 |
| 4 | 6 | 2 | 8 | 7 | 5 | 1 | 3 |
| 6 | 4 | 8 | 2 | 5 | 7 | 3 | 1 |
| 4 | 6 | 2 | 8 | 5 | 3 | 7 | 1 |
| 6 | 4 | 8 | 2 | 3 | 5 | 1 | 7 |
| 4 | 6 | 2 | 8 | 3 | 5 | 7 | 1 |
| 6 | 4 | 8 | 2 | 1 | 3 | 7 | 5 |
| 6 | 8 | 4 | 1 | 2 | 7 | 3 | 5 |
| 8 | 6 | 4 | 7 | 2 | 5 | 3 | 1 |
| 8 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| 1 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |

Example of Extension 3.

| | | | | | | | | |
|---|---|---|---|----|----|----|----|-----------|
| 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | → ad inf. |
| 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | 7 | 1 | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 1 | 9 | 3 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | T | E | 9 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 4 | T | 2 | 9 | E | 7 | 1 | 5 | 3 |
| 6 | 8 | 4 | 0 | 2 | T | 9 | 7 | E | 5 | 1 | 3 |
| 8 | 6 | 0 | 4 | T | 2 | 7 | 9 | 5 | E | 3 | 1 |
| 6 | 8 | 4 | 0 | 2 | T | 7 | 5 | 9 | 3 | E | 1 |
| 8 | 6 | 0 | 4 | T | 2 | 5 | 7 | 3 | 9 | 1 | E |
| 6 | 8 | 4 | 0 | 2 | T | 5 | 3 | 7 | 1 | 9 | E |
| 8 | 6 | 0 | 4 | T | 2 | 3 | 5 | 1 | 7 | E | 9 |
| 6 | 8 | 4 | 0 | 2 | T | 3 | 1 | 5 | E | 7 | 9 |
| 8 | 6 | 0 | 4 | T | 2 | 1 | 3 | E | 5 | 9 | 7 |
| 8 | 0 | 6 | T | 4 | 1 | 2 | E | 3 | 9 | 5 | 7 |
| 0 | 8 | T | 6 | 4 | E | 2 | 9 | 3 | 7 | 5 | 1 |
| 0 | T | 8 | 6 | E | 4 | 9 | 2 | 7 | 3 | 5 | 1 |
| T | 0 | 8 | E | 6 | 9 | 4 | 9 | 2 | 5 | 3 | 1 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| T | E | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| E | T | 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 | 1 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 1 | 4 | 3 | 6 | 5 |
| 2 | 4 | 1 | 6 | 3 | 5 |
| 4 | 2 | 6 | 1 | 5 | 3 |
| 2 | 4 | 6 | 5 | 1 | 3 |
| 4 | 2 | 5 | 6 | 3 | 1 |
| 2 | 4 | 5 | 3 | 6 | 1 |
| 4 | 2 | 3 | 5 | 1 | 6 |
| 2 | 4 | 3 | 1 | 5 | 6 |
| 4 | 2 | 1 | 3 | 6 | 5 |
| 4 | 2 | 6 | 3 | 5 | 1 |
| 4 | 6 | 2 | 5 | 3 | 1 |
| 1 | 6 | 4 | 5 | 2 | 3 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 6 | 2 | 8 | 1 | 7 | 3 | 5 |
| 6 | 4 | 8 | 2 | 7 | 1 | 5 | 3 |
| 4 | 6 | 2 | 8 | 7 | 5 | 1 | 3 |
| 6 | 4 | 8 | 2 | 5 | 7 | 3 | 1 |
| 4 | 6 | 2 | 8 | 5 | 3 | 7 | 1 |
| 6 | 4 | 8 | 2 | 3 | 5 | 1 | 7 |
| 4 | 6 | 2 | 8 | 3 | 1 | 5 | 7 |
| 6 | 4 | 8 | 2 | 1 | 3 | 7 | 5 |
| 6 | 8 | 4 | 1 | 2 | 7 | 3 | 5 |
| 8 | 6 | 4 | 7 | 2 | 5 | 3 | 1 |
| 8 | 1 | 6 | 7 | 4 | 5 | 2 | 3 |
| 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| 1 | 7 | 8 | 5 | 6 | 3 | 4 | 2 |

Example of Extension A.

| | | | | | |
|---|---|---|---|----|---------|
| 2 | 4 | 6 | 8 | 10 | → admf. |
| 4 | 4 | 4 | 4 | 4 | |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 6 | 4 | 8 | 2 | 0 | 1 | 9 | 3 | 7 | 5 |
| 6 | 8 | 4 | 0 | 2 | 9 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 6 | 8 | 4 | 0 | 2 | 9 | 7 | 5 | 1 | 3 |
| 8 | 6 | 0 | 4 | 9 | 2 | 5 | 7 | 3 | 1 |
| 6 | 8 | 4 | 0 | 2 | 9 | 5 | 3 | 7 | 1 |
| 8 | 6 | 0 | 4 | 9 | 2 | 3 | 5 | 1 | 7 |
| 6 | 8 | 4 | 0 | 2 | 9 | 3 | 1 | 5 | 7 |
| 8 | 6 | 0 | 4 | 9 | 2 | 1 | 3 | 7 | 5 |
| 8 | 0 | 6 | 9 | 4 | 1 | 2 | 7 | 3 | 5 |
| 0 | 8 | 9 | 6 | 1 | 4 | 7 | 2 | 5 | 3 |
| 0 | 9 | 8 | 1 | 6 | 7 | 4 | 5 | 2 | 3 |
| 9 | 0 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| 9 | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 | 1 |
| 9 | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 | 1 |
| 1 | 7 | 9 | 5 | 0 | 3 | 8 | 2 | 6 | 4 |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 6 | 2 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | 1 | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 1 | 9 | 3 | 7 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 1 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 1 | 5 | 3 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 7 | 5 | 1 | 3 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 5 | 7 | 3 | 1 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 5 | 3 | 7 | 1 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 3 | 5 | 1 | 7 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 3 | 1 | 5 | 7 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 1 | 3 | 7 | 5 |
| 0 | T | 8 | E | 6 | 9 | 4 | 1 | 2 | 7 | 3 | 5 |
| T | 0 | E | 8 | 9 | 6 | 1 | 4 | 7 | 2 | 5 | 3 |
| T | E | 0 | 9 | 8 | 6 | 7 | 4 | 5 | 2 | 3 | 1 |
| E | T | 9 | 0 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |
| E | 9 | T | 0 | 7 | 8 | 5 | 6 | 3 | 4 | 2 | 1 |
| 9 | E | T | 7 | 0 | 5 | 8 | 3 | 6 | 2 | 4 | 1 |
| 9 | E | 7 | T | 5 | 0 | 3 | 8 | 2 | 6 | 4 | 1 |
| 9 | 7 | E | 5 | T | 3 | 0 | 2 | 8 | 4 | 6 | 1 |

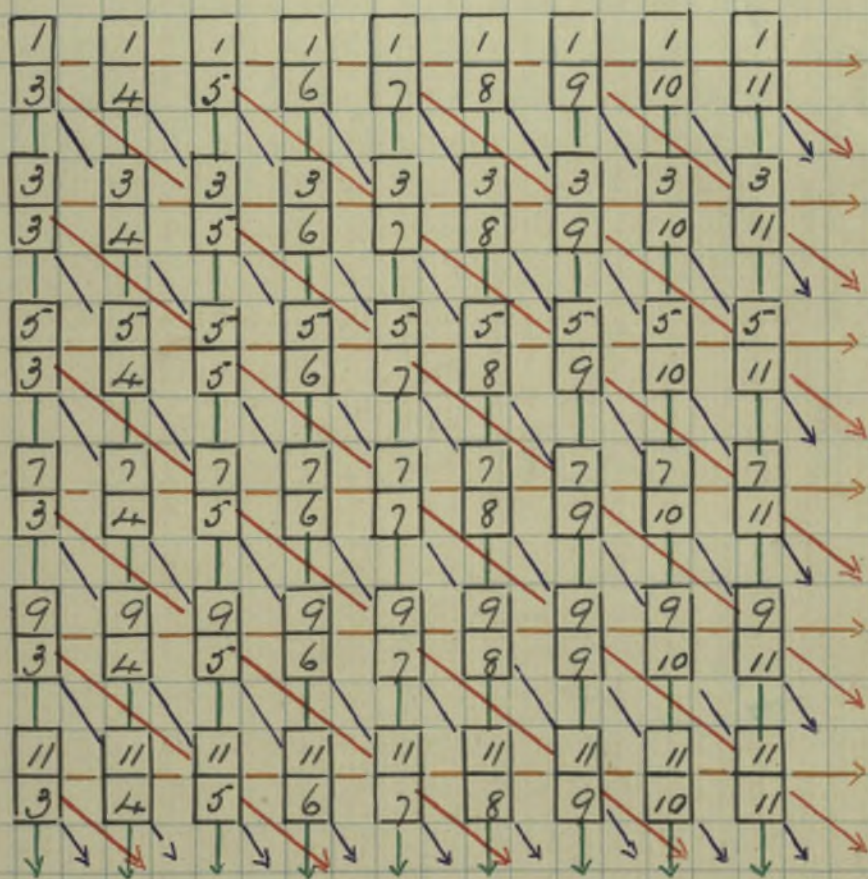
TREBLE BOB PRINCIPLE

SLOW WORK CONSTRUCTIONAL SHUNTS

Nos of Slow Work Bells to be odd.

Slow Work Bell nearest to Other Bells to make
Place consecutively in interior of Section.

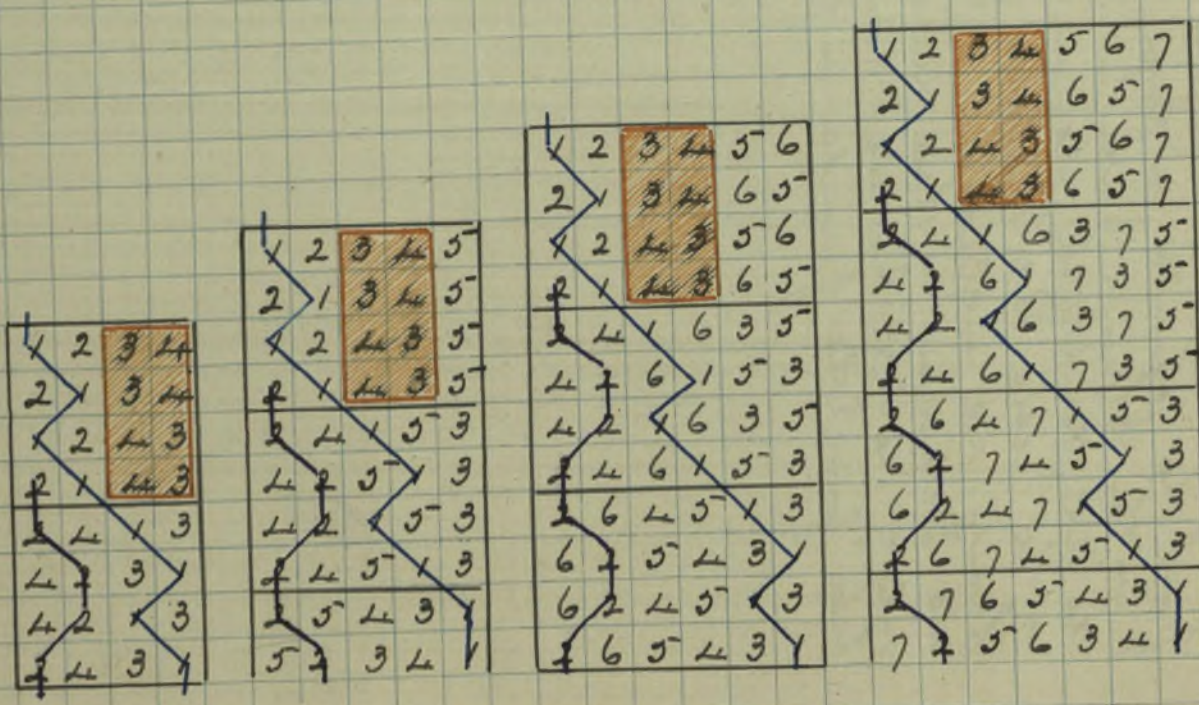
The Rest of the Slow Work Bells to dodge continuously.



Ad. int.

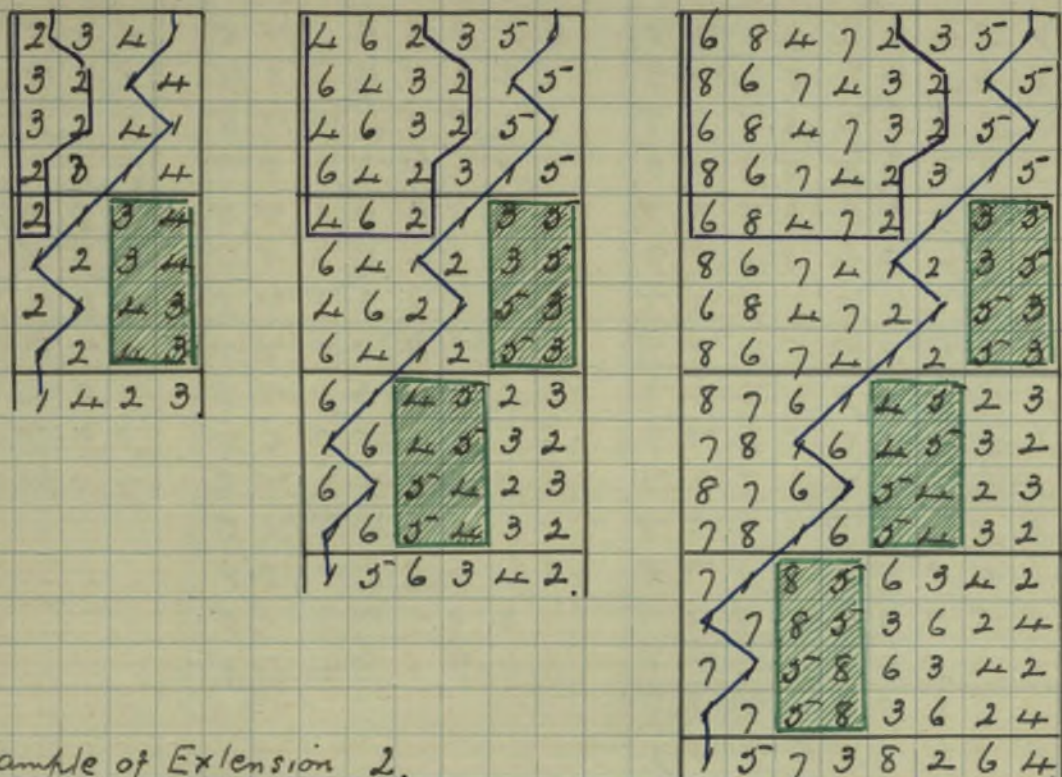
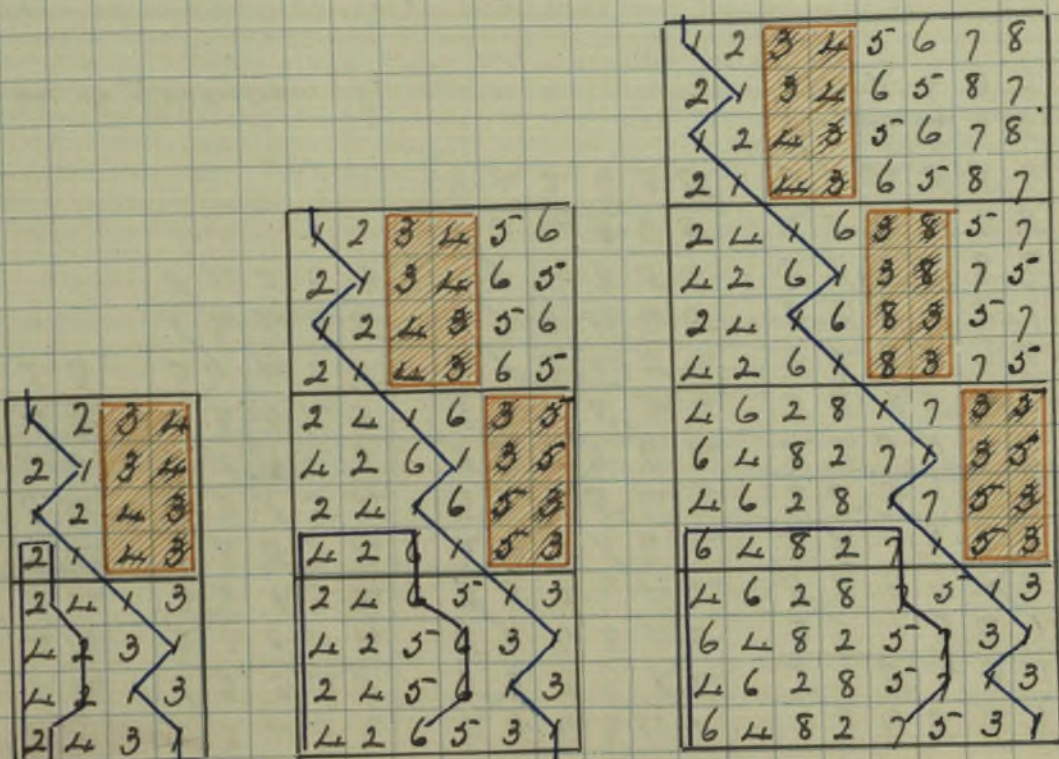
The following are examples of Extension
from the formula on page 374.

As the Shuntis given in that formula
do not completely remove the falseness
of the Treble Bob Principle other Add:
Shuntis are included. I have given
one Extension of these Additional Shuntis
only. The full number possible can be
had from the formula on p.p. 340, 341.



Example of Extension 1.

$\frac{1}{3} \quad \frac{1}{4} \quad \frac{1}{5} \quad \frac{1}{6} \quad \frac{1}{7} \quad \frac{1}{8} \quad \frac{1}{9} \quad \frac{1}{10} \quad \frac{1}{11} \rightarrow \text{Ad. inf.}$



Example of Extension 2.

| | | | | | | | | |
|---|---|---|---|---|----|----|----|----------|
| 1 | 3 | 5 | 7 | 9 | 11 | 13 | 15 | → Adint. |
| 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | |

| | | |
|-------------|-----------------|---------------------|
| 1 2 3 4 5 6 | 1 2 3 4 5 6 7 8 | 1 2 3 4 5 6 7 8 9 0 |
| 2 1 3 4 6 5 | 2 1 3 4 6 5 8 7 | 2 1 3 4 6 5 8 7 0 9 |
| 1 2 4 3 5 6 | 1 2 4 3 5 6 7 8 | 1 2 4 3 5 6 7 8 9 0 |
| 2 1 4 3 6 5 | 2 1 4 3 6 5 8 7 | 2 1 4 3 6 5 8 7 0 9 |
| 2 4 1 6 3 5 | 2 4 1 6 3 8 5 7 | 2 4 1 6 3 8 5 0 7 9 |
| 4 2 6 1 5 3 | 4 2 6 1 3 8 7 5 | 4 2 6 1 3 8 0 5 9 7 |
| 4 2 1 6 3 5 | 2 4 6 1 8 3 5 7 | 2 4 6 1 8 3 5 0 7 9 |
| 2 4 6 1 5 3 | 4 2 6 1 8 3 7 5 | 4 2 6 1 8 3 0 5 9 7 |
| 2 4 6 1 5 3 | 2 4 6 8 1 7 3 5 | 4 6 2 8 1 0 3 9 5 7 |
| 2 6 4 5 1 3 | 4 2 8 6 7 1 5 3 | 6 4 8 2 0 3 9 7 5 |
| 6 2 5 4 3 1 | 2 4 8 6 1 7 3 5 | 4 6 2 8 0 9 3 5 7 |
| 6 2 4 5 1 3 | 4 2 6 8 7 1 5 3 | 6 4 8 2 0 9 3 7 5 |
| 2 6 5 4 3 1 | 2 4 6 7 8 5 1 3 | 4 6 2 8 0 9 1 7 3 5 |
| | 4 2 7 6 5 8 3 1 | 6 4 8 2 9 0 7 1 5 3 |
| | 2 4 7 6 8 5 1 3 | 4 6 2 8 9 0 1 7 3 5 |
| | 4 2 6 7 5 8 3 1 | 6 4 8 2 0 9 7 1 5 3 |
| | | 4 6 2 8 0 7 9 5 1 3 |
| | | 6 4 8 2 7 0 5 9 3 1 |
| | | 4 6 2 8 7 0 9 5 1 3 |
| | | 6 4 8 2 0 7 5 9 3 1 |

| | | |
|-------------|-------------------|-----------------------|
| 2 5 6 3 4 1 | 4 6 2 1 5 7 3 8 1 | 6 8 4 0 2 1 5 7 3 9 1 |
| 5 2 3 6 1 4 | 6 4 5 2 3 7 1 8 | 8 6 0 4 5 2 3 7 1 9 |
| 5 3 6 3 4 1 | 4 6 5 2 7 3 8 1 | 6 8 4 0 5 2 7 3 9 1 |
| 2 5 3 6 1 4 | 6 4 2 5 3 7 1 8 | 8 6 0 4 2 5 3 7 1 9 |
| 2 3 5 1 6 4 | 4 6 2 3 5 1 7 8 | 6 8 4 0 2 3 5 1 7 9 |
| 3 2 1 5 4 6 | 6 4 3 2 1 5 8 7 | 8 6 0 4 3 2 1 5 9 7 |
| 3 2 5 1 6 4 | 4 6 3 2 5 1 7 8 | 6 8 4 0 3 2 5 1 7 9 |
| 2 3 1 5 4 6 | 6 4 2 3 1 5 8 7 | 8 6 0 4 2 3 1 5 9 7 |
| 2 3 4 5 6 | 4 6 2 1 3 8 5 7 | 6 8 4 0 2 1 3 9 5 7 |
| 2 3 4 6 5 | 6 4 2 3 8 7 5 | 8 6 0 4 2 3 9 7 5 |
| 2 4 3 5 6 | 4 6 2 8 3 5 7 | 6 8 4 0 2 1 9 3 5 7 |
| 2 4 3 6 5 | 6 4 1 2 8 3 7 5 | 8 6 0 4 2 3 9 3 7 5 |
| 1 4 2 6 3 5 | 6 1 4 8 2 7 3 5 | 8 0 6 1 4 9 2 7 3 5 |
| | 6 4 8 7 2 5 3 | 0 8 6 4 9 7 2 5 3 |
| | 6 8 4 2 7 3 5 | 8 0 6 9 4 2 7 3 5 |
| | 6 8 4 7 2 5 3 | 0 8 6 9 4 7 2 5 3 |
| | 1 8 6 7 4 5 2 3 | 0 1 8 9 6 7 4 5 2 3 |
| | | 1 0 8 9 7 6 5 4 3 2 |
| | | 0 9 8 6 7 4 5 2 3 |
| | | 1 0 9 8 7 6 5 4 3 2 |
| | | 1 9 0 7 8 5 6 3 4 2 |

Example of Extension 3.

| | | | | | | |
|---|---|---|---|---|----|------|
| 1 | 3 | 5 | 7 | 9 | 11 | Ad. |
| 5 | 5 | 5 | 5 | 5 | 5 | inf. |

The following (pp. 380-389) are examples of the Extension of Methods which have overlapping Additional Premises. The Lead marked A is produced from the Principle. The Lead marked B is produced from A; C is produced from B and so on. These are not given as the only possible extension in each particular instance; or even, necessarily, as the best extension. But as typical examples illustrating laws applicable to methods in general. On pp. 383-385 is an illustration of the Extension of a B-S Count Premise (p. 218).

A.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 1 | 8 | 3 | 7 | 5 |
| 4 | 2 | 6 | 8 | 1 | 3 | 7 | 5 |
| 2 | 4 | 8 | 6 | 3 | 1 | 5 | 7 |
| 2 | 8 | 4 | 3 | 6 | 5 | 1 | 7 |
| 8 | 2 | 3 | 4 | 5 | 6 | 7 | 1 |
| 8 | 3 | 2 | 5 | 4 | 7 | 6 | 1 |
| 3 | 8 | 5 | 2 | 7 | 4 | 1 | 6 |
| 3 | 5 | 8 | 7 | 2 | 1 | 4 | 6 |
| 5 | 3 | 7 | 8 | 1 | 2 | 6 | 4 |
| 5 | 3 | 7 | 1 | 8 | 2 | 6 | 4 |
| 3 | 5 | 7 | 2 | 8 | 4 | 6 | 1 |
| 3 | 5 | 2 | 7 | 4 | 8 | 6 | 1 |
| 3 | 2 | 5 | 4 | 7 | 6 | 8 | 1 |
| 3 | 5 | 2 | 7 | 4 | 8 | 6 | 1 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 2 | 6 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 2 | 4 | 8 | 6 | 0 | 1 | 9 | 3 | 7 | 5 |
| 4 | 2 | 6 | 0 | 6 | 9 | 1 | 3 | 7 | 5 |
| 8 | 2 | 0 | 4 | 9 | 6 | 3 | 1 | 5 | 7 |
| 8 | 0 | 2 | 9 | 4 | 3 | 6 | 5 | 1 | 7 |
| 0 | 8 | 9 | 2 | 3 | 4 | 5 | 6 | 7 | 1 |
| 0 | 9 | 8 | 3 | 2 | 5 | 4 | 7 | 6 | 1 |
| 9 | 0 | 3 | 8 | 5 | 2 | 7 | 4 | 1 | 6 |
| 9 | 3 | 0 | 5 | 8 | 7 | 2 | 1 | 4 | 6 |
| 3 | 9 | 5 | 0 | 7 | 8 | 1 | 2 | 6 | 4 |
| 3 | 5 | 9 | 7 | 0 | 1 | 8 | 2 | 6 | 4 |
| 5 | 3 | 7 | 9 | 1 | 0 | 2 | 8 | 4 | 6 |
| 5 | 3 | 7 | 1 | 9 | 2 | 0 | 4 | 8 | 6 |
| 3 | 5 | 1 | 7 | 2 | 9 | 4 | 0 | 6 | 8 |
| 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 | 1 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 0 | 1 |
| 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 | 1 |

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|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 2 | 4 | 1 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 4 | 2 | 6 | 1 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 4 | 2 | 6 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 2 | 4 | 8 | 6 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 2 | 8 | 4 | 0 | 6 | T | 1 | E | 3 | 9 | 5 | 7 |
| 8 | 2 | 0 | 4 | T | 6 | E | 1 | 9 | 3 | 7 | 5 |
| 8 | 0 | 2 | T | 4 | E | 6 | 9 | 1 | 3 | 7 | 5 |
| 0 | 8 | T | 2 | E | 4 | 9 | 6 | 3 | 1 | 5 | 7 |
| 0 | T | 8 | E | 2 | 9 | 4 | 3 | 6 | 5 | 1 | 7 |
| T | 0 | E | 8 | 9 | 2 | 3 | 4 | 5 | 6 | 7 | 1 |
| T | E | 0 | 9 | 8 | 3 | 2 | 5 | 4 | 7 | 6 | 1 |
| E | T | 9 | 0 | 3 | 8 | 5 | 2 | 7 | 4 | 1 | 6 |
| E | 9 | T | 3 | 0 | 5 | 8 | 7 | 2 | 1 | 4 | 6 |
| 9 | E | 3 | T | 5 | 0 | 7 | 8 | 1 | 2 | 6 | 4 |
| 9 | 3 | E | 5 | T | 7 | 0 | 1 | 8 | 2 | 6 | 4 |
| 3 | 9 | 5 | E | 7 | T | 1 | 0 | 2 | 8 | 4 | 6 |
| 3 | 5 | 9 | 7 | E | 1 | T | 2 | 0 | 4 | 8 | 6 |
| 5 | 3 | 7 | 9 | 1 | E | 2 | T | 4 | 0 | 6 | 8 |
| 5 | 3 | 7 | 1 | 9 | 2 | E | 4 | T | 6 | 0 | 8 |
| 3 | 5 | 1 | 7 | 2 | 9 | 4 | E | 6 | T | 8 | 0 |
| 3 | 5 | 2 | 7 | 4 | 9 | 6 | E | 8 | T | 0 | 1 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | E | 0 | T | 1 |
| 3 | 5 | 2 | 7 | 4 | 9 | 6 | E | 8 | T | 0 | 1 |

B.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 4 | 5 | 6 | 8 | 7 |
| 2 | 3 | 1 | 5 | 4 | 8 | 6 | 7 |
| 3 | 2 | 5 | 1 | 8 | 4 | 6 | 7 |
| 3 | 2 | 5 | 8 | 1 | 4 | 7 | 6 |
| 2 | 3 | 8 | 5 | 4 | 1 | 6 | 7 |
| 2 | 8 | 3 | 4 | 5 | 6 | 1 | 7 |
| 8 | 2 | 3 | 4 | 5 | 6 | 7 | 1 |
| 8 | 3 | 2 | 5 | 4 | 7 | 6 | 1 |
| 3 | 8 | 2 | 5 | 4 | 7 | 1 | 6 |
| 3 | 2 | 8 | 4 | 5 | 1 | 7 | 6 |
| 2 | 3 | 4 | 8 | 1 | 5 | 6 | 7 |
| 2 | 3 | 4 | 1 | 8 | 5 | 6 | 7 |
| 3 | 2 | 4 | 5 | 8 | 7 | 6 | 1 |
| 3 | 1 | 2 | 5 | 4 | 7 | 8 | 6 |
| 3 | 2 | 5 | 4 | 7 | 6 | 8 | 1 |
| 1 | 3 | 5 | 2 | 7 | 4 | 8 | 6 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 3 | 4 | 5 | 6 | 8 | 7 | 0 | 9 |
| 2 | 3 | 1 | 5 | 4 | 8 | 6 | 0 | 7 | 9 |
| 3 | 2 | 5 | 1 | 8 | 4 | 0 | 6 | 9 | 7 |
| 3 | 2 | 5 | 8 | 1 | 0 | 4 | 9 | 6 | 7 |
| 2 | 3 | 8 | 5 | 0 | 1 | 9 | 4 | 7 | 6 |
| 2 | 8 | 3 | 0 | 5 | 9 | 1 | 4 | 7 | 6 |
| 8 | 2 | 0 | 3 | 9 | 5 | 4 | 1 | 6 | 7 |
| 8 | 0 | 2 | 9 | 3 | 4 | 5 | 6 | 1 | 7 |
| 0 | 8 | 9 | 2 | 3 | 4 | 5 | 6 | 7 | 1 |
| 0 | 9 | 8 | 3 | 2 | 5 | 4 | 7 | 6 | 1 |
| 9 | 0 | 3 | 8 | 2 | 5 | 4 | 7 | 1 | 6 |
| 9 | 3 | 0 | 2 | 8 | 4 | 5 | 1 | 7 | 6 |
| 3 | 9 | 2 | 0 | 4 | 8 | 1 | 5 | 6 | 7 |
| 3 | 2 | 9 | 4 | 0 | 1 | 8 | 5 | 6 | 7 |
| 2 | 3 | 4 | 9 | 1 | 0 | 5 | 8 | 7 | 6 |
| 2 | 3 | 4 | 1 | 9 | 5 | 0 | 7 | 8 | 6 |
| 3 | 2 | 4 | 5 | 9 | 7 | 0 | 6 | 8 | 1 |
| 3 | 1 | 2 | 5 | 4 | 7 | 9 | 6 | 0 | 8 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 0 | 1 |
| 1 | 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 |

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|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 3 | 4 | 5 | 6 | 8 | 7 | 0 | 9 | T | E |
| 2 | 3 | 1 | 5 | 4 | 8 | 6 | 0 | 7 | T | 9 | E |
| 3 | 2 | 5 | 1 | 8 | 4 | 0 | 6 | T | 7 | E | 9 |
| 3 | 2 | 5 | 8 | 1 | 0 | 4 | T | 6 | E | 7 | 9 |
| 2 | 3 | 8 | 5 | 0 | 1 | T | 4 | E | 6 | 9 | 7 |
| 2 | 8 | 3 | 0 | 5 | T | 1 | E | 4 | 9 | 6 | 7 |
| 8 | 2 | 0 | 3 | T | 5 | E | 1 | 9 | 4 | 7 | 6 |
| 8 | 0 | 2 | T | 3 | E | 5 | 9 | 1 | 4 | 7 | 6 |
| 0 | 8 | T | 2 | E | 3 | 9 | 5 | 4 | 1 | 6 | 7 |
| 0 | T | 8 | E | 2 | 9 | 3 | 4 | 5 | 6 | 1 | 7 |
| T | 0 | E | 8 | 9 | 2 | 3 | 4 | 5 | 6 | 7 | 1 |
| T | E | 0 | 9 | 8 | 3 | 2 | 5 | 4 | 7 | 6 | 1 |
| E | T | 9 | 0 | 3 | 8 | 2 | 5 | 4 | 7 | 1 | 6 |
| E | 9 | T | 3 | 0 | 2 | 8 | 4 | 5 | 1 | 7 | 6 |
| 9 | E | 3 | T | 2 | 0 | 4 | 8 | 1 | 5 | 6 | 7 |
| 9 | 8 | E | 2 | T | 4 | 0 | 8 | 5 | 6 | 7 | 1 |
| 3 | 9 | 2 | E | 4 | T | 1 | 0 | 5 | 8 | 7 | 6 |
| 3 | 2 | 9 | 4 | E | 1 | T | 5 | 0 | 7 | 8 | 6 |
| 2 | 3 | 4 | 9 | 1 | E | 5 | T | 7 | 0 | 6 | 8 |
| 2 | 3 | 4 | 1 | 9 | 5 | E | 7 | T | 6 | 0 | 8 |
| 3 | 2 | 4 | 5 | 9 | 7 | E | 6 | T | 8 | 0 | 1 |
| 3 | 1 | 2 | 5 | 4 | 7 | 9 | 6 | E | 8 | T | 0 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | E | 0 | T | 1 |
| 1 | 3 | 5 | 2 | 7 | 4 | 9 | 6 | E | 8 | T | 0 |

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|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 5 | 4 | 6 | 8 | 7 |
| 2 | 3 | 1 | 4 | 5 | 8 | 6 | 7 |
| 3 | 2 | 4 | 1 | 8 | 5 | 7 | 6 |
| 2 | 3 | 4 | 8 | 1 | 5 | 6 | 7 |
| 3 | 2 | 8 | 4 | 5 | 1 | 7 | 6 |
| 3 | 8 | 2 | 5 | 4 | 7 | 1 | 6 |
| 8 | 3 | 2 | 4 | 5 | 7 | 6 | 1 |
| 8 | 2 | 3 | 5 | 4 | 6 | 7 | 1 |
| 2 | 8 | 3 | 4 | 5 | 6 | 1 | 7 |
| 2 | 3 | 8 | 5 | 4 | 1 | 6 | 7 |
| 3 | 2 | 5 | 8 | 1 | 4 | 7 | 6 |
| 2 | 3 | 5 | 1 | 8 | 4 | 6 | 7 |
| 3 | 2 | 1 | 5 | 4 | 8 | 7 | 6 |
| 3 | 1 | 2 | 4 | 5 | 7 | 8 | 6 |
| 3 | 2 | 5 | 4 | 7 | 6 | 8 | |
| 1 | 3 | 5 | 2 | 7 | 4 | 8 | 6 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 3 | 5 | 4 | 6 | 8 | 7 | 0 | 9 |
| 2 | 3 | 1 | 4 | 5 | 8 | 6 | 0 | 7 | 9 |
| 3 | 2 | 4 | 1 | 8 | 5 | 0 | 6 | 9 | 7 |
| 2 | 3 | 4 | 8 | 1 | 0 | 5 | 9 | 6 | 7 |
| 3 | 2 | 8 | 4 | 0 | 1 | 9 | 5 | 7 | 6 |
| 3 | 8 | 2 | 0 | 4 | 9 | 1 | 5 | 6 | 7 |
| 8 | 3 | 0 | 2 | 9 | 4 | 5 | 1 | 7 | 6 |
| 8 | 0 | 3 | 9 | 2 | 5 | 4 | 7 | 1 | 6 |
| 0 | 8 | 9 | 3 | 2 | 4 | 5 | 7 | 6 | 1 |
| 0 | 9 | 8 | 2 | 3 | 5 | 4 | 6 | 7 | 1 |
| 9 | 0 | 2 | 8 | 3 | 4 | 5 | 6 | 7 | 1 |
| 9 | 2 | 0 | 3 | 8 | 5 | 4 | 1 | 6 | 7 |
| 2 | 9 | 3 | 0 | 5 | 8 | 1 | 4 | 7 | 6 |
| 2 | 3 | 9 | 5 | 0 | 1 | 8 | 4 | 6 | 7 |
| 3 | 2 | 5 | 9 | 1 | 0 | 4 | 8 | 7 | 6 |
| 2 | 3 | 5 | 1 | 9 | 4 | 0 | 7 | 8 | 6 |
| 3 | 2 | 5 | 4 | 9 | 7 | 0 | 6 | 8 | |
| 3 | 2 | 4 | 5 | 7 | 9 | 6 | 0 | 8 | |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | 0 | |
| 1 | 3 | 5 | 2 | 7 | 4 | 9 | 6 | 0 | 8 |

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|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 1 | 3 | 5 | 4 | 6 | 8 | 7 | 0 | 9 | T | E |
| 2 | 3 | 1 | 4 | 5 | 8 | 6 | 0 | 7 | T | 9 | E |
| 3 | 2 | 4 | 1 | 8 | 5 | 0 | 6 | T | 7 | E | 9 |
| 2 | 3 | 4 | 8 | 1 | 0 | 5 | T | 6 | E | 7 | 9 |
| 3 | 2 | 8 | 4 | 0 | 1 | T | 5 | E | 6 | 9 | 7 |
| 3 | 8 | 2 | 0 | 4 | T | 1 | E | 5 | 9 | 6 | 7 |
| 8 | 3 | 0 | 2 | T | 4 | E | 1 | 9 | 5 | 7 | 6 |
| 8 | 0 | 3 | T | 2 | E | 4 | 9 | 1 | 5 | 6 | 7 |
| 0 | 8 | T | 3 | E | 2 | 9 | 4 | 5 | 1 | 7 | 6 |
| 0 | T | 8 | E | 3 | 9 | 2 | 5 | 4 | 7 | 1 | 6 |
| T | 0 | E | 8 | 9 | 3 | 2 | 4 | 5 | 7 | 6 | 1 |
| T | E | 0 | 9 | 8 | 2 | 3 | 5 | 4 | 6 | 7 | 1 |
| E | T | 9 | 0 | 2 | 8 | 3 | 4 | 5 | 6 | 1 | 7 |
| E | 9 | T | 2 | 0 | 3 | 8 | 5 | 4 | 1 | 6 | 7 |
| 9 | E | 2 | T | 3 | 0 | 5 | 8 | 1 | 4 | 7 | 6 |
| 9 | 2 | E | 3 | T | 5 | 0 | 1 | 8 | 4 | 6 | 7 |
| 2 | 9 | 3 | E | 5 | T | 0 | 4 | 8 | 7 | 6 | |
| 2 | 3 | 9 | 5 | E | T | 4 | 0 | 7 | 8 | 6 | |
| 3 | 2 | 5 | 9 | 1 | E | 4 | T | 7 | 0 | 6 | 8 |
| 2 | 3 | 5 | 1 | 9 | 4 | E | 7 | T | 6 | 0 | 8 |
| 3 | 2 | 5 | 4 | 9 | 7 | E | 6 | T | 8 | 0 | |
| 3 | 1 | 2 | 4 | 5 | 7 | 9 | 6 | E | 8 | T | 0 |
| 3 | 2 | 5 | 4 | 7 | 6 | 9 | 8 | E | 0 | T | |
| 1 | 3 | 5 | 2 | 7 | 4 | 9 | 6 | E | 8 | T | 0 |

A

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|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 4 | 3 | 6 | 5 | |
| 1 | 2 | 4 | 6 | 3 | 5 |
| 2 | 6 | 4 | 5 | 3 | |
| 2 | 6 | 4 | 3 | 5 | |
| 6 | 2 | 4 | 5 | 3 | |
| 2 | 6 | 4 | 3 | 5 | |
| 6 | 2 | 4 | 5 | 3 | |
| 2 | 6 | 4 | 5 | 3 | |
| 6 | 2 | 5 | 4 | 3 | |
| 2 | 6 | 4 | 5 | 3 | |
| 6 | 2 | 5 | 4 | 3 | |
| 6 | 5 | 2 | 3 | 4 | 1 |

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A2

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 7 |
| 2 | 6 | 4 | 8 | 3 | 7 | 5 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 7 | |
| 6 | 2 | 4 | 8 | 3 | 7 | 5 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 7 | |
| 6 | 2 | 4 | 8 | 3 | 7 | 5 | |
| 2 | 6 | 4 | 8 | 7 | 3 | 5 | |
| 6 | 2 | 8 | 4 | 7 | 5 | 3 | |
| 2 | 6 | 4 | 8 | 7 | 3 | 5 | |
| 6 | 2 | 8 | 4 | 7 | 5 | 3 | |
| 6 | 8 | 2 | 7 | 4 | 5 | 1 | 3 |
| 8 | 6 | 7 | 2 | 5 | 4 | 3 | 1 |
| 6 | 8 | 2 | 7 | 4 | 5 | 3 | |
| 8 | 6 | 7 | 2 | 5 | 4 | 3 | |
| 8 | 7 | 6 | 5 | 2 | 3 | 4 | 1 |

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A2

* Incomplete See p. 218.

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|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |

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| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 2 | 6 | 4 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 6 | 2 | 4 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 6 | 2 | 4 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 2 | 6 | 4 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 6 | 2 | 8 | 4 | 0 | 9 | 3 | 7 | 5 | |
| 2 | 6 | 4 | 8 | 1 | 0 | 3 | 9 | 5 | 7 |
| 6 | 2 | 8 | 4 | 0 | 1 | 9 | 3 | 7 | 5 |
| 6 | 8 | 2 | 0 | 4 | 9 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 2 | 9 | 4 | 7 | 1 | 5 | 3 |
| 6 | 8 | 2 | 0 | 4 | 9 | 1 | 7 | 3 | 5 |
| 8 | 6 | 0 | 2 | 9 | 4 | 7 | 1 | 5 | 3 |
| 8 | 0 | 6 | 9 | 2 | 7 | 4 | 5 | 1 | 3 |
| 0 | 8 | 9 | 6 | 7 | 2 | 5 | 4 | 3 | |
| 8 | 0 | 6 | 9 | 2 | 7 | 4 | 5 | 1 | 3 |
| 0 | 8 | 9 | 6 | 7 | 2 | 5 | 4 | 3 | |
| 0 | 9 | 8 | 7 | 6 | 5 | 2 | 3 | 4 | 1 |

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A2

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 2 | 6 | 4 | 8 | 3 | 0 | 5 | T | 7 | E | 9 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | |
| 6 | 2 | 4 | 8 | 3 | 0 | 5 | T | 7 | E | 9 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | |
| 6 | 2 | 4 | 8 | 3 | 0 | 5 | T | 7 | E | 9 | |
| 2 | 6 | 4 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 2 | 8 | 4 | 0 | 7 | 3 | E | 5 | 9 | 7 | |
| 2 | 6 | 4 | 8 | 1 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 2 | 8 | 4 | 0 | 1 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 2 | 0 | 4 | T | 1 | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 2 | T | 4 | E | 9 | 3 | 7 | 5 | |
| 6 | 8 | 2 | 0 | 4 | T | E | 3 | 9 | 5 | 7 | |
| 8 | 6 | 0 | 2 | T | 4 | E | 1 | 9 | 3 | 7 | 5 |
| 8 | 0 | 6 | T | 2 | E | 4 | 9 | 1 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 2 | 9 | 4 | 7 | 1 | 5 | 3 |
| 8 | 0 | 6 | T | 2 | E | 4 | 9 | 1 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 2 | 9 | 4 | 7 | 1 | 5 | 3 |
| 0 | T | 8 | E | 6 | 9 | 2 | 7 | 4 | 5 | 1 | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 2 | 5 | 4 | 3 | |
| 0 | T | 8 | E | 6 | 9 | 2 | 7 | 4 | 5 | 1 | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 2 | 5 | 4 | 3 | |
| T | E | 0 | 9 | 8 | 7 | 6 | 5 | 2 | 3 | 4 | 1 |

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B.

| | | | | | |
|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | | 4 | 3 | 6 | 5 |
| 1 | 2 | 4 | 6 | 3 | 5 |
| 2 | | 6 | 4 | 5 | 3 |
| 2 | 6 | | 4 | 3 | 5 |
| 6 | 2 | | | 5 | 3 |
| 6 | 2 | | | 4 | 3 |
| 2 | 6 | | | 4 | 5 |
| 6 | 2 | 4 | 8 | | 3 |
| 6 | 2 | 4 | 5 | | 3 |
| 2 | 6 | 8 | 4 | | 3 |
| 6 | 2 | 8 | 4 | | 3 |
| 6 | 5 | 2 | 3 | 4 | |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | | 4 | 3 | 6 | 5 | 8 | 7 |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 7 |
| 2 | | 6 | 4 | 8 | 3 | 7 | 5 |
| 2 | 6 | | 4 | 3 | 8 | 5 | 7 |
| 6 | 2 | | | 8 | 3 | 7 | 5 |
| 6 | 2 | | | 4 | 3 | 8 | 5 |
| 2 | 6 | | | 8 | 3 | 7 | 5 |
| 6 | 2 | 4 | 8 | | 7 | 3 | 5 |
| 6 | 2 | 4 | 8 | | 7 | 5 | 3 |
| 2 | 6 | 8 | 4 | | 7 | 3 | 5 |
| 6 | 2 | 8 | 4 | | 7 | 5 | 3 |
| 6 | 8 | 2 | 7 | 4 | 5 | | 3 |
| 8 | 6 | 7 | 2 | 4 | 5 | | 3 |
| 6 | 8 | 2 | 7 | 5 | 4 | | 3 |
| 8 | 6 | 7 | 2 | 5 | 4 | | 3 |
| 8 | 7 | 6 | 5 | 2 | 3 | 4 | |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |
| 2 | | 6 | 4 | 8 | 3 | 0 | 5 | 9 | 7 |
| 2 | 6 | | 4 | 3 | 8 | 5 | 0 | 7 | 9 |
| 6 | 2 | | | 8 | 3 | 0 | 5 | 9 | 7 |
| 6 | 2 | | | 4 | 3 | 8 | 5 | 0 | 7 |
| 2 | 6 | | | 8 | 3 | 0 | 5 | 9 | 7 |
| 6 | 2 | 4 | 8 | | 0 | 3 | 9 | 5 | 7 |
| 6 | 2 | 4 | 8 | | 0 | 9 | 3 | 7 | 5 |
| 2 | 6 | 8 | 4 | | 0 | 3 | 9 | 5 | 7 |
| 6 | 2 | 8 | 4 | | 0 | 9 | 3 | 7 | 5 |
| 6 | 8 | 2 | 0 | 4 | 9 | | 7 | 3 | 5 |
| 8 | 6 | 0 | 2 | 4 | 9 | | 7 | 5 | 3 |
| 6 | 8 | 2 | 0 | 9 | 4 | | 7 | 3 | 5 |
| 8 | 6 | 0 | 2 | 9 | 4 | | 7 | 5 | 3 |
| 8 | 0 | 6 | 9 | 2 | 7 | 4 | 5 | | 3 |
| 0 | 8 | 9 | 6 | 7 | 2 | 4 | 5 | | 3 |
| 8 | 0 | 6 | 9 | 2 | 7 | 5 | 4 | | 3 |
| 0 | 8 | 9 | 6 | 7 | 2 | 5 | 4 | | 3 |
| 0 | 9 | 8 | 7 | 6 | 5 | 2 | 3 | 4 | |

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 2 | | 6 | 4 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 2 | 6 | | 4 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 6 | 2 | | | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 6 | 2 | | | 4 | 3 | 8 | 5 | 0 | 7 | T | 9 |
| 2 | 6 | | | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 6 | 2 | 4 | 8 | | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 2 | 4 | 8 | | 0 | T | 3 | E | 5 | 9 | 7 |
| 2 | 6 | 8 | 4 | | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 2 | 8 | 4 | | 0 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 2 | 0 | 4 | T | | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 2 | 4 | T | | E | 9 | 3 | 7 | 5 |
| 6 | 8 | 2 | 0 | T | 4 | | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 2 | T | 4 | | E | 9 | 3 | 7 | 5 |
| 8 | 0 | 6 | T | 2 | E | 4 | 9 | | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 2 | 4 | 9 | | 7 | 5 | 3 |
| 8 | 0 | 6 | T | 2 | E | 9 | 4 | | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 2 | 9 | 4 | | 7 | 5 | 3 |
| 0 | T | 8 | E | 6 | 9 | 2 | 7 | 4 | 5 | | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 2 | 4 | 5 | | 3 |
| 0 | T | 8 | E | 6 | 9 | 2 | 7 | 5 | 4 | | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 2 | 5 | 4 | | 3 |
| T | E | 0 | 9 | 8 | 7 | 6 | 5 | 2 | 3 | 4 | |

C.

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|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 |
| 2 | 4 | 3 | 6 | 5 | |
| 2 | 4 | 6 | 3 | 5 | |
| 2 | 6 | 4 | 5 | 3 | |
| 2 | 6 | 4 | 3 | 5 | |
| 6 | 2 | 4 | 5 | 3 | |
| 6 | 2 | 4 | 3 | 5 | |
| 2 | 6 | 4 | 5 | 3 | |
| 6 | 2 | 4 | 5 | 3 | |
| 6 | 4 | 2 | 5 | 3 | |
| 4 | 6 | 5 | 2 | 3 | |
| 6 | 4 | 5 | 2 | 3 | |
| 6 | 5 | 4 | 3 | 2 | 1 |

*A2

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 6 | 4 | 8 | 3 | 7 | 5 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 7 | |
| 6 | 2 | 4 | 8 | 3 | 7 | 5 | |
| 6 | 2 | 4 | 3 | 8 | 5 | 7 | |
| 2 | 6 | 4 | 8 | 3 | 7 | 5 | |
| 6 | 2 | 4 | 8 | 7 | 3 | 5 | |
| 6 | 4 | 2 | 8 | 7 | 3 | 5 | |
| 4 | 6 | 8 | 2 | 7 | 3 | 5 | |
| 6 | 4 | 8 | 2 | 7 | 3 | 5 | |
| 6 | 8 | 4 | 7 | 2 | 5 | 3 | |
| 8 | 6 | 7 | 4 | 2 | 5 | 3 | |
| 6 | 8 | 4 | 7 | 5 | 2 | 3 | |
| 8 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |

*A2

* A2 = Completion of A1. p 383

| | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | E | T |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | T | E | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | T | 9 | E | |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 2 | 6 | 4 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 2 | 6 | 4 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 6 | 2 | 4 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 6 | 2 | 4 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 2 | 6 | 4 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 6 | 2 | 4 | 8 | 0 | 3 | 9 | 5 | 7 | |
| 6 | 4 | 2 | 8 | 0 | 9 | 3 | 7 | 5 | |
| 4 | 6 | 8 | 2 | 0 | 3 | 9 | 5 | 7 | |
| 6 | 4 | 8 | 2 | 0 | 9 | 3 | 7 | 5 | |
| 6 | 8 | 4 | 0 | 2 | 9 | 7 | 3 | 5 | |
| 8 | 6 | 0 | 4 | 2 | 9 | 7 | 5 | 3 | |
| 6 | 8 | 4 | 0 | 9 | 2 | 7 | 3 | 5 | |
| 8 | 6 | 0 | 4 | 9 | 2 | 7 | 5 | 3 | |
| 8 | 0 | 6 | 9 | 4 | 7 | 2 | 5 | 3 | |
| 0 | 8 | 9 | 6 | 7 | 4 | 2 | 5 | 3 | |
| 8 | 0 | 6 | 9 | 4 | 7 | 5 | 2 | 3 | |
| 0 | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 | |
| 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |

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*A2

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|---|---|---|---|---|---|---|---|---|---|---|
| 2 | 6 | 4 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 2 | 6 | 4 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 6 | 2 | 4 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 6 | 2 | 4 | 3 | 8 | 5 | 0 | 7 | T | 9 | E |
| 2 | 6 | 4 | 8 | 3 | 0 | 5 | T | 7 | E | 9 |
| 6 | 2 | 4 | 8 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 2 | 8 | 0 | T | 3 | E | 5 | 9 | 7 |
| 4 | 6 | 8 | 2 | 0 | 3 | T | 5 | E | 7 | 9 |
| 6 | 4 | 8 | 2 | 0 | T | 3 | E | 5 | 9 | 7 |
| 6 | 8 | 4 | 0 | 2 | T | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | 2 | T | E | 9 | 3 | 7 | 5 |
| 6 | 8 | 4 | 0 | T | 2 | E | 3 | 9 | 5 | 7 |
| 8 | 6 | 0 | 4 | T | 2 | E | 9 | 3 | 7 | 5 |
| 8 | 0 | 6 | T | 4 | E | 2 | 9 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 2 | 9 | 7 | 5 | 3 |
| 8 | 0 | 6 | T | 4 | E | 9 | 2 | 7 | 3 | 5 |
| 0 | 8 | T | 6 | E | 4 | 9 | 2 | 7 | 5 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 2 | 5 | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 2 | 5 | 3 |
| 0 | T | 8 | E | 6 | 9 | 4 | 7 | 5 | 2 | 3 |
| T | 0 | E | 8 | 9 | 6 | 7 | 4 | 5 | 2 | 3 |
| T | E | 0 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 |

A.

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|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |

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|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 | |
| 4 | 2 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 3 | 6 | 5 | 7 | 8 | 9 | 0 | |
| 4 | 2 | 6 | 3 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 3 | 6 | 5 | 7 | 8 | 9 | 0 | |
| 4 | 2 | 6 | 3 | 5 | 8 | 7 | 0 | 9 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 9 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 9 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 0 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 9 | 0 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 0 | 9 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 9 | 0 | 7 | 1 |

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|---|---|---|---|---|---|---|--|
| 2 | 4 | 3 | 6 | 7 | 5 | 8 | |
| 4 | 2 | 6 | 3 | 5 | 7 | 8 | |
| 2 | 4 | 3 | 6 | 7 | 5 | 8 | |
| 4 | 2 | 6 | 3 | 5 | 7 | 8 | |
| 2 | 4 | 3 | 6 | 5 | 7 | 8 | |
| 4 | 2 | 6 | 3 | 5 | 8 | 7 | |
| 2 | 4 | 3 | 6 | 5 | 7 | 8 | |
| 4 | 2 | 6 | 3 | 5 | 8 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |

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|---|---|---|---|---|---|---|---|---|--|
| 2 | 4 | 3 | 6 | 5 | 8 | 9 | 7 | 0 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 9 | 0 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 9 | 7 | 0 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 9 | 0 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 9 | 0 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 0 | 9 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 7 | 9 | 0 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 0 | 9 | |
| 2 | 4 | 3 | 6 | 8 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 0 | 5 | 9 | 7 | |
| 2 | 4 | 3 | 6 | 8 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 0 | 5 | 9 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 0 | 5 | 9 | 7 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | |

See p.p. 331 - 334
also p.p. 370 - 372.

B.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 2 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 4 | 2 | 1 | 3 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | 1 | 6 | 5 | 8 | 7 |
| 4 | 2 | 3 | 6 | 1 | 5 | 8 | 7 |
| 4 | 3 | 2 | 6 | 8 | 1 | 7 | 5 |
| 3 | 4 | 6 | 2 | 1 | 8 | 5 | 7 |
| 3 | 6 | 4 | 2 | 8 | 1 | 7 | 5 |
| 6 | 3 | 2 | 4 | 8 | 7 | 1 | 5 |
| 6 | 2 | 3 | 4 | 8 | 7 | 1 | 5 |
| 2 | 6 | 4 | 3 | 7 | 8 | 1 | 5 |
| 2 | 4 | 6 | 3 | 7 | 8 | 1 | 5 |

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|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 4 | 2 | 1 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 1 | 6 | 5 | 8 | 7 | 0 | 9 |
| 4 | 2 | 3 | 6 | 1 | 5 | 7 | 8 | 9 | 0 |
| 2 | 4 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 |
| 4 | 2 | 6 | 3 | 5 | 1 | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | 5 | 1 | 8 | 7 | 0 | 9 |
| 4 | 2 | 6 | 3 | 5 | 8 | 1 | 0 | 7 | 9 |
| 2 | 4 | 6 | 5 | 3 | 8 | 0 | 1 | 9 | 7 |
| 4 | 2 | 5 | 6 | 8 | 3 | 0 | 7 | 9 | 1 |
| 2 | 4 | 5 | 8 | 6 | 3 | 0 | 1 | 9 | 7 |
| 4 | 2 | 8 | 5 | 3 | 6 | 0 | 9 | 1 | 7 |
| 2 | 4 | 8 | 3 | 5 | 6 | 0 | 9 | 7 | 1 |
| 4 | 2 | 3 | 8 | 6 | 5 | 9 | 0 | 7 | 1 |
| 2 | 4 | 3 | 6 | 8 | 5 | 9 | 0 | 7 | 1 |

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|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 6 | 7 | 5 | 8 | 1 |
| 4 | 3 | 2 | 6 | 7 | 5 | 8 | 1 |
| 3 | 4 | 6 | 2 | 5 | 7 | 8 | 1 |
| 3 | 6 | 4 | 2 | 5 | 7 | 8 | 1 |
| 6 | 3 | 2 | 4 | 5 | 7 | 8 | 1 |
| 6 | 2 | 3 | 4 | 5 | 8 | 7 | 1 |
| 2 | 6 | 4 | 3 | 5 | 7 | 8 | 1 |
| 2 | 4 | 6 | 3 | 1 | 5 | 8 | 7 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | 1 |
| 2 | 4 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | 1 |

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|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 6 | 3 | 5 | 8 | 9 | 7 | 0 | 1 |
| 2 | 4 | 6 | 5 | 3 | 8 | 9 | 7 | 0 | 1 |
| 4 | 2 | 5 | 6 | 8 | 3 | 7 | 9 | 0 | 1 |
| 2 | 4 | 5 | 8 | 6 | 3 | 7 | 9 | 0 | 1 |
| 4 | 2 | 8 | 5 | 3 | 6 | 7 | 1 | 9 | 0 |
| 2 | 4 | 8 | 3 | 5 | 6 | 7 | 1 | 0 | 9 |
| 4 | 2 | 3 | 8 | 6 | 5 | 7 | 1 | 9 | 0 |
| 2 | 4 | 3 | 6 | 8 | 5 | 7 | 1 | 0 | 9 |
| 4 | 2 | 6 | 3 | 8 | 1 | 5 | 0 | 7 | 9 |
| 2 | 4 | 3 | 6 | 8 | 1 | 5 | 0 | 9 | 7 |
| 4 | 2 | 3 | 6 | 8 | 1 | 5 | 0 | 7 | 9 |
| 2 | 4 | 6 | 3 | 8 | 0 | 5 | 9 | 7 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 2 | 4 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |
| 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 | 1 |

C.

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|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 4 | 5 | 6 | 7 | 8 |
| 1 | 2 | 4 | 3 | 6 | 5 | 8 | 7 |
| 2 | 1 | 4 | 6 | 3 | 8 | 5 | 7 |
| 2 | 4 | 1 | 6 | 8 | 3 | 7 | 5 |
| 4 | 2 | 6 | 1 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 8 | 3 | 7 | 5 | |
| 2 | 4 | 6 | 1 | 3 | 8 | 5 | 7 |
| 4 | 2 | 6 | 3 | 1 | 5 | 8 | 7 |
| 4 | 6 | 2 | 3 | 5 | 7 | 8 | |
| 6 | 4 | 3 | 2 | 1 | 5 | 8 | 7 |
| 6 | 3 | 4 | 2 | 5 | 1 | 7 | 8 |
| 3 | 6 | 2 | 4 | 5 | 7 | 1 | 8 |
| 3 | 2 | 6 | 4 | 5 | 7 | 8 | |
| 2 | 3 | 4 | 6 | 7 | 5 | 1 | 8 |
| 2 | 4 | 3 | 6 | 7 | 5 | 8 | 1 |

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|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 3 | 5 | 6 | 7 | 8 | 9 | 0 |
| 1 | 2 | 3 | 4 | 6 | 5 | 8 | 7 | 0 | 9 |
| 2 | 1 | 4 | 3 | 6 | 8 | 5 | 0 | 7 | 9 |
| 2 | 4 | 1 | 3 | 8 | 6 | 0 | 5 | 9 | 7 |
| 4 | 2 | 3 | | 6 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | | 3 | 8 | 6 | 0 | 5 | 9 | 7 |
| 2 | 4 | 3 | 1 | 6 | 8 | 5 | 0 | 7 | 9 |
| 4 | 2 | 3 | 6 | 1 | 8 | 0 | 5 | 9 | 7 |
| 2 | 4 | 6 | 3 | 8 | | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | | 8 | 0 | 5 | 9 | 7 |
| 2 | 4 | 3 | 6 | 8 | 1 | 5 | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 8 | 5 | 1 | 7 | 0 | 9 |
| 2 | 4 | 6 | 8 | 3 | 5 | 7 | | 9 | 0 |
| 4 | 2 | 8 | 6 | 5 | 3 | | 7 | 0 | 9 |
| 2 | 4 | 8 | 5 | 6 | 3 | 7 | 1 | 9 | 0 |
| 4 | 2 | 5 | 8 | 3 | 6 | 7 | 9 | 1 | 0 |
| 2 | 4 | 5 | 3 | 8 | 6 | 7 | 9 | 0 | 1 |
| 4 | 2 | 3 | 5 | 6 | 8 | 9 | 7 | 1 | 0 |
| 2 | 4 | 3 | 6 | 5 | 8 | 9 | 7 | 0 | 1 |

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|---|---|---|---|---|---|---|---|
| 4 | 2 | 6 | 3 | 7 | 8 | 5 | 1 |
| 4 | 6 | 2 | 3 | 7 | 8 | 5 | 1 |
| 6 | 4 | 3 | 2 | 8 | 7 | 5 | 1 |
| 6 | 3 | 4 | 2 | 8 | 7 | 1 | 5 |
| 3 | 6 | 2 | 4 | 8 | 1 | 7 | 5 |
| 3 | 2 | 6 | 4 | 8 | 5 | 7 | |
| 2 | 3 | 4 | 6 | 8 | 7 | 5 | |
| 2 | 4 | 3 | 6 | 1 | 8 | 5 | 7 |
| 4 | 2 | 3 | 1 | 6 | 5 | 8 | 7 |
| 2 | 4 | 1 | 3 | 5 | 6 | 7 | 8 |
| 2 | 4 | 3 | | 6 | 5 | 8 | 7 |
| 4 | 2 | 1 | 3 | 5 | 6 | 7 | 8 |
| 4 | 1 | 2 | 3 | 6 | 5 | 8 | 7 |
| 1 | 4 | 2 | 6 | 3 | 8 | 5 | 7 |
| 1 | 4 | 2 | 6 | 3 | 8 | 5 | 7 |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | |
| 1 | 4 | 6 | 2 | 8 | 3 | 7 | 5 |
| 1 | 4 | 2 | 6 | 3 | 8 | 5 | 7 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 6 | 3 | 8 | 5 | 9 | 0 | 7 | 1 |
| 2 | 4 | 6 | 8 | 3 | 5 | 9 | 0 | 7 | 1 |
| 4 | 2 | 8 | 6 | 5 | 9 | 0 | 9 | 7 | 1 |
| 2 | 4 | 8 | 5 | 6 | 3 | 0 | 9 | 7 | 1 |
| 4 | 2 | 5 | 8 | 3 | 6 | 0 | | 9 | 7 |
| 2 | 4 | 5 | 3 | 8 | 6 | | 0 | 7 | 9 |
| 4 | 2 | 3 | 5 | 6 | 8 | 0 | | 9 | 7 |
| 2 | 4 | 3 | 6 | 5 | 8 | | 0 | 7 | 9 |
| 4 | 2 | 6 | 3 | 5 | | 8 | 7 | 0 | 9 |
| 2 | 4 | 3 | 6 | | 5 | 7 | 8 | 9 | 0 |
| 4 | 2 | 3 | 6 | 5 | | 8 | 7 | 0 | 9 |
| 2 | 4 | 6 | 3 | | 5 | 7 | 8 | 9 | 0 |
| 4 | 2 | 6 | | 3 | 5 | 8 | 7 | 0 | 9 |
| 2 | 4 | | 6 | 5 | 3 | 7 | 8 | 9 | 0 |
| 4 | 2 | | 6 | 5 | 3 | 7 | 8 | 9 | 0 |
| 4 | 1 | 2 | 6 | 3 | 5 | 8 | 7 | 0 | 9 |
| 1 | 4 | 6 | 2 | 3 | 8 | 5 | 0 | 7 | 9 |
| 4 | 1 | 2 | 6 | 8 | 3 | 0 | 5 | 9 | 7 |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 1 | 4 | 2 | 6 | 3 | 8 | 5 | 0 | 7 | 9 |

D.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 3 | 5 | 4 | 7 | 6 | 8 | |
| 2 | 5 | 3 | 7 | 4 | 8 | 6 | |
| 2 | 5 | 7 | 3 | 8 | 4 | 6 | |
| 2 | 5 | 7 | 8 | 3 | 6 | 4 | |
| 5 | 2 | 7 | 3 | 8 | 4 | 6 | |
| 5 | 2 | 7 | 8 | 3 | 6 | 4 | |
| 2 | 5 | 7 | 3 | 8 | 4 | 6 | |
| 5 | 2 | 7 | 3 | 4 | 8 | 6 | |
| 5 | 7 | 2 | 3 | 4 | 6 | 8 | |
| 7 | 5 | 3 | 2 | 4 | 8 | 6 | |
| 7 | 3 | 5 | 2 | 4 | 6 | 8 | |
| 3 | 7 | 2 | 5 | 4 | 6 | 8 | |
| 3 | 2 | 7 | 4 | 5 | 6 | 8 | |
| 2 | 3 | 4 | 7 | 6 | 5 | 8 | |
| 2 | 4 | 3 | 6 | 7 | 5 | 8 | |

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|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 4 | 3 | 5 | 7 | 6 | 9 | 8 | 0 | |
| 2 | 3 | 4 | 7 | 5 | 9 | 6 | 0 | 8 | |
| 2 | 4 | 3 | 7 | 9 | 5 | 0 | 6 | 8 | |
| 2 | 4 | 3 | 9 | 7 | 0 | 5 | 8 | 6 | |
| 4 | 2 | 3 | 7 | 9 | 5 | 0 | 6 | 8 | |
| 4 | 2 | 3 | 9 | 7 | 0 | 5 | 8 | 6 | |
| 2 | 4 | 3 | 7 | 9 | 5 | 0 | 6 | 8 | |
| 4 | 2 | 3 | 7 | 9 | 0 | 5 | 8 | 6 | |
| 2 | 4 | 7 | 3 | 9 | 5 | 0 | 6 | 8 | |
| 4 | 2 | 7 | 3 | 9 | 0 | 5 | 8 | 6 | |
| 2 | 4 | 3 | 7 | 9 | 5 | 0 | 6 | 8 | |
| 4 | 2 | 7 | 3 | 9 | 5 | 6 | 0 | 8 | |
| 2 | 4 | 7 | 9 | 3 | 5 | 6 | 8 | 0 | |
| 4 | 2 | 9 | 7 | 5 | 3 | 6 | 0 | 8 | |
| 2 | 4 | 9 | 5 | 7 | 3 | 6 | 8 | 0 | |
| 4 | 2 | 5 | 9 | 3 | 7 | 6 | 8 | 0 | |
| 2 | 4 | 5 | 3 | 9 | 6 | 7 | 8 | 0 | |
| 4 | 2 | 3 | 5 | 6 | 9 | 8 | 7 | 0 | |
| 2 | 4 | 3 | 6 | 5 | 8 | 9 | 7 | 0 | |

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|---|---|---|---|---|---|---|--|
| 4 | 2 | 6 | 3 | 7 | 8 | 5 | |
| 4 | 6 | 2 | 7 | 3 | 8 | 5 | |
| 6 | 4 | 7 | 2 | 8 | 3 | 5 | |
| 6 | 7 | 4 | 8 | 2 | 3 | 5 | |
| 7 | 6 | 8 | 4 | 2 | 3 | 5 | |
| 7 | 8 | 6 | 4 | 2 | 5 | 3 | |
| 8 | 7 | 4 | 6 | 2 | 3 | 5 | |
| 8 | 4 | 7 | 6 | 2 | 5 | 3 | |
| 4 | 8 | 7 | 6 | 5 | 2 | 3 | |
| 8 | 4 | 7 | 5 | 6 | 3 | 2 | |
| 8 | 4 | 7 | 6 | 5 | 2 | 3 | |
| 4 | 8 | 7 | 5 | 6 | 3 | 2 | |
| 4 | 8 | 7 | 6 | 5 | 2 | 3 | |
| 4 | 8 | 6 | 7 | 2 | 5 | 3 | |
| 4 | 6 | 8 | 2 | 7 | 3 | 5 | |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 4 | 2 | 6 | 3 | 8 | 5 | 9 | 0 | 7 | |
| 2 | 4 | 6 | 8 | 3 | 9 | 5 | 0 | 7 | |
| 4 | 2 | 8 | 6 | 9 | 3 | 0 | 5 | 7 | |
| 2 | 4 | 8 | 9 | 6 | 0 | 3 | 5 | 7 | |
| 4 | 2 | 9 | 8 | 0 | 6 | 3 | 5 | 7 | |
| 2 | 4 | 9 | 0 | 8 | 6 | 3 | 7 | 5 | |
| 4 | 2 | 0 | 9 | 6 | 8 | 3 | 5 | 7 | |
| 2 | 4 | 0 | 6 | 9 | 8 | 3 | 7 | 5 | |
| 4 | 2 | 6 | 0 | 9 | 8 | 7 | 3 | 5 | |
| 2 | 4 | 0 | 6 | 9 | 7 | 8 | 5 | 3 | |
| 4 | 2 | 0 | 6 | 9 | 8 | 7 | 3 | 5 | |
| 2 | 4 | 6 | 0 | 9 | 7 | 8 | 5 | 3 | |
| 4 | 2 | 6 | 1 | 0 | 9 | 8 | 7 | 3 | 5 |
| 2 | 4 | 6 | 9 | 0 | 7 | 8 | 5 | 3 | |
| 2 | 4 | 6 | 0 | 9 | 8 | 7 | 3 | 5 | |
| 4 | 2 | 6 | 0 | 9 | 8 | 7 | 3 | 5 | |
| 4 | 6 | 2 | 0 | 8 | 9 | 3 | 7 | 5 | |
| 4 | 2 | 6 | 8 | 0 | 3 | 9 | 5 | 7 | |
| 4 | 6 | 2 | 8 | 3 | 0 | 5 | 9 | 7 | |
| 4 | 2 | 6 | 3 | 8 | 0 | 7 | 9 | | |

Extension by adding to the number of
Horntis. The nature of cyclical
 movement is such that, every method
 in which the main construction consists
 of Horntis and Extreme Pells, can be
 extended by adding to the number of
 the Horntis in arithmetical progression.
 As the expansion of the Plain Principle
 is equal, the capacity of Plain methods
 to extend in this way is entirely
 unrestricted. The formula on page 394
 will so far as the Horntis are concerned
 apply to every one of these methods. If
 we examine the Example given on
 p. 297 we shall see that as the number
 of Extreme Pells remains constant on
 all numbers, the room available for
 making Conditional and Additional
 Shunt remains constant also. This
 room consists of four triangles, and
 the relationships between these triangles
 remains the same. And if, as in that
 example, we retain the same symbols
 for the Extreme Pells on all numbers
 we find that the work within these
 triangles is represented by exactly the
 same figures. I have dealt with this

Form of Extension at Considerable Length
and detail in an article in the Bell
News on Odd and Even Bell Methods.

Methods on the Treble Bob and other
Principles can also be extended by
adding to the Hunts; but as the expansion
of those Principles is unequal such
Extension is, to some extent, restricted.

It is a general Law that all Treble
Bob Methods will extend by adding
to the Hunts five at a time, the
number of Hunts being in either of
the following progressions -

1 3 5 7 9 11 13 →

2 4 6 8 10 12 14 →

Since, however, the number of Sections
increases in regular ratio, but the number
of Hunts, designed to counteract the
natural falseness of those Sections,
remains constant, any Extension of
a Treble Bob Method by adding to the
Hunts must contain repetition of Rows.
The following are five examples. It will
be seen that in the case of London this
falseness at once appears. In the case
of Cambridge it does not appear until
twelve bells are reached.

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | | 3 | 5 | 4 | 7 | 6 | 8 |
| 3 | 2 | | 3 | 7 | 4 | 8 | 6 |
| 4 | 1 | 5 | 7 | 3 | 8 | 4 | 6 |
| 5 | 2 | 5 | 1 | 7 | 8 | 3 | 6 |
| 6 | 5 | 7 | | 3 | 8 | 4 | 6 |
| 7 | 5 | 2 | | 7 | 8 | 3 | 6 |
| 8 | 2 | 5 | 7 | 3 | 8 | 4 | 6 |
| 9 | 5 | 2 | 7 | 3 | 1 | 4 | 8 |
| 0 | 5 | 7 | 2 | 3 | 4 | 6 | 8 |
| 1 | 7 | 5 | 3 | 2 | 4 | 8 | 6 |
| 2 | 7 | 3 | 5 | 2 | 4 | 6 | 8 |
| 3 | 7 | 2 | 5 | 4 | 6 | 8 | 1 |
| 4 | 9 | 2 | 7 | 4 | 5 | 6 | 8 |
| 5 | 7 | 3 | 4 | 7 | 6 | 5 | 1 |
| 6 | 2 | 4 | 3 | 6 | 7 | 5 | 8 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | | 4 | 8 | 5 | 7 | 6 | 9 | 8 | 0 |
| 3 | 1 | 2 | 3 | 4 | 7 | 5 | 9 | 6 | 0 |
| 4 | 1 | 4 | 3 | 7 | 9 | 5 | 0 | 6 | 8 |
| 5 | 2 | 4 | 1 | 7 | 3 | 9 | 0 | 5 | 8 |
| 6 | 4 | 2 | 7 | 9 | 3 | 5 | 0 | 6 | 8 |
| 7 | 4 | 7 | 2 | 9 | 1 | 5 | 3 | 6 | 0 |
| 8 | 4 | 9 | 2 | 5 | 6 | 3 | 8 | 0 | |
| 9 | 4 | 5 | 9 | 7 | 5 | 3 | 6 | 0 | 8 |
| 0 | 4 | 7 | 9 | 2 | 5 | 1 | 6 | 3 | 8 |
| 1 | 4 | 9 | 5 | 2 | 6 | 1 | 8 | 3 | 0 |
| 2 | 7 | 9 | 4 | 5 | 6 | 2 | 8 | 1 | 0 |
| 3 | 9 | 7 | 5 | 4 | 6 | 8 | 3 | 0 | |
| 4 | 9 | 5 | 7 | 4 | 6 | 2 | 8 | 1 | 0 |
| 5 | 9 | 4 | 7 | 6 | 8 | 2 | 0 | 1 | 3 |
| 6 | 5 | 4 | 9 | 6 | 7 | 8 | 0 | 2 | 1 |
| 7 | 4 | 5 | 6 | 9 | 8 | 7 | 2 | 0 | 1 |
| 8 | 4 | 6 | 5 | 8 | 9 | 7 | 0 | 2 | 1 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 4 | 2 | 6 | 3 | 7 | 8 | 5 | 1 |
| 4 | 6 | 2 | 7 | 3 | 8 | 5 | 1 |
| 6 | 4 | 7 | 2 | 8 | 3 | 5 | 1 |
| 6 | 7 | 4 | 8 | 2 | 3 | 1 | 5 |
| 7 | 6 | 8 | 4 | 2 | 1 | 3 | 5 |
| 7 | 8 | 6 | 4 | 1 | 2 | 5 | 3 |
| 8 | 7 | 4 | 6 | 2 | 1 | 3 | 5 |
| 8 | 4 | 7 | 6 | 1 | 2 | 5 | 3 |
| 4 | 8 | 7 | 6 | 5 | 2 | 3 | |
| 8 | 4 | 7 | 5 | 6 | 3 | 2 | |
| 8 | 4 | 7 | 6 | 5 | 2 | 3 | |
| 4 | 8 | 7 | 5 | 6 | 3 | 2 | |
| 4 | 1 | 8 | 7 | 6 | 5 | 2 | 3 |
| 1 | 4 | 8 | 6 | 5 | 2 | 5 | 8 |
| 4 | 6 | 8 | 2 | 7 | 3 | 5 | |
| 4 | 6 | 2 | 8 | 3 | 7 | 5 | |
| 4 | 2 | 6 | 3 | 8 | 5 | 7 | |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 6 | 4 | 8 | 5 | 9 | 0 | 7 | 3 | 2 | 1 |
| 6 | 8 | 4 | 9 | 5 | 0 | 8 | 7 | 1 | 2 |
| 8 | 6 | 9 | 4 | 0 | 5 | 7 | 3 | 2 | 1 |
| 8 | 9 | 6 | 0 | 4 | 5 | 3 | 7 | 2 | 1 |
| 9 | 8 | 0 | 6 | 4 | 3 | 5 | 1 | 7 | 2 |
| 9 | 0 | 8 | 6 | 3 | 4 | 1 | 5 | 2 | 7 |
| 0 | 9 | 6 | 8 | 4 | 0 | 5 | 1 | 7 | 2 |
| 0 | 6 | 9 | 8 | 3 | 4 | 1 | 5 | 2 | 7 |
| 6 | 0 | 9 | 8 | 1 | 4 | 2 | 5 | 7 | |
| 9 | 6 | 3 | 9 | 8 | 2 | 4 | 7 | 5 | |
| 0 | 6 | 9 | 8 | 4 | 2 | 5 | 7 | | |
| 6 | 0 | 8 | 9 | 8 | 2 | 4 | 7 | 5 | |
| 8 | 3 | 0 | 9 | 2 | 8 | 7 | 4 | 5 | |
| 3 | 6 | 0 | 2 | 9 | 7 | 8 | 5 | 4 | |
| 6 | 3 | 0 | 9 | 2 | 8 | 7 | 4 | 5 | |
| 6 | 6 | 0 | 2 | 9 | 7 | 8 | 5 | 4 | |
| 3 | 6 | 2 | 9 | 9 | 8 | 7 | 4 | 5 | |
| 3 | 2 | 6 | 0 | 8 | 9 | 4 | 7 | 5 | |
| 3 | 6 | 2 | 8 | 0 | 4 | 9 | 5 | 7 | |
| 3 | 2 | 6 | 8 | 4 | 0 | 5 | 9 | 7 | |
| 4 | 2 | 3 | 6 | 4 | 8 | 5 | 0 | 7 | 9 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 2 | 1 | 3 | 6 | 5 | 8 | 7 | |
| 1 | 2 | 4 | 6 | 3 | 8 | 5 | 7 |
| 2 | 1 | 6 | 4 | 8 | 3 | 7 | 5 |
| 2 | 6 | 1 | 3 | 8 | 5 | 7 | |
| 6 | 2 | 4 | 1 | 8 | 3 | 7 | 5 |
| 6 | 2 | 4 | 8 | 7 | 3 | 5 | |
| 2 | 6 | 4 | 1 | 7 | 8 | 5 | 3 |
| 6 | 2 | 4 | 7 | 1 | 8 | 3 | 5 |
| 2 | 6 | 7 | 4 | 8 | 1 | 5 | 3 |
| 2 | 7 | 6 | 4 | 8 | 3 | 5 | |
| 7 | 2 | 4 | 6 | 8 | 1 | 5 | 3 |
| 2 | 7 | 6 | 4 | 8 | 5 | 1 | 3 |
| 7 | 2 | 4 | 6 | 5 | 8 | 3 | 1 |
| 7 | 4 | 2 | 5 | 6 | 8 | | 3 |
| 4 | 7 | 5 | 2 | 8 | 6 | 3 | 1 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 2 | 1 | 4 | 0 | 6 | 5 | 8 | 7 | 0 | 9 |
| 1 | 2 | 3 | 4 | 6 | 8 | 5 | 0 | 7 | 9 |
| 2 | 1 | 4 | 3 | 8 | 6 | 0 | 5 | 9 | 7 |
| 2 | 4 | 1 | 8 | 3 | 6 | 5 | 0 | 7 | 9 |
| 4 | 2 | 8 | 1 | 6 | 0 | 5 | 9 | 7 | |
| 2 | 4 | 1 | 8 | 3 | 6 | 0 | 9 | 5 | 7 |
| 4 | 2 | 8 | 1 | 6 | 3 | 9 | 0 | 7 | 5 |
| 4 | 8 | 2 | 6 | 1 | 9 | 3 | 0 | 5 | 7 |
| 8 | 4 | 6 | 2 | 9 | | 0 | 8 | 7 | 5 |
| 8 | 4 | 2 | 6 | 1 | 9 | 3 | 0 | 5 | 7 |
| 4 | 8 | 6 | 2 | 9 | 1 | 0 | 3 | 7 | 5 |
| 8 | 4 | 6 | 9 | 2 | 0 | 1 | 7 | 3 | 5 |
| 4 | 8 | 9 | 6 | 0 | 2 | 7 | 1 | 5 | 3 |
| 4 | 9 | 8 | 6 | 2 | 0 | 1 | 7 | 3 | 5 |
| 9 | 4 | 6 | 8 | 0 | 2 | 7 | 1 | 5 | 3 |
| 4 | 9 | 8 | 6 | 0 | 7 | 2 | 5 | 1 | 3 |
| 9 | 4 | 6 | 8 | 7 | 0 | 5 | 2 | 3 | 1 |
| 9 | 6 | 4 | 7 | 8 | 0 | 2 | 5 | 1 | 3 |
| 6 | 9 | 7 | 4 | 0 | 8 | 5 | 2 | 3 | 1 |

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 7 | 4 | 2 | 5 | 6 | 8 | 3 | |
| 4 | 7 | 5 | 2 | 8 | 6 | | 3 |
| 4 | 5 | 7 | 8 | 2 | 6 | 3 | |
| 5 | 4 | 8 | 7 | 6 | 2 | | 3 |
| 4 | 5 | 7 | 8 | 6 | | 2 | 3 |
| 5 | 4 | 8 | 7 | 6 | 3 | 2 | |
| 5 | 8 | 4 | 7 | 6 | | 2 | 3 |
| 8 | 5 | 7 | 4 | 6 | 3 | 2 | |
| 5 | 8 | 7 | 4 | 6 | | 2 | 3 |
| 8 | 5 | | 7 | 6 | 4 | 3 | 2 |
| 8 | 5 | 7 | | 6 | 3 | 4 | 2 |
| 5 | 8 | 1 | 7 | 3 | 6 | 2 | 4 |
| 5 | 8 | 7 | 6 | 3 | 4 | 2 | |
| 5 | 8 | 1 | 7 | 3 | 6 | 2 | 4 |
| 5 | 1 | 7 | 3 | 8 | 2 | 6 | 4 |
| 5 | 3 | 7 | 2 | 8 | 4 | 6 | |
| 1 | 5 | 7 | 3 | 8 | 2 | 6 | 4 |

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 9 | 6 | 4 | 7 | 8 | 0 | 5 | 3 | 2 | 1 |
| 6 | 9 | 7 | 4 | 0 | 8 | 5 | 3 | | 2 |
| 6 | 7 | 9 | 0 | 4 | 8 | 5 | 3 | | 2 |
| 7 | 6 | 0 | 9 | 8 | 4 | 3 | 5 | | 2 |
| 6 | 7 | 9 | 0 | 8 | 5 | 4 | | 3 | 2 |
| 7 | 6 | 0 | 9 | 3 | 8 | | 4 | 2 | 5 |
| 7 | 0 | 6 | 9 | 8 | 5 | 4 | | 3 | 2 |
| 0 | 7 | 9 | 6 | 3 | 8 | | 4 | 2 | 5 |
| 7 | 0 | 9 | 3 | 6 | | 8 | 2 | 4 | 5 |
| 0 | 7 | 3 | 9 | | 6 | 2 | 8 | 5 | 4 |
| 0 | 7 | 9 | 3 | 6 | | 8 | 2 | 4 | 5 |
| 7 | 0 | 3 | 9 | 1 | 6 | 2 | 8 | 5 | 4 |
| 7 | 3 | 0 | | 9 | 2 | 6 | 8 | 4 | 5 |
| 3 | 7 | 0 | | 9 | 8 | 6 | 5 | 4 | |
| 7 | 3 | 0 | | 9 | 2 | 8 | 5 | 6 | 4 |
| 3 | 7 | 0 | | 9 | 5 | 8 | 4 | 6 | |
| 3 | 7 | 2 | 0 | 9 | 8 | 5 | 6 | 4 | |
| 1 | 3 | 2 | 7 | 9 | 0 | 5 | 8 | 4 | 6 |
| 3 | 1 | 7 | 2 | 9 | 5 | 0 | 4 | 8 | 6 |
| 3 | 2 | | 7 | 5 | 9 | 4 | 0 | 6 | 8 |
| 1 | 2 | 3 | | 9 | 5 | 0 | 4 | 8 | 6 |

The progression of the Rows and the Diagram of the Method.

In the Extension of any Method, produced by a progression of Shubis (i.e. of Cyclical Movement), every other essential feature of the Method will also be in progression. The more important of these features are two, which in themselves comprise or imply most of the others. They are the Diagram of the Method (or Skeleton Cause) and the Rows. The first represents the work of an individual bell; the other the Combined result of the works of all the bells. No Extension can claim to be a true Extension in which these two are not in progression.

It is the fashion to say that an Extension must be the same Method, but on a larger number of bells; and in a very real sense this is strictly true. We can define a Method as an abstract entity consisting of certain rules for producing movement among the bells, which has a greater or less capacity for expressing itself on different numbers. The expressions

will differ somewhat, the thing itself
 always remains the same. Hence we
 get the "essential" and the "accidental"
 features of a method. When you come
 to think of it, this is how in a misty
 and undefined way an ordinary ringer
 does consider a method. Medman is to
 him, not merely, the sum of Medman
 Doubles, Triples, Quads and Complexes. It is
 something wider, which is behind them, and
 of which they are the expressions under
 peculiar circumstances. But directly
 the ringer tries to reduce this vague idea
 to something definite, he goes astray and
 gets involved in errors and contradictions.
 When he comes to put his Extension down
 on paper he talks about the work being
 the same, the Lead Ends the same and
 so forth. But, quite obviously, a Row of
 six bells cannot be the same as a Row
 of four bells. Hence though the idea that
 men are trying to express is, in the main,
 a sound one, yet the accepted statement
 that "an Extension must have the same Lead
 Ends as its original" is quite unscientific.
 Even if, as I did, you substitute for the
 word "same" the more plastic word "equivalent,"

you shift the difficulty rather than remove it. For the truth is that no Row has an exact equivalent on a higher number. Even if we admit (as I do not) that given 135264 as the six bell Lead End, the eight bell Lead End must be 3527486 ; and given 142635 as the six bell Lead End, the eight bell Lead End must be 14263857 - how are we to decide what is the same on eight that 64523 is on six?

Is it to be 6482735 or 8674523 ? And if either how can we tell that there is not a third or that there are not alternatives in the first two instances given?

These difficulties disappear when we consider an Extension as a progression but there are still things which require explanation

| | | | |
|---|----------|----|----------|
| A | 342 | B. | 423 |
| | 3524 | | 4253 |
| | 35264 | | 42635 |
| | 352746 | | 426375 |
| | 3527486 | | 4263857 |
| | 35274968 | | 42638597 |

These quite obviously are in progression.
So too are the following -

C. 3 4 2
 5 6 3 4 2
 7 8 5 6 3 4 2
 9 0 7 8 5 6 3 4 2
 E T 9 0 7 8 5 6 3 4 2.

But now take the following -

| | | | |
|---|-----------------------|---|-------------------|
| D | 4 2 3 | E | 3 4 2 |
| | 5 4 3 2 | | 5 4 3 2 |
| | 5 6 3 4 2 | | 6 4 5 2 3 |
| | 5 7 3 6 2 4 | | 6 4 7 2 5 3 |
| | 5 7 3 8 2 6 4 | | 6 4 8 2 7 3 5 |
| F | 6 4 5 2 3 | G | 5 6 3 4 2 |
| | 7 8 5 6 3 4 2 | | 8 6 7 4 5 2 3 |
| | 7 9 5 0 3 8 2 6 4 | | 8 6 0 4 9 2 7 3 5 |
| | 7 9 5 E 3 T 2 0 4 8 6 | | |

If these were merely arithmetical figures it might be rather difficult to say that they are all true progressions throughout. It might be rather difficult for instance to justify the position of 4 2 3 in D or 3 4 2 in E. But they are not merely arithmetical figures. They are symbols which stand for the positions of moving

bells. They must be read in connection with the previous Lead End and the Coursing Order of the Method. Rounds is assumed to be the previous Lead End in each case. At that point the bell Coursing two positions in front of the Treble is, on four bells, the 4th; but on all other numbers the 5th again; the first bell in the series E represents on four bells, the bell Coursing next before the Treble; on five bells the bell Coursing (at the previous Lead End) two positions in front of the Treble; on six bells, three positions in front; on seven bells, four positions in front. These bells are represented by the figure 3 on four bells, 5 on five bells, and 6 on all other numbers. Read with reference to Coursing Order all these series of Lead Ends are in strict progression.

It is in this sense and in this sense alone that a Method and its Extensions must have the same Lead Ends.

Having agreed that an Extension must have the same Lead Ends as its original, most Composers are content to let the

matter rest there. What happens to the interior Rows is with them largely a matter of chance. But apart from its position, and apart from the fact that open it may stand for the signature of the Lead, as the Cause End does of the Cause, there is no real reason why the Lead End should be treated as different from any other Row. If it must be in a progression, so must they.

But the expansion of a method is unequal, it may have several factors, and this necessarily results in the progression of the internal Rows being more or less involved. Especially is this the case where those Rows are the result of one or more Add: Shunts.

H 4 2 6 3 7 8 5
 4 2 6 3 8 5 9 0 7
 4 2 6 3 8 5 0 12 12 9.
 4 2 6 3 8 5 0 12 13 14 11
 4 2 6 3 8 5 0 7 12 9 14 11 15 16 13
 4 2 6 3 8 5 0 7 12 9 14 11 16 13 17 18 15

These are the Half Lead Ends of the Extension of London Major given on page 389. It is

not difficult to see that these are in a line progression, (though not in so simple a one as the series A to G), nor to trace from the figures on pp 386-9 the effect of the various shunts.

The Half Lead Ends of Cambridge are in a more involved progression -

J 2 5 6 4 3
 7 4 2 5 6 8 3
 4 7 0 8 2 5 6 9 3
 11 8 4 7 0 12 2 5 6 9 3

This progression can perhaps best be understood as follows. -

x 3 2 4 6 5
 3 2 4 6 8 7 5
 3 2 4 6 8 0 9 7 5
 3 2 4 6 8 0 T E 9 7 5

y. 3 6 2 5 4
 3 6 2 7 4 5 8
 3 6 2 0 4 7 8 5 9
 3 6 2 0 4 E 8 7 T 5 9

x is the Couising Order of the previous Lead End.

In x mark the fourth bell and every alternate bell following, as well as the last bell. Then write the figures down, alternately a plain figure and a marked figure. This will give y , which is the Counting Order of 1, the Half Lead End. Why x should be so marked can be seen by examining the method and the effect of its Shunts.

Similarly it will be found that in a fine Extension all the internal Rows will be in a more or less involved progression. It will sometimes be well to consider the part of the Row above or below the Hunt by itself, and afterwards adjust the relationship of the two Halves.

The first of the following examples is from the Extension of Durham Surprise Minor p. 385; the two following from the Extension of London Surprise Major p. 389.

Progression of Rows.

| No. of Bells | No. of Row | Row. |
|--------------|------------|--|
| 6 | 10th | 6 4 2 5 3 1 |
| 8 | 10th | 6 4 2 8 7 1 5 3 |
| 10 | 10th | 6 4 2 8 0 1 9 3 7 5 |
| 12 | 10th | 6 4 2 8 0 1 7 3 E 5 9 7 |
| 14 | 10th | 6 4 2 8 0 1 12 3 14 5 13 7 9 11. |
| <hr/> | | |
| 8 | 8th | 2 5 7 1 3 8 4 6 |
| 10 | 12th | 2 4 3 7 9 1 5 0 6 8 |
| 12 | 16th | 2 4 3 6 5 9 11 1 7 12 8 0 |
| 14 | 20th | 2 4 3 6 5 8 7 11 13 1 9 14 0 12 |
| 16 | 24th | 2 4 3 6 5 8 7 10 9 13 15 1 11 16 12 14 |
| <hr/> | | |
| 8 | 12th | 7 3 5 2 4 1 6 8 |
| 10 | 16th | 2 4 9 5 7 3 6 1 8 0 |
| 12 | 20th | 2 4 3 6 11 7 9 5 8 1 0 12 |
| 14 | 24th | 2 4 3 6 5 8 13 9 11 7 0 1 12 14 |
| 16 | 28th | 2 4 3 6 5 8 7 0 15 11 13 9 12 1 14 16 |
| Ad. int. | | |

The progression of the Diagram of the Method. More important even than the progression of the Rows, it is, that the Diagram of the Method should be in a line progression, in an Extension. For this represents the movement - the work - of the bells, which alike in theory and in practice is the really essential feature.

Men say that in an Extension, the Work must be the same as in the original. But in any strict sense of the word this is impossible. Even in the obvious Extensions of the simple Methods you will find features which are altered. As in Stedman where on five bells, one plain hunt is from front to back, and from back to front; but does not do so on any other number. Or in Cambridge where in Minor and Major a bell does the same thing, but not on any other number. Or in Forward where the Minor is double but ~~the~~ Extension to other numbers is not. You cannot have the same work in an Extension; what you can have is a progression of the work. As Expansion is unequal, and there may be more than one factor in the progression, the progression will in no

* page 279.

Case be a simple one, and in many cases will be a very involved one.

As a result of the inequality of expansion the relative prominence of some work will differ in the various members of an Extension. We saw that this is so in Forward*. Equally it is so in Kent. Another good example of this is in the Extension of London given on p. 389. Anyone who has rung London, or who has examined the method analytically, cannot fail to have noticed that, superficially, the most prominent feature of the Major is plain backward hunting. In the Extension I have given the relative prominence of this backward hunting steadily decreases, till on a very large number of bells it appears almost insignificant. On the other hand the relative prominence of dragging steadily increases. Almost unnoticed on eight, it becomes on the higher numbers, superficially, the most prominent feature. In this the Extension is obeying a general law, inherent in the nature of a progression of Stents, and more or less common to all Extensions; especially of Methods which contain additional Stents.

In actual ringing there are many features which necessarily have great prominence and are really of great importance, but which in their nature belong to the accidental and not to the essential part of the Method. Such are those which I have mentioned in connection with Stedman, Cambridge, and Forward. And such too are many familiar features of other Methods. For, by the essential nature of ringing, all work is resolvable into Forward and Backward movement, either on all the bells or on a sectional part of them. This includes all Places whether internal or external. A Whole Turn is only three steps of Forward hunting, followed by three steps of Backward hunting, or vice versa. The same Combined movement produces the Half Turn, and the Single Fourth or Single Fifth of Bristol. The difference is merely in the position of the bells involved. Again the 6-5-6 and the Long Work of London are the result of partly forward Treble Bar hunting and partly plain hunting backward. And since expansion is unequal, it may well be that a fine

12. The same that produces the Whole Turn.

* "Duffield" page 5. For many years I held a similar opinion which led me to doubt if the Extension were, even in theory, a sound one.

progression of movement will fail to reproduce these features exactly as in the original. A good example of this is found in the case of Double Norwich. The Exercise has generally agreed that on paper at any rate, Double Norwich Major, Royal, and Mascinus are the same Method. But so far as practice is concerned, many ringers, perhaps the majority, would agree with Sir Arthur Heywood in saying that "the relationships of Major to Royal and Mascinus is so slight as to make them to all intents and purposes different methods" * Yet the extension of the movement is in a perfect progression, and provided the accidental features are ignored a set of rules can be had by which all three can equally well be rung. In the same way that many men ring Plain Bob Minor and Major, i.e. by counting the steps of plain hunting between the dodges. Rightly to judge of the movement of the bells in an Extension, one should have full diagrams of the Method on at least three numbers of bells, preferably more.

I cannot give such diagrams here, considerations of space forbid; but I give some formulae showing the progressions of movement in the Extensions of various methods.

These progressions are of increasing complexity, and naturally the progressions of some other Extensions will be much more involved still. They will not however differ in nature from those given. As each term represents the path of a bell it must be read cyclically.

Formulae of the Progression of Work.

In the following Forward Hunting is marked +, Backward Hunting - External Places are included in the Forward and Backward Hunting Internal Places which are part of hunting on a sectional number of bells are for convenience specially marked.

E = The Internal Place of an Extreme Hunt

C = The two Places of a Court Hunt with the movement joining them.

K = A pair of Kent Places (i.e. three steps of backward hunting in two positions).

P = Three steps of Forward Movement in the first two positions i.e. Seconds and a whole Pull Before.

T. = +3-1 i.e. ordinary Treble Bob Hunting

1. PLAIN BOB. one Hunt.

No of Bells

| | | | |
|----|---|----------------|-----|
| 4 | E | $(+7-1)^2$ | +7 |
| 5 | E | $(+9-1)^3$ | +9 |
| 6 | E | $(+11-1)^4$ | +11 |
| 7 | E | $(+13-1)^5$ | +13 |
| 8 | E | $(+15-1)^6$ | +15 |
| 9 | E | $(+17-1)^7$ | +17 |
| 10 | E | $(+19-1)^8$ | +19 |
| 11 | E | $(+21-1)^9$ | +21 |
| 12 | E | $(+23-1)^{10}$ | +23 |

Ad mt.

2 FORWARD

| | | | | | | | | | | | |
|----|---|----|----|----|----|----|---|----|----|---------------|----|
| 6 | K | +2 | -1 | +3 | -1 | +2 | K | +2 | -1 | $(+3-1)^1$ | +2 |
| 8 | K | +2 | -1 | +3 | -1 | +2 | K | +2 | -1 | $(+3-1)^3$ | +2 |
| 10 | K | +2 | -1 | +3 | -1 | +2 | K | +2 | -1 | $(+3-1)^5$ | +2 |
| 12 | K | +2 | -1 | +3 | -1 | +2 | K | +2 | -1 | $(+3-1)^7$ | +2 |
| 14 | K | +2 | -1 | +3 | -1 | +2 | K | +2 | -1 | $(+3-1)^9$ | +2 |
| 16 | K | +2 | -1 | +3 | -1 | +2 | K | +2 | -1 | $(+3-1)^{11}$ | +2 |
| 18 | K | +2 | -1 | +3 | -1 | +2 | K | +2 | -1 | $(+3-1)^{13}$ | +2 |

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| | | | | | | | | | | | | |
|----|-----------|----|----|----|----|----|-----------|----|----|----|----|----|
| 6 | $(K+1)^1$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^1$ | +1 | -1 | +3 | -1 | +2 |
| 8 | $(K+1)^2$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^2$ | +1 | -1 | +3 | -1 | +2 |
| 10 | $(K+1)^3$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^3$ | +1 | -1 | +3 | -1 | +2 |
| 12 | $(K+1)^4$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^4$ | +1 | -1 | +3 | -1 | +2 |
| 14 | $(K+1)^5$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^5$ | +1 | -1 | +3 | -1 | +2 |
| 16 | $(K+1)^6$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^6$ | +1 | -1 | +3 | -1 | +2 |
| 18 | $(K+1)^7$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^7$ | +1 | -1 | +3 | -1 | +2 |
| 20 | $(K+1)^8$ | +1 | -1 | +3 | -1 | +2 | $(K+1)^8$ | +1 | -1 | +3 | -1 | +2 |

5 KENT TREBLE BOB One Hunt.

| | | | | | |
|----|----------|-----------------|------------------|-----------------|------------|
| 6 | +1 -1 +2 | P ⁴ | +1 -1 +2 K +2 -1 | T ² | +6 K +2 -1 |
| 8 | +1 -1 +2 | P ⁶ | +1 -1 +2 K +2 -1 | T ⁴ | +6 K +2 -1 |
| 10 | +1 -1 +2 | P ⁸ | +1 -1 +2 K +2 -1 | T ⁶ | +6 K +2 -1 |
| 12 | +1 -1 +2 | P ¹⁰ | +1 -1 +2 K +2 -1 | T ⁸ | +6 K +2 -1 |
| 14 | +1 -1 +2 | P ¹² | +1 -1 +2 K +2 -1 | T ¹⁰ | +6 K +2 -1 |
| 16 | +1 -1 +2 | P ¹⁴ | +1 -1 +2 K +2 -1 | T ¹² | +6 K +2 -1 |
| 18 | +1 -1 +2 | P ¹⁶ | +1 -1 +2 K +2 -1 | T ¹⁴ | +6 K +2 -1 |
| 20 | +1 -1 +2 | P ¹⁸ | +1 -1 +2 K +2 -1 | T ¹⁶ | +6 K +2 -1 |

| | | | | | | | |
|-----------------|-------|------------------|----------------------|-----------------|------------|-----------------|---------|
| T ² | +7 -1 | (T ³ | +7 -1) ¹ | T ² | +2 K +6 -1 | T ² | +2 K -1 |
| T ⁴ | +7 -1 | (T ⁵ | +7 -1) ³ | T ⁴ | +2 K +6 -1 | T ⁴ | +2 K -1 |
| T ⁶ | +7 -1 | (T ⁷ | +7 -1) ⁵ | T ⁶ | +2 K +6 -1 | T ⁶ | +2 K -1 |
| T ⁸ | +7 -1 | (T ⁹ | +7 -1) ⁷ | T ⁸ | +2 K +6 -1 | T ⁸ | +2 K -1 |
| T ¹⁰ | +7 -1 | (T ¹¹ | +7 -1) ⁹ | T ¹⁰ | +2 K +6 -1 | T ¹⁰ | +2 K -1 |
| T ¹² | +7 -1 | (T ¹³ | +7 -1) ¹¹ | T ¹² | +2 K +6 -1 | T ¹² | +2 K -1 |
| T ¹⁴ | +7 -1 | (T ¹⁵ | +7 -1) ¹³ | T ¹⁴ | +2 K +6 -1 | T ¹⁴ | +2 K -1 |
| T ¹⁶ | +7 -1 | (T ¹⁷ | +7 -1) ¹⁵ | T ¹⁶ | +2 K +6 -1 | T ¹⁶ | +2 K -1 |

6 DOUBLE OXFORD. One Hunt.

(The Formula represents the work of half a Course)

| | | | | | |
|---------|----------------------|----------|-----------------------|-------|---|
| E +3 -1 | (+1 -1) ² | +3 -1 +1 | C(+1 -1) ¹ | +3 -1 | (+1 -1) ² |
| E +3 -1 | (+1 -1) ⁴ | +3 -1 +1 | C(+1 -1) ³ | +3 -1 | (+1 -1) ² +1 C(+1 -1) ¹ |
| E +3 -1 | (+1 -1) ⁶ | +3 -1 +1 | C(+1 -1) ⁵ | +3 -1 | (+1 -1) ² +1 C(+1 -1) ³ |
| E +3 -1 | (+1 -1) ⁸ | +3 -1 +1 | C(+1 -1) ⁷ | +3 -1 | (+1 -1) ² +1 C(+1 -1) ⁵ |

| | | | | |
|-----|-------------|-------|---------|-------------|
| | | | | +3 C |
| 4 | | | | +3 C |
| -1) | | | | +3 C |
| 4 | 1 | 6 | | +3 C |
| -1) | +1 C(+1 -1) | +3 -1 | (+1 -1) | |
| 4 | 3 | 6 | 1 | 8 |
| -1) | +1 C(+1 -1) | +3 -1 | (+1 -1) | +1 C(+1 -1) |
| | | | | +3 -1 |
| | | | | (+1 -1) |
| | | | | +3 C |

Note

In the last Chapter I showed that Capacity for Extension is not an exceptional quality, confined to a small number of Methods, but is a characteristic of most Methods, and is limited only by local Considerations. Further I showed that many Methods have more than one equally valid Extension. The question is still open - How far are these Extensions entitled to be called by the same name as the original? This is outside the scope of the present book. I have shown for instance what are the five Extensions of Bristol Surprise Major, but I do not here and now express any opinion, as to which is Bristol Surprise Royal or whether there is such a Method.



